## Experiment 2: Measurements and Density

## Prelab:

1. Read the How to Make a Good Graph pages in your course packet. An additional section about graphing is in your text, Appendix A. Define "independent" and "dependent" variable, and on what axis they should be placed.
2. Make a graph, BY HAND, on graph paper (in back of this booklet) for the data below, which was determined by finding the mass of a rope that was cut at specific lengths. Make sure that you read the how to make a good graph sections and follow the examples at the end of this document (page 10 or so).

| length $(\mathrm{cm})$ | 10.0 | 15.0 | 20.0 | 25.0 | 30.0 | 35.0 | 45.0 | 55.0 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| mass $(\mathrm{g})$ | 19.1 | 35.2 | 39.9 | 54.4 | 69.6 | 78.8 | 99.7 | 116.4 |

3. Using the graph of the data above, determine the quantitative relationship of mass to length (the slope) and express as a sentence, with measurements and units.
4. Use this information to find the mass of a piece of rope which has the length of your date of birth, in inches.
5. Read the section on density in your text, AND the introduction below. Write a definition for density, and explain why the density of water has a value that is easy to remember.
6. Calculate the density of an object that has a mass of 79.2 g and a volume of $95.2 \mathrm{~cm}^{3}$ ?
7. Read the online directions for using Graduated Cylinders, Pipets and Analytical Balances. http://academic.cuesta.cc.ca.us/gbaxley/chem1A/volume/prelab_reading_for_week_2.htm
What are the proper accuracy levels for graduated cylinders and pipets?

Questions to consider while performing this lab:
$\star$ Do all devices record identical values?
$\star$ Does each piece of chemistry glassware measure volumes to the same precision?
$\star$ Can the density of a solution be determined via a standard calibration curve?

## Introduction:

When writing a measurement:
$\checkmark$ always include both the number (eg. 22.3) and the unit (eg. cm)
$\checkmark$ always write down the correct number of digits (digits that you know plus one estimated).
Your instructor will demonstrate how to determine how many digits to include.

## What is Density, and How is it Useful?

Were you ever caught by the riddle "what weighs more, a pound of feathers or a pound of lead?" They each weigh the same, of course, but ask the joker which they would prefer to have dropped on their foot! The reason why this riddle is amusing is that even though a pound of one
thing weighs the same any other, the density of the lead is much different. The density is a ratio of the mass over the volume for a substance. It is an intensive property, meaning that density doesn't depend on how much of the sample is being measured. The mass any block of lead divided by its volume will yield the same ratio, regardless of the size of the block.

Because most substances increase in volume as their temperature increases while their mass stays constant, the ratio of mass to volume (density) decreases. This is why density is also reported with a temperature. Gasoline is sold on a "per volume" basis. Do you get more mass for your dollar when buying gasoline on cold days or hot days?

Density is fairly easy to measure, and is an important indicator for certain biological fluids. Urine density is analyzed as one indicator of a type of diabetes, and also for dehydration, infection, and renal failure. Blood donors typically have their blood tested by the "float test," where a drop of blood is tested for hemoglobin (and therefore iron) content by observing its density compared to a copper sulfate solution.

Density is also used to express the concentration of solutions. A $5.0 \%$ weight/weight solution of NaCl means that there are 5.0 g of NaCl in 100 g of solution, or 5.0 g of NaCl in 95 g of water. The $5.0 \%$ solution could also be made with 50.0 g of NaCl and 950.0 g of $\mathrm{H}_{2} \mathrm{O}$. We will study other units for concentration later in the year.

In today's lab, you will:

- Analyze student data from different measuring devices to determine if one device is more accurate or precise than the others.
- Determine the density and concentration of a solution by a common analytical method: using a calibration graph made with known volumes and concentrations of solutions.


## Safety:

Although the solutions used today are relatively harmless, GOGGLES and APRONS will be worn at all times. All solutions can be disposed of in the sink.
There is a data sheet at the end of this handout for your measurements. Record all data in INK.

Part 1: Graphing (may be done at any time in lab)
Check out a lap top computer, $\log$ on as $\underline{2105}$ (no password needed) and start Microsoft Excel. Unfamiliar with Excel? There is a step by step Excel guide in the course packet starting on p. 14.

Using an application like Excel is very helpful for science and engineering majors, so if you are not familiar with how to use Excel make sure that you learn today.
Answer the graphing questions on p .11 before leaving lab. Check your answers with your instructor.

## Part 2: Determination of the Concentration of a Solution by Density

## A. Data collection (in class)

1. Rinse and dry 2100 mL beakers and record their masses to the nearest 0.001 g in Table 1. Mark the beakers with tape for easy identification.
2. Obtain about 50 mL of one of the unknown solutions in a clean, dry 150 mL beaker.
3. Using the pipet bulb, fill the 10 mL volumetric pipet with about 2-3 mL of the unknown solution. Rinse the bulb of the pipet with the wash, and discard. Rinse twice more.
4. Using good pipet techniques, fill the pipet with the unknown solution so it's above the etched mark. Wipe the tip of the pipet with paper towel, hold the tip against the beaker, and allow to drain to the mark.
5. Holding the tip of the pipet against the weighing beaker, allow the pipet to drain completely, except for the last drop that does not drain by gravity. Repeat to deliver 10 mL of the solution to the second beaker.
6. Weigh the beakers separately, recording the masses of the beaker + solution.
7. Calculate the masses of the solutions.

## B. Determining the Concentration of the Unknown Solution (in class)

The density of aqueous (dissolved in water) solutions of salts is related to how much of the salt is dissolved in a given amount of water. The densities and of several calcium chloride solutions are provided for you in the table below.

| Percent by mass | 1.00 | 8.50 | 14.00 | 22.00 | 32.00 | 40.00 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Density $(\mathrm{g} / \mathrm{mL})$ | 1.008 | 1.080 | 1.120 | 1.198 | 1.310 | 1.39 |

Using the information in the table, the concentration of any calcium chloride solution can be determined once its density is measured. The density of an unknown solution of $\mathrm{CaCl}_{2}$ will be determined using a pipet. Preparing a calibration graph of the density (easily measured) of the known solutions will allow the concentration of the unknown solutions to be determined.
8. Calculate the density of the unknown solution using your data in Table 1.
9. Check out a laptop computer, $\log$ on as 2105 (no password needed) and start Microsoft Excel. Prepare a graph of the density and concentrations of the calibration solutions above using MS Excel. There is a step by step Excel guide in the course packet starting on p. 14. Each student should prepare their own graph from a blank Excel worksheet DURING class.
10. Before finalizing your graph, consider these questions:
a. What are the independent and dependent variables? Which axes are appropriate?
b. What sort or relationship exists between the density and concentration?
c. Use $\underline{\text { both }}$ an extrapolated line on the graph paper and the equation for the line to determine the concentration of salt in the solutions of unknown concentration.

## Part 3: Comparing the Precision and Accuracy of Two Common Measuring Devices

In a previous semester, students collected density data for two types of Snapple drinks, Regular (sweetened with sugar) and Diet (artificially sweetened). Two measuring devices were used to measure the volumes of the liquids, 50 mL graduated cylinders and 10.00 mL volumetric pipets. The goal of the experiment was to determine which device was more precise, and if there was a difference in densities of the two kinds of drinks.
11. Open the Density Comparison Excel file by opening from the desktop:

My Computer_chemistry on labvol....(Q:)_Baxley_Density Comparison for Accuracy and Precision.xls
12. Use Excel to calculate the average and standard deviations for each of the columns of data. Help with formulas is on page 17.

Name $\qquad$ lab day/section $\qquad$
partner $\qquad$

## Graphing Questions: answer in lab

The temperature of a water sample was measured with 2 thermometers, one in Celsius and the other in Fahrenheit. The design of the experiment was such that the temperature of the water was measured at every $20^{\circ} \mathrm{C}$ increase, as ice water was heated to boiling. The data are given below:

| $\mathrm{T}^{\circ} \mathrm{F}$ | 32 | 68 | 104 | 140 | 176 | 212 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathrm{~T}^{\circ} \mathrm{C}$ | 0 | 20 | 40 | 60 | 80 | 100 |

Prepare a graph for the data above using MS Excel, and answer the following questions about the graph. Make sure to follow the guidelines for using Excel and making good graphs in this lab manual. Print the graph and attach after this page, but do not print with a gray background!

G1. Which is the dependent variable? Why?

G2. Find the linear relationship between ${ }^{\circ} \mathrm{F}$ and ${ }^{\circ} \mathrm{C}$. Record the equation for the line using y and x , and also translate these variables into ${ }^{\circ} \mathrm{F}$ and ${ }^{\circ} \mathrm{C}$. Include correct units.

G3. Explain in words the meaning of the slope and $y$-intercept values determined from your graph.

G4. Using the equation for the line, what value of ${ }^{\circ} \mathrm{F}$ will be equal to $37.0^{\circ} \mathrm{C}$ ? (show your work)

G5. Using the equation for the line, what value of ${ }^{\circ} \mathrm{C}$ will be equal to $145^{\circ} \mathrm{F}$ ? (this is about the threshold temperature of pain for most people)

G6. The equation for calculating the temperature in Kelvin from degrees Celcius is exactly the same as the equation that would describe the best fit line of a graph of temperature in K vs. ${ }^{\circ} \mathrm{C}$. What is the slope of this line?

## Part 2, Unknown $\mathrm{CaCl}_{2}$ Solution

Name $\qquad$
Scientists record all data in INK-no white out!
Table 1: Mass and Volume for Unknown salt solution: attach graph after this page

| Unknown ID: | Trial 1 | Trial 2 |
| :---: | :---: | :---: |
| Mass beaker |  |  |
| Mass beaker + liquid |  |  |
| Mass liquid |  |  |
| Volume |  |  |
| Density |  |  |
| Concentration (\% by mass) <br> (from graph, see procedure section for data) |  |  |

sample calculations for density of unknown and concentration of unknown (from graph):

Using the equation of the line from the graph, what would be the density of a $54.0 \% \mathrm{CaCl}_{2}$ solution? Show your calculation below.

Using the equation of the line from the graph, what is the concentration of a solution with a density of $1.24 \mathrm{~g} / \mathrm{mL}$ ?

## Part 3, Precision and Density Questions:

1. Use the class data to compute the mean (average) density for each data set (each beverage, by each measuring device. See p. 17 in the course packet for how to make Excel do this for you! Enter your results in the table below.

|  | Regular drink |  | Diet drink |  |
| :--- | :---: | :---: | :---: | :---: |
|  | Grad. Cyl. | Pipet | Grad. Cyl. | Pipet |
| Average |  |  |  |  |
| Standard <br> deviation |  |  |  |  |
|  |  |  |  |  |

2. Evaluate the graph showing the ranges of the density data for each of the two measuring devices. Based on the graph, which device is more precise? Cite examples from the data, and include a definition of precision in your answer.
3. Is it possible to determine which device is more accurate? Be specific, and cite data.
4. From the data collected by the class, compare the densities of the diet and regular beverages. Which drink is more dense? (cite data)
5. In terms of the ingredients of drinks sweetened with sugar compared to aspartame (one artificial sweetener), why would the densities be different between regular and diet drinks? This may require some research on your part.
6. Will an object that is 0.332 kg and $42.0 \mathrm{~cm}^{3}$ float in 10.0 L of liquid with a mass of $7.9 \times 10^{3} \mathrm{~g}$ ?
7. A standard issue U.S. Federal Reserve gold bar measures $7.00 \times 3.625 \times 1.75$ inches. If gold has a density of $19.3 \mathrm{~g} / \mathrm{cm}^{3}$, what is the mass of a gold bar in kg and pounds?
8. On a 'Nick at Nite' rerun of McGyver, the villain is shown pushing a snow sled upon which is a pile of gold bars that is about $1 \mathrm{~m}^{3}$ in size. What mass (in pounds) would this stack of gold weigh?
9. Briefly describe the feasibility of the villain pushing the sled full of gold across a field of snow.
10. Gasoline has a density of about $0.680 \mathrm{~g} / \mathrm{mL}$ at $20^{\circ} \mathrm{C}$. What is the mass of 15.0 gal. of gas?

## How to Make a Good Graph

Graphs can be a useful way to represent data (a picture is worth a thousand words). Often just listing the data in a table does not show trends as well as a graph. The ability to draw and interpret graphs is necessary for almost all disciplines.

1. First, make sure that your data is in a convenient form. Prepare a table with the data in columns that are labeled with the type of information and units in that column. For example, column headings might read "time (min)" and "distance (cm)."
2. Not all graphs need to begin at 0,0 . If the data doesn't include numbers close to zero, choose the next lowest number that is easy to use (multiples of 1,2 , or 5 ). Look at the range of numbers to be graphed and choose the best scale interval to fill as much of the page as possible, but using multiples of 1,2 , or 5 . The x and y axis do not need to start at the same value or have the same scales. This is probably the hardest part of making a graph. Label each major gridline (usually the thicker lines) with the appropriate number.
3. Label each axis with the data and units being graphed. The $x$-axis is the horizontal axis and the $y$ axis is the vertical axis. The independent variable goes on the x-axis. That is the variable that you knew before you did the experiment. For example, if I rolled a ball and measured its distance every 30 seconds, "time" would be the independent variable and go on the x-axis and "distance" would be the dependent variable and go on the $y$-axis. Another guide is that the independent variable is the one you are most sure of.
4. Plot the data by drawing a small dot for each data point.
5. If the graph is linear, draw the best straight line through the points with a straight edge. The line may not necessarily run through all, or any, of the points, but is an average of the points. DO NOT simply connect the first data point with the last data point, and DO NOT connect the dots. If the graph is not linear, draw the best smooth curve that you can through the data. Again, do not connect the dots; the curve may not go right through every point.
6. Add a descriptive title to the top of your graph. Describe the experiment; don't just list the variables. Time vs. Temp is not very informative.
7. To determine your slope, find two pairs of points on the line that are near your first and last data point. DO NOT simply use two of your data points, unless they are EXACTLY on the line. Calculate the difference in the values for the y axis points, and then the difference in the x axis points. Divide the y axis difference by the x axis difference.

$$
\begin{aligned}
& \text { slope } \\
& \frac{\mathrm{Y}_{2}-\mathrm{Y}_{1}}{\mathrm{X}_{2}-\mathrm{X}_{1}}=\text { slope (include the units of the } \mathrm{y} \text { and } \mathrm{x} \text { axes) }
\end{aligned}
$$

The slope likely has units! In the graph below, the units are $\mathrm{m} / \mathrm{sec}$, so the slope would be given as $1.5 \mathrm{~m} / \mathrm{sec}$.

If your graph is computer generated, you need not recalculate the slope by hand, as most graphing applications will generate a best fit line and equation for you. However, you must understand what the equation means. Below, the equation for the line might be " $y=1.5 x+12$ " The equation must be written with appropriate symbols, $\mathrm{d}=1.5\left(\frac{\mathrm{~m}}{\mathrm{~s}}\right) \times \mathrm{t}(\mathrm{sec})+12 \mathrm{~m}$ AND real words, "the distance traveled in meters is equal to 1.5 times the time, in seconds, plus 12 meters."

Below is a sample graph. It satisfies all of the criteria for a good graph, except that it is too small. Ideally, the graph below would be printed in landscape mode, at full page size.


## Graphs will be graded on the following criteria:

1. Title, describing what is being graphed
2. Both axis labeled in terms of their measured values, with units
3. Good scales and intervals

- $\quad$ Not all graphs need to go through 0,0
- Origin (starting point) is multiple of 1,2 , or 5
- Intervals are multiples of 1,2 , or 5

4. Scale intervals linear and appropriately labeled
5. Independent variable on $x$-axis; dependent variable on $y$-axis
6. Data area of the graph takes up as much of the page as possible
7. Best fit linear or smooth line (as appropriate), not necessarily through points but an average
8. Correct determination of slope, with units
9. If graph is computer generated, I also look for:

- A legend so it's easy to see what has been graphed
- Include major and minor gridlines OR tick marks on both x and y axis
- Not crowded (not too many gridlines or ticks)

10. Equations written for linear plots must be written with symbols for the variables on each axis, and include appropriate units. (see above)

## Sample Graphs

Both graphs should be printed at least $1 / 2$ page size!


The good: The graph above shows a good linear relationship between the data, with a perfectly straight line that fits the data as well as possible. The axes are well labeled, and the scale/tick marks are perfect. Note how the data points take up most of the area of the graph. The equation for the line is printed, and the student provides an explanation in words.

The bad: The y axis has too many minor tick marks; they are just a blur.


The good: The graph above shows a curve fit for the data, with a smooth curve that fits the data as well as possible. Neither graph is "connect the dots." The x axis is well labeled, and the scale/tick marks are perfect.

The bad: The y axis is not labeled with units for conductivity. The x axis extends too far out.

## Plotting Data and Determining Slope Using EXCEL 2007

Microsoft Excel is a spreadsheet program that allows you to organize data, perform repetitive calculations, and create graphs. It is a very useful program to handle scientific or statistical data, to create databases (lists of information such as an address book or a library catalog) or to do accounting.
This handout is a guide fo how to enter data, perform calculations and make graphs with Excel. All tabs and menu selections are shown in bold italics. Make sure that "How to Make a Good Graph" is consulted.

## 1. Entering the data.

1. Start up a computer, log on to the computer as 2105. You may want to bring a USB disk to save your graph. Click on the Microsoft Excel icon. A blank data sheet should now appear on the screen:
2. It's helpful to enter the names and units of your data in the cell above the column of data. Columns can be widened with a left click on the line to the right of a column heading, then dragging the line. Or, double left click the right hand line to the right of a column heading.
3. Enter $x, y$ data in side by side columns, with the $x$ axis data in the left hand column and the $y$ data to the right, but this isn't necessary. Press the "Enter" to move down a cell, or use an arrow key or the mouse to move to a new cell.
4. You can make Excel calculate values with equations you enter. Start with $=$ in the cell, then use standard arithmetic symbols. You can use SUM, LN or LOG, STDEV, or SQRT (+ others). The cell would read: $=$ SUM $(\mathrm{A} 1: \mathrm{A} 3)$ to add numbers in a range of 3 cells (A1+A2+A3). Use lots of brackets ()., see the Formulas page, p. 17.
5. Graphing the data.
6. To select the data to plot, left click on the top left cell and drag to the bottom right cell. All the cells in both columns containing data should now be highlighted.
7. Click the Insert tab and then the Scatter Chart button (see below). The type of plot you need is an XY (scatter) plot with with only markers (no line).

8. Check your graph carefully to make sure the proper data is on the $x$ axis. If the $x$ data is on the $y$ axis, right click in the chart area and click on Select Data. Click the Edit button and change the letters in the series $X$ values and series $Y$ values fields.
9. Add Titles and Axis labels: Click on the chart to outline in blue, and select the Layout tab under Chart Tools.
a. Click Chart Title and Above Chart, then add your descriptive title (not simply y units vs. x units). Highlight the title with the mouse, and reduce the font size to something reasonable (12 or 14 pt ).
b. With the chart selected, under the Layout tab in Chart Tools, click Axis Titles and enter titles and units for the $x$ (horizontal, title below axis) and the $y$ (vertical, rotated).

## 3. Best-fit line and correlation coefficient.

9. With the chart still selected, click on the Design tab under Chart Tools. Use the left mouse button to select one data point, then right click. Select Add Trendline. Make sure the "linear" box is checked, and
check the 2 boxes at the bottom (Display equation on chart, and Display $\boldsymbol{R}^{2}$ value on chart). Close the window.

The $\mathbf{R}$ value indicated on your graph is the correlation coefficient. The value of $R^{2}$ gives an indication of predictive value of your equation, and extent that variance in $y$ depends on $x$ (and not other factors). The closer it is to 1.0 the more predictive value of your data.
10. Select the Legend box and delete.
4. Add tick marks and adjusting the axes.
11. To add minor tick marks, right click a number on an axis, and select Format Axis. Select "Inside" in the menu for Minor tick marks. The scale of the tick marks can also be adjusted to add more or remove some of the marks. The scale of the axis can be adjusted to maximize the space for the actual data in the chart window. The placement of the $x$ axis can be adjusted in the $y$ axis formatting box, useful for graphs with


## 5. Sharing work

It is expected that you and your lab partner will have identical data (you'd better) and, therefore, have identical graphs. Many of you will work with your lab partner on the graph. This is OK, as long as both of you are actively involved in making the graph. You are NOT LEARNING if your lab partner is creating the graph, printing out two copies and giving one to you. You are paying money to learn, don't waste the opportunity. May you be cursed with lousy jobs and sleepless nights if you don't take advantage of your chances to learn.

If your graph is computer generated, you need not recalculate the slope by hand, as most graphing applications will generate a best fit line and equation for you.

There are two sample graphs on the next page.

## How to make superscripts and subscripts in Microsoft Word 2003

There are several ways to make superscripts and subscripts. If you are not using your own computer and/or you don't want to change the settings on the computer, use method \#1. If you would like to change the settings on your computer and would like to set up a quick method, use method \#2.

## Method \#1

1. Type the text without subscripts or superscripts (eg: H2O)
2. Highlight whatever you would like to super- or sub- (eg: H 2 O )
3. In the menu, click on "Format" the "Font."
4. In the middle of the box, you are given several choices of "Effects." Click on the one you want to put a check mark in the box. Click "OK." You're all done! (eg: $\left.\mathrm{H}_{2} \mathrm{O}\right)$
5. Immediately after subscripting one number (before you type anything else), you can highlight the next number (or letter) to be subscripted. Then click control-y. This will repeat the last formatting. This works for super-scripting as well.

## Method \#2

1. This method will put icons in your toolbar for superscript and subscript. The icons will always be there, unless you take them off, even after turning your computer off and on again.
2. Click on "Tools" in the menu bar. Towards the bottom, click "Customize." Under "Categories" on the right, click "Format." Under "Commands" on the left, scroll down until you find " $x^{2}$ Superscript." Click-hold-and drag this icon into your toolbar wherever you'd like it placed.
3. Repeat step 2, but drag the " $x_{2}$ Subscript" icon into the toolbar next to the superscript icon.
4. Now you're ready to type. The new icons will toggle between plain text and super- or subscript. For example, if you want to type $\mathrm{H}_{2} \mathrm{O}$, type " H " the click " $\mathrm{x}^{2}$ " icon, type " 2 ", click " $\mathrm{x}^{2}$ " again, then type "O". Or, if you'd prefer, you can type everything in without supers and subs, then follow the steps for Method \#1, except use the new icons instead of using "Format" etc in the menu.

## How to Write Formulas in Microsoft Excel

Excel is a great tool for simplifying difficult mathematical and statistical chores. Using the following data table as an example, several things can be shown.

|  | A | B | C | D |
| :--- | :---: | :---: | :---: | :---: |
| $\mathbf{1}$ | 5.129 | 3.261 | 3.67 |  |
| $\mathbf{2}$ | 2.876 | 1.839 | 5.52 |  |
| $\mathbf{3}$ | 3.573 | 2.248 | 8.25 |  |
| $\mathbf{4}$ | 1.753 | 1.107 | 11.37 |  |

To calculate the sum of column A in cell A5, the text in A5 would read: =sum(A1:A4) You can type the cell address or use the mouse to highlight the cells once the first parentheses has been typed. Type "Enter" after using an equal sign (=) using the mouse to click another cell changes the formula!
To calculate the average of row 1, the text in D1 would read: =average(A1:C1)
To calculate the natural log, use: $=\mathrm{LN}(\mathrm{A} 1)$, and base ten log is: $=\mathrm{LOG}(\mathrm{A} 1)$.

The standard deviation of column $A$ is calculated as: $=\operatorname{stdev}(\mathrm{A} 1: \mathrm{A} 4)$.
Copy a formula from one cell to another: drag the lower right corner of a cell down or to the right.


