Unsupervised Parts-of-Speech Induction for Bengali

Joydeep Nath[1], Monojit Choudhury[2], Animesh Mukherjee[1], Chris Biemann[3], Niloy Ganguly[1]

[1]Department of Computer Science and Engineering, Indian Institute of Technology Kharagpur, India
[2]Microsoft Research Lab, Bangalore India, Email: monojitc@microsoft.com
[3]University of Leipzig, Germany

Abstract

We present a study of the word interaction networks of Bengali in the framework of complex networks. The topological properties of these networks reveal interesting insights into the morpho-syntax of the language, whereas clustering helps in the induction of the natural word classes leading to a principled way of designing POS tagsets. We compare different network construction techniques and clustering algorithms based on the cohesiveness of the word clusters. Cohesiveness is measured against two gold-standard tagsets by means of the novel metric of *tag-entropy*. The approach presented here is a generic one that can be easily extended to any language.

1. Introduction

Parts-of-speech (POS, also known as *word class* or *lexical category*) are the linguistic categories of words defined by their morphological and syntactic properties. The word categories that are distinctive in one language may exhibit identical behavior in another language. Linguists identify the lexical categories through manual inspection of the morpho-syntactic patterns present in a language. Can there be a principled and computational approach to this problem of identification of the lexical categories? The answer turns out to be 'yes', thanks to the concept of "distributional hypothesis" (Harris, 1968).

In fact, this hypothesis is the underlying (implicit or explicit) assumption of all computational approaches to POS tagging which is a very important preprocessing task for several NLP applications. Ironically, compared to the work done in the area of POS tagging, the volume of research dedicated to POS tagset (i.e., the set of lexical categories) design is quite small, even though the tagset is largely responsible for the efficiency as well as the effectiveness of a POS tagger.

The two basic questions that need to be answered while designing a POS tagset are: (a) which lexical categories are distinguishable in a language? and (b) does making a distinction between two categories help us in further NLP applications such as chunking and parsing? In other words, a tagset is always dependent on the language under consideration as well as the end application to which the POS-tagger caters. In fact, often the natural word classes present in a language are those that are easy to distinguish as well as sufficient in facilitating deeper linguistic processing. A key to the identification of these natural word classes is to understand the syntactic structure of a language, which is captured through the complex interaction of the words. This is arguably an outcome of a self-organizing process governing the dynamics of language and grounded in the cognitive abilities of human beings (Steels, 2000). In this context, language can be viewed as a network of words and formation of lexical categories an emergent property of this network. Thus, understanding the structure and function of this network will help us in procuring deeper insight into the nature of word classes in a given language.

In this work, we present a study of the lexical classes of Bengali obtained through the analysis of the word interaction networks. Although the scheme presented here is not essentially novel and has been motivated by several work on unsupervised induction of POS based on the distributional hypothesis (Finch and Chater, 1992; Schütze, 1993; Schütze, 1995; Gauch and Futrelle, 1994; Clark, 2000; Rapp, 2005; Biemann, 2006b), our main contributions reside in – (a) a comparative study of various approaches to POS tagset induction on Bengali, (b) rigorous linguistic analysis of the word classes and suggestions for a Bengali tagset design, (c) introduction of a novel metric, called tag entropy, to evaluate the goodness of the induced word classes, and most importantly, (d) analysis of the word interaction networks within the framework of complex network theory to understand the syntactic structure of Bengali. The analytical scheme presented here is a generic one and can be readily applied to any language for which a raw text corpus of moderate size is available.

Sec. 2. puts this work in the context of previous research in the areas of unsupervised POS induction and complex network theory. In Sec. 3. we define the word interaction networks and analyze their topological properties. Sec. 4. introduces the POS tagset induction models, experimental settings and the metric of tag-entropy, followed by a quantitative comparison of the results obtained from these models. In Sec. 5. we present a linguistic analysis of the induced word classes. Sec. 6. concludes the paper by summarizing our observations.

2. Background

The present work is based on two different lines of research. On one hand, from the perspective of NLP applications, it is based on the use of unsupervised machine learning techniques for induction of POS categories, and on the other hand it models and analyzes the syntactic distribution of the words in the framework of complex networks. In this section, we present a brief survey of both these research areas.

2.1. Unsupervised Induction of POS

Unsupervised induction of syntactic categories or POS tags involves use of machine learning techniques to automatically cluster the words of a given raw text corpus into syntactic classes. The formation of syntactic classes can be

governed by providing a seed lexicon or can be left at the discretion of the learning algorithm. These techniques, especially the latter ones, help us to (a) create a partial tagging dictionary[1] automatically from a raw text corpus, which can then be used for developing a POS tagger, and (b) acquire important insights into the natural syntactic classes present in a language, which in turn helps in deciding on a tagset for the language.

There are a number of approaches to derive syntactic categories. All of them employ a syntactic version of Harris' distributional hypothesis (Harris, 1968), which states that words of similar parts of speech can be observed in the same syntactic contexts. Since the function words form the syntactic skeleton of a language and almost exclusively contribute to the most frequent words in a corpus, contexts in that sense are often restricted to the most frequent words (Miller and Charles, 1991). The words used to describe syntactic contexts are further called *feature words*[2].

The general methodology (Finch and Chater, 1992; Schütze, 1993; Schütze, 1995; Gauch and Futrelle, 1994; Clark, 2000; Rapp, 2005; Biemann, 2006b) for inducing word class information can be outlined as follows, (a) collect global context vectors of target words by counting how often feature words appear in the neighboring positions, and, (b) apply a clustering algorithm on these vectors to obtain word classes.

Throughout, feature words are the most frequent 50-250 words. Some authors employ a much larger number of features and reduce the dimensions of the resulting matrix using Singular Value Decomposition (Schütze, 1993; Rapp, 2005). The choice of high frequency words as features is motivated by Zipf's law: these few stop words constitute the bulk of the tokens in a corpus.

Contexts are the feature words appearing in the immediate neighborhood of a word. The word's global context is the sum of all its contexts. Clustering consists of a similarity measure and a clustering algorithm. (Finch and Chater, 1992) uses the Spearman Rank Correlation Coefficient and a hierarchical clustering, (Schütze, 1993; Schütze, 1995) use the cosine of the angle between the vectors and Buckshot clustering, (Gauch and Futrelle, 1994) uses cosine on Mutual Information vectors for hierarchical agglomerative clustering and (Clark, 2000) applies Kullback-Leibler divergence.

Slightly different variations of the above generic scheme can be found in (Clark, 2003), (Freitag, 2004) and (Dhillon et al., 2003). For small size raw corpora, Bayesian approaches are known to be capable of producing good results (Haghighi and Klein, 2006; Goldwater and Griffiths, 2007). However, these approaches rely on a predefined set of tags and a small annotated corpus or a partial lexicon. A further related work is (Dasgupta and Ng, 2007), which proposes an unsupervised morphological analysis to create a soft clustering on word classes in their weakly supervised word class induction system for English and Bengali.

[1] A tagging dictionary consists of the distinct words (possibly inflected) of a language and their corresponding POS tags.

[2] *Target words*, as opposed to this, are the words that are to be grouped into syntactic clusters. Note that usually, the feature words form a subset of the target words.

2.2. Syntax as a Self-organizing Phenomenon

Recently, there has been several studies on the structural patterns of human languages within the framework of *complex network theory* (see (Newman, 2003) for a review). A complex network is a collection of entities (represented as nodes) and their interactions (represented as links or edges between the nodes). Such networks have been successfully used to explain the structure, function and evolutionary dynamics of a variety of natural systems found in the domains of biology, economics, physics, social sciences and information sciences. See (da F. Costa et al., 2007) for a survey on applications of networks in various areas. In the context of syntax, studies on *word collocation networks* and *syntactic dependency networks* have revealed several interesting cross-linguistic universals and their possible explanations in terms of human cognition.

In word collocation networks, words are the nodes and two words are linked if they are neighbors, that is they collocate, in a sentence (Ferrer-i-Cancho and Sole, 2001; Ferrer-i-Cancho et al., 2007b). Such networks, constructed for various languages, have been found to exhibit small world properties. The average path length between any two nodes is small (around 2 to 3) and the clustering coefficients are high (around 0.69). However, the most striking observation regarding these networks is that the degree distributions follow a two regime power-law. The degree distribution of the 5000 most connected words follow a power-law with an exponent -3.07, which is surprisingly close to that of the Barabási-Albert preferential attachment based growth model (Barabási and Albert, 1999). These findings led the authors to argue that the word usage of the human languages is preferential in nature, where the frequency of a word defines the comprehensibility and production capability. In essence, the authors conclude that evolution of language has resulted in an optimal structure of the word interactions that facilitate easier and faster production, perception and navigation of the words.

Although collocation networks are easier to construct, they do not necessarily capture the syntactic and semantic relationships between the words. This is because syntactic and semantic relations often extend beyond the local neighborhood of a word. Ferrer-i-Cancho and his co-authors (Ferrer-i-Cancho, 2005; Ferrer-i-Cancho and Sole, 2004) defined the *syntactic dependency network* (SDN) where the words are the nodes and there is a directed edge between two words if in any of the sentences of a given corpus there is a directed dependency relation between them. The SDNs were constructed from the dependency treebanks for three languages: Czech, German and Romanian, and found to exhibit strikingly similar characteristics. All the networks exhibit power-law degree distributions, small world structure, disassortative mixing and a hierarchical organization. More recently, (Ferrer-i-Cancho et al., 2007a) showed that spectral clustering of SDN puts words belonging to the same syntactic categories in the same cluster.

Thus, word collocation as well as the syntactic dependency networks unfurl various interesting facts about the nature of word interactions and syntactic patterns.

3. Word Networks

The definition and the construction of the word networks presented here are primarily based on the work by (Biemann, 2006b). Nevertheless, we also explore some variations while defining the network as well as their construction for Bengali data. Moreover, we study the topological properties of these networks, which provides us with insights into the syntactic structure of Bengali. We also conduct a comparative study of two different clustering algorithms.

3.1. Feature words, Context Vectors and Similarity Metric

We take a raw Bengali text corpus consisting of n tokens and compute the unigram frequency counts for each of the types observed in the corpus. We select the first m types that have the highest unigram frequencies as the *feature words*. The intuition is that since the function words have a very high frequency, the feature words selected on the basis of frequency will largely correspond to the function words of the language.

However, we observe that for corpora pertaining to specific domains (e.g., only news articles), several content words also creep into the list of top few words deemed here as feature words. Therefore, to ensure the absence of any content word in the set of feature words, we also construct networks where this set is manually selected from a frequency-based sorted list of words. We shall refer to the former (i.e., frequency based feature word selection) networks by a prefixed superscript *fr* and the latter networks by another prefixed superscript *ms*.

Let $w_{-2}w_{-1}ww_1w_2$ be a window of 5 tokens around the target word w. A *context vector* for the target word w is defined as a vector of dimension $4m$ in which the entries $(4i+1), (4i+2), (4i+3)$ and $(4i+4)$ correspond to the number of occurrences of the $(i-1)$th feature word at the w_{-2}, w_{-1}, w_1 and w_2 positions respectively.

In (Biemann, 2006b), the distributional similarity between two words w and v is defined as $sim(w,v) = \frac{1}{1-cos(\vec{w},\vec{v})}$, where $\vec{w}$ and $\vec{v}$ represent the context vectors of the words w and v respectively, that are computed from a large raw text corpus; $cos(\vec{x},\vec{y})$ is the normalized dot product of the vectors $\vec{x}$ and $\vec{y}$, i.e., the cosine of the angle between them. An alternative definition of the similarity could be simply the cosine of the angle between $\vec{w}$ and $\vec{v}$, that is $sim(w,v) = cos(\vec{w},\vec{v})$. We shall denote the networks constructed using the metric proposed in (Biemann, 2006b) by a prefixed superscript *b* (for Biemann) and the latter ones by another prefixed superscript *c* (for cosine).

3.2. Definition and Construction of the Networks

The word network is a weighted undirected graph $G = \langle V, E \rangle$, where V consists of 5000 nodes corresponding to the most frequent 5000 types excluding the feature words. The number of nodes in V has been decided based on the fact that with a corpus of size around 10M words, enough context information is available only for the top few words. The weight of the edge between any two nodes representative of the words w and v is given by $sim(w,v)$ and this edge exists if $sim(w,v)$ exceeds a threshold τ. Thus, considering all the variations in definition of feature words and similarity metric, we can construct four different networks for a given corpus: ${}^{fr,b}G$, ${}^{fr,c}G$, ${}^{ms,b}G$ and ${}^{ms,c}G$.

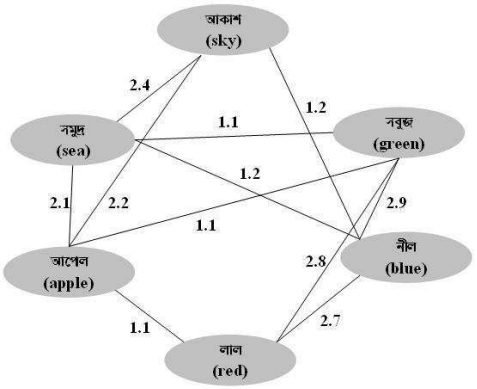

Figure 1: A hypothetical illustration of the word network. The English gloss for each of the Bengali words is provided within parentheses. Note that the edge weights are hypothetical and do not correspond to any of the similarity metrics.

Figure 1 presents a hypothetical illustration of the word network.

We have used the newspaper corpus[3] Ananda Bazaar Patrika for the creation of word networks. This corpus has around 17M words. We shall represent a network constructed from a corpus of size n using m feature words as $G_{n,m}$. Therefore, for a frequency-based selection of feature words and cosine similarity metric, the networks will be denoted as ${}^{fr,c}G_{n,m}$. Also, we shall drop the superscripts or subscripts whenever we refer to the networks corresponding to all the combinations for the part dropped.

We construct 20 word networks for all possible combinations of $n = \{$ 1M, 2M, 5M, 10M, 17M $\}$ and $m = \{25, 50, 100, 200\}$. In order to construct $G_{n,m}$ for $n < 17$, we have randomly selected a subset of documents from the original corpus. Note that in our experiments we consider the different inflected forms of a root morpheme as different types.

3.3. Properties of the Word Networks

In this section we present some of the important topological properties of the word networks. Interestingly, the four basic variations in network construction give rise to networks that have very similar topological properties. Therefore, we shall present all the results for ${}^{fr,b}G_{n,m}$, which might be generalized to the other cases as well. Note that the calculation of the degree distribution and the clustering coefficient is done on the unweighted version of the networks (all edges below the threshold τ are deleted).

3.3.1. Degree Distribution

The cumulative degree distribution (CDD) of a network, P_k, is the probability that a randomly chosen node has de-

[3]The authors thank ISI Kolkata for providing this corpora for the purpose of the experiments.

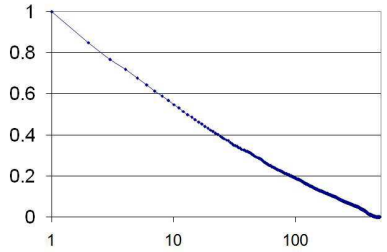

Figure 2: Cumulative Degree Distribution for the word network ${}^{fr,b}G_{17M,50}$. x-axis: $\log(k)$, y-axis: P_k

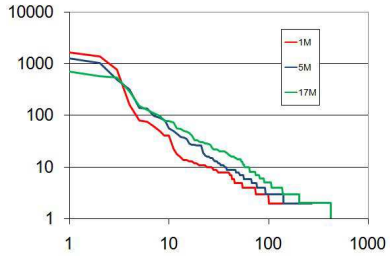

Figure 3: Rank (x-axis) versus cluster size (y-axis) in doubly logarithmic scale for ${}^{fr,b}G_{n,50}$ where n is 1M, 5M and 17M. The clusters are assigned a rank in descending order of their size (i.e. the number of words in the cluster), so that the largest cluster gets rank 1.

gree greater than or equal to k. CDD provides important information about the topology of the network. Figure 2 shows the CDD for the word network ${}^{fr,b}G_{17M,50}$. We observe that the CDD follows a logarithmic distribution (i.e., $P_k \propto log(k)$), which means that $-\frac{dP_k}{dk} = p_k$ (probability that a randomly chosen node has degree equal to k) or the non-cumulative degree distribution is proportional to k^{-1} (popularly known as power-law or Zipfian distribution, but it is not clear whether this is a consequence of Zipf's law). Similar results have been observed for the networks with varying m and n.

Power-law networks are believed to have a self-similar hierarchical structure. In this case, the hierarchy is a reflection of syntactic ambiguities. Highly ambiguous words that belong to several lexical categories have the highest degrees. The next level of hierarchy is manifested by words that belong to a few lexical categories, whereas the last level of hierarchy is represented by the words that are unambiguous in nature. The power-law indicates that there are few words that belong to a large number of lexical categories, while the most of the words belong to only one lexical category.

3.3.2. Clustering Coefficient

The clustering coefficient of a node is the probability that a randomly chosen pair of its neighbors are themselves neighbors. We observe that there is a positive correlation between the degree of a node and its clustering coefficient. In particular, high degree nodes (i.e., the most ambiguous ones) have a high clustering coefficient. This implies that the network is very dense (clique-ish) around the high degree nodes. As we shall see later, this has a significant effect on the cluster size distribution and the efficacy of this method as such. The mean clustering coefficient for ${}^{fr,b}G_{17M,50}$ is 0.53, which is much higher than that of random graphs. This again points to the fact that there is a strong community structure in the networks reflecting the presence of natural word classes.

3.4. Community Structure

In order to gain insight into the topology of the network we cluster them using the following two different approaches.

Chinese Whispers: The Chinese Whispers (CW) algorithm (Biemann, 2006a) is a non-parametric random-walk based clustering algorithm, where initially each node is in a separate cluster. In every iteration, the nodes propagate information about their current cluster to all the neighbors, and in turn, decide upon their own cluster labels based on a weighted majority voting of the cluster information received from the neighbors. The algorithm terminates when the labels do not change considerably over successive iterations.

Agglomerative Hierarchical Clustering: In this approach (Rapp, 2005), initially all the words are in separate clusters. At every iteration, two clusters closest to each other (where "closeness" between the centroids of the two clusters is measured by $sim(w, v)$) are merged to form a new cluster. The algorithm terminates after obtaining a predefined number of clusters.

We plot the cluster size distributions for ${}^{fr,b}G$ in Fig. 3 for various values of n and m following the CW algorithm. In fact, the distributions are identical for both the clustering approaches and all the other networks. The cluster size distributions (CSD) show a power-law behavior, which gets better as n increases. Thus, there are a few giant clusters, as is expected from the presence of the nodes with high degree and high clustering coefficient in the networks. Thus, the giant clusters consist of words that belong to multiple POS categories. In fact, these are the words that make POS tagging a non-trivial and challenging task. It would be interesting to devise techniques that can break the giant cluster into smaller clusters. We also observe that the words belonging to the giant clusters need not have high frequency in the corpus.

In this section, we have analyzed the word networks from a complex network perspective, which has revealed several significant properties underlying the syntactic structure of Bengali. We shall revisit these issues in Sec. 6., but before that we shall analyze the word clusters from the perspectives of NLP and linguistics in general.

4. Experiments and Evaluation

Evaluation of the word clusters is challenging and there are two different ways in which this can be done. One way would be to compare the word clusters against a predesigned set of lexical categories, in which case we are biased towards some gold standard tagset and consequently, contradicting the objective of automatic induction of the categories. Moreover, this method is incapable of evaluating the goodness of the clusters that are finer than the standard tagset. A better way is to resort to some task completion method for evaluation. Unfortunately, in absence of

n	m	Baseline	$MTE(C)$	$WMTE(C)$	% gain for MTE	% gain for $WMTE$	m	Baseline	$MTE(C)$	$WMTE(C)$	% gain for MTE	% gain for $WMTE$
1M	25	4.09 (4.02)	1.75 (1.09)	3.51 (3.30)	57 (73)	14 (18)	100	4.10 (4.03)	1.61 (1.11)	3.57 (3.38)	61 (72)	13 (16)
	50	4.08 (4.01)	1.69 (1.10)	3.53 (3.32)	59 (72)	13 (17)	200	4.11 (4.05)	1.77 (1.12)	3.60 (3.44)	57 (72)	12 (15)
2M	25	4.13 (4.09)	1.60 (0.99)	3.48 (3.30)	61 (76)	16 (19)	100	4.12 (4.08)	1.56 (1.00)	3.51 (3.36)	62 (75)	15 (18)
	50	4.11 (4.08)	1.58 (1.01)	3.49 (3.31)	62 (75)	15 (19)	200	4.14 (4.10)	1.55 (0.96)	3.55 (3.39)	63 (76)	14 (17)
5M	25	4.08 (4.06)	1.52 (1.04)	3.23 (3.04)	63 (74)	21 (25)	100	4.04 (4.01)	1.46 (0.94)	3.22 (3.04)	64 (77)	20 (24)
	50	4.03 (4.01)	1.49 (0.95)	3.21 (3.04)	63 (76)	20 (24)	200	4.03 (4.01)	1.36 (0.81)	3.21 (3.05)	66 (80)	20 (24)
10M	25	4.06 (4.07)	1.41 (0.88)	3.16 (2.94)	65 (78)	22 (28)	100	4.08 (4.10)	1.35 (0.83)	3.17 (2.97)	67 (80)	22 (27)
	50	4.05 (4.07)	1.38 (0.88)	3.16 (2.95)	66 (78)	22 (28)	200	4.07 (4.09)	1.28 (0.77)	3.20 (3.04)	69 (81)	21 (25)
17M	25	4.04 (4.04)	1.53 (1.04)	3.03 (2.83)	62 (74)	25 (30)	100	3.96 (3.97)	1.38 (0.85)	2.97 (2.78)	65 (79)	25 (30)
	50	3.95 (3.96)	1.45 (0.99)	2.93 (2.74)	63 (75)	**26 (31)**	200	3.98 (3.99)	1.32 (0.76)	2.98 (2.81)	67 (81)	24 (29)

Table 1: Results for $CW_{n,m}$ model. The values in parentheses refer to the case where the words unknown to the morphological analyzer have been manually corrected. Best results in bold font.

any standard task completion based evaluation strategy for the current work, we compare the clusters against two gold standard tagsets for Bengali described in (Dandapat et al., 2004) and (Dasgupta and Ng, 2007).

4.1. Tag Entropy

Given a word w, a morphological analyzer returns all the possible segmentation of the word w along with the corresponding lexical categories[4]. For example, the Bengali word *kare* has three possible categories: NN (noun), gloss: palm - locative; VF (finite verb), gloss: do - present, simple, third person; and VN (non-finite verb), gloss: having done.

Let $cat_1, cat_2, \ldots cat_T$ be the universal set of lexical categories, where T is the total number of categories. We define a T-dimensional binary vector Tag_w for a word w as the *tag-vector*, where the value of $Tag_w(i)$ is 1 if and only if according to the morphological analyzer cat_i is a possible category for w. Thus, the tag-vector of *kare* will have 1 only in three positions (corresponding to the categories NN, VF and VN) and rest $T-3$ positions have 0s.

Given a cluster $c = \{w_1, w_2, \ldots w_s\}$, the cluster is perfectly cohesive if the tag-vectors of all the words in c are identical. On the other hand, the cluster is incohesive if the 1s and 0s are distributed randomly across them. Our objective is to define a metric over the tag vectors of the words in c, which will be able to quantify the cohesiveness of the cluster. Since binary entropy (Shannon and Weaver, 1949) measures the disorderedness of a system, we define the (in)cohesiveness of a cluster c of size s as

$$TE(c) = -\sum_{i=1}^{T} \left(p_i(c) \log_2 p_i(c) + q_i(c) \log_2 q_i(c)\right) \quad (1)$$

where

$$p_i(c) = \frac{1}{s}[\text{\# words in } c \text{ for which } Tag_w(i) = 1]$$

and $q_i(c) = 1 - p_i(c)$.

In words, $TE(c)$ is the sum of the binary entropies of the cluster over each of the categories. We call $TE(c)$ the *tag entropy* of the cluster c. For a perfectly cohesive cluster, $p_i(c)$ is 1 or 0 for all i, and therefore, $TE(c) = 0$. For a perfectly incohesive cluster, $TE(c)$ is T. This happens when $p_i(c) = 0.5$ for all the categories. The lower the tag entropy, the higher the cohesiveness of the cluster.

4.2. Evaluation Metrics

The clustering algorithm splits the 5000 words into several clusters. Let $C = \{c_1, c_2, \ldots c_r\}$ be the set of word clusters for a particular experimental setup. Based on tag entropy, we define two metrics for evaluation of C: *mean tag entropy* $MTE(C)$ and *weighted mean tag entropy* $WMTE(C)$, as follows.

$$MTE(C) = \frac{1}{r}\sum_{i=1}^{r} TE(c_i) \quad (2)$$

$$WMTE(C) = \frac{1}{5000}\sum_{i=1}^{r} |c_i| TE(c_i) \quad (3)$$

where $|c_i|$ is the number of words in cluster c_i.

We define our baseline as the case when all the 5000 words are in the same cluster. Thus, the baseline MTE is equal to the baseline WMTE, which in turn is equal to $TE(V)$, where V is set of nodes in the network[5]. The motivation behind the definition of baseline is as follows. The quantity $TE(V) - WMTE(C)$ gives an estimate of information gain with respect to the standard tagset by splitting V into set of clusters C. Therefore, the higher the value of this quantity, the better the clustering.

4.3. Experiments

We use the 17M word *Anandabazaar Patrika* (a Bengali daily: http://www.anandabazar.com/) corpus for all our experiments. We have 4 different methods for network construction, 20 different combinations of m and n, 2 different clustering algorithms and 2 gold standard tagsets. This together gives rise to $4 \times 20 \times 2 \times 2 = 320$ possible experiments. It is quite a formidable task to report all these experiments here. Therefore, we divide our experiments into three sets, where we systematically investigate certain parameters.

[4]For the tagset presented in (Dandapat et al., 2004), we use the morphological analyzer for Bengali described in the same paper. However, for the purpose at hand, it suffices to have a lexicon with all the inflected forms of the root words and their categories. This is what we perform for the tagset presented in (Dasgupta and Ng, 2007).

[5]This is a slight abuse of notation because V is the set of nodes, whereas TE is defined on set of words. Nevertheless, the notation is unambiguous as every node in V correspond to one and only one word.

Metric	${}^{fr,b}G$	${}^{fr,c}G$	${}^{ms,b}G$	${}^{ms,c}G$
WMTE	36.2 (25.3)	37.7 (30.1)	36.7 (26.1)	**39.2 (38.1)**
MTE	86.7 (87.4)	64.0 (75.2)	**87.9 (88.9)**	70.5 (75.5)

Table 2: Percentage gain in MTE and WMTE for the 4 different graph construction methods and agglomerative hierarchical clustering. Best results are in bold fonts. The values in parentheses refer to the case where the words unknown to the morphological analyzer have been manually corrected.

4.3.1. Set I

In this set of experiments, we fix the network to ${}^{fr,b}G_{n,m}$, use CW clustering algorithm and compare our results for the (Dandapat et al., 2004) tagset. Thus, we have 20 experiments corresponding to the various combinations of m and n, the results of which are summarized in Table 1. The aim of this set of experiments is to study the behavior of the clusters as we increase the corpus size and number of feature words. There are 450 to 500 clusters (including singletons) per graph found by the CW algorithm[6]. There were a large number of named entities among the target words that were unknown to the morphological analyzer. These words, around 1900 in number, have been manually assigned the appropriate POS categories and included for computation of WMTE.

The best results are obtained for $n = 17M$ and $m = 50$. As is expected, the goodness of the induced lexicon increases rather significantly with the corpus size. For a given corpus, using more feature words does not necessarily improve the results. In general, the ideal value of m seems to be a monotonically increasing function of n.

4.3.2. Set II

In this set of experiments, we investigate the effectiveness of the four different graph construction methods. For this set, we only use the hierarchical clustering method. The evaluations are made against the (Dandapat et al., 2004) tagset and all the graphs are constructed for $n = 17M$ and $m = 50$, for which the best results are obtained in Set I.

The primary observation is that the hierarchical clustering gives better result than the CW algorithm. Nevertheless, unlike CW, the WMTE is lower (or the information gain is higher) for hierarchical clustering when the named entities are manually corrected. This implies that CW is able to cluster the named entities more efficiently than hierarchical clustering. Among the graph construction methods, the best results are obtained for ${}^{ms,c}G$, which shows that manual selection of feature words has a positive impact on the word clusters. This revalidates the fact that function words are better suited for POS tag induction.

4.3.3. Set III

As we have mentioned earlier, it is not appropriate to evaluate the goodness of the word clusters that emerge after clustering based on a predefined set of tags. One way to circumvent this problem is to evaluate across multiple tagsets. The previous two sets of experiments are based on the tagset defined in (Dandapat et al., 2004). In the third set of experiments, we use the tagset described in (Dasgupta and Ng, 2007) and the dataset made available by the authors (*http://www.hlt.utdallas.edu/∼sajib/posDatasets.html*) consisting of 5000 Bengali words and their corresponding tags to evaluate our clusters. Since we do not have an access to the training corpus used in (Dasgupta and Ng, 2007), we have filtered our clusters obtained during the experiments in Set I and Set II, so that they contain only words present in the Dasgupta and Ng dataset. Consequently, the clustered networks now contain around 800 words.

The best results have been obtained for the combination of ${}^{fr,b}G_{17M,50}$ and CW algorithm, for which the entropy reduction is 89% and 57% for MTE and WMTE respectively. Note that these figures are 75% and 31% in the case of Dandapat et al. tagset. The best results for hierarchical clustering is obtained for ${}^{fr,c}G_{17M,50}$, where the respective reductions are 88% and 42%.

Although it is tempting to reason that the vast improvement in the results for the Dasgupta and Ng dataset is because of the small number of tags, in reality this might not be the case as the baseline tag entropies for both the datasets are close (around 4). In the next section, we shall discuss the possible reasons behind this improvement.

5. Linguistic Analysis and Tagset Design

Bengali is an Indo-Aryan language spoken in Bangladesh and the eastern parts of India. The syntax of the language is morphologically rich and the word order is relatively free. The case relations between the verb and its arguments are usually marked by inflectional suffixes on the nouns. There are a handful of overloaded suffixes that mark various cases depending on the context. Verbs inflect for tense, aspect, mood and person. There are three non-finite verb forms that act as participles and gerunds. Bengali has a small repertoire of verb roots and a large number of compound verbs are formed by noun-verb and adjective-verb combinations. Use of "do-support" verbs are also extremely common. Bengali makes use of classifiers (a word/morpheme used to classify nouns according to meaning, number, definiteness etc.), but does not distinguish between gender. Although number distinctions are sometimes reflected through nominal classifiers or suffixes, it is not marked on the verbs.

There has been very few work towards POS tagging in Bengali and consequently there are no standard and well-accepted tagset for the language. For instance, the two tagsets that we have used as gold standards differ substantially in their design principles. The tagset presented in (Dandapat et al., 2004) has 40 tags covering the nouns (2 classes), verbs (6 classes), adjectives and quantifiers (6 classes), pronouns (11 classes) and other function words. This tagset is heavily influenced by the English Penn Treebank tagset and words are tagged primarily based on their syntactic function, rather than morphological form. Thus, except for the verbs, the different morphological variations of a root word are not placed into different lexical categories. On the other hand, the tagset described in (Dasgupta and Ng, 2007) consists of only 11 tags that partially covers the lexical categories of Bengali. Nouns are divided into

[6]Some of the example clusters can be found at *http://banglaposclusters.googlepages.com/home*

7 classes based on proper vs. common, singular vs. plural and different case-marker (genitive, locative, accusative and nominative) distinctions. There is one class each for adjectives and adverbs. Verbs are divided into two classes based on their morphological form (finite or non-finite). Hence, this tagset has been designed based on the forms of the words rather than their functions.

Let us investigate the nature of the clusters that emerged during our experiments. As discussed earlier, in all the experiments we observe the presence of a few (typically 2 to 4) giant clusters that mainly consist of ambiguous words and thus are "bad" clusters. In fact, it has been observed that by filtering the top few large clusters one can considerably reduce the tag entropy of the clustering. Manual inspection reveals that the medium to small size clusters are "good" and mostly composed of words belonging to similar morpho-syntactic category. There are, however, a few clusters formed on the basis of semantic similarity between the constituent words. See Table 5. for some example clusters[7]. The trends in which clusters are formed and merged during the hierarchical clustering provides us useful information about the distinguishabilty between the various lexical classes. We enumerate some of the natural classes that emerged out of our experiments and the categorical distinctions that seem needless for Bengali.

Nouns: Possessive nouns and pronouns (e.g. *gharera* 'of house', *tomAra* 'your') form a separate cluster and are similar to adjectives in their distribution than other nouns. Although nouns with locative (e.g. *ghare* 'in house') and accusative (e.g. *pradhAnamantrIke* 'to the prime minister') case-markers form separate clusters initially, they merge with other nouns at a later stage of clustering. We further observe that there is no distinction between the distributions of plural and singular nouns.

Proper Nouns: Different clusters emerge for the different types of proper nouns, such as names of person, location, organization, month and days. Moreover, first and last names of persons show up as separate clusters.

Verbs: In all the models we observe that finite (e.g. *kareChena* 'have done'), modal (e.g. *pAre* 'can do'), non-finite (e.g. *uThe* 'having stood up') and infinitive (e.g. *karate* 'to do') verbs emerge as four basic categories. Non-finites and infinitives merge at a later stage. Verbal nouns (e.g. *khAoyA* 'to eat') form a separate cluster initially and later merge with nouns.

Adjectives and Numbers: The distinctions between quantifiers, intensifiers and numbers are observable, though in the later stages of clustering the former two categories merge with other adjectives.

Other Categories: We also observe the question words (e.g. *kI* 'what', *kemana* 'how'), relative pronouns (e.g. *ye* 'whoever', *yakhana* 'whenever'), punctuation marks, conjuncts (e.g. *o* 'and', *bA* 'or') forming separate clusters. However, since these are closed-classes with a very few representative words, it is difficult to make any strong claims about their naturalness.

[7]In this article, we use Romanized script to represent Bengali words following the ITRANS (*http://www.aczoom.com/itrans/*) convention.

Therefore, one should take into account the aforementioned factors while designing a tagset for Bengali. Despite the fact that the tagset of (Dasgupta and Ng, 2007) makes a larger number of distinctions between the noun forms, this partial tagset, as reflected in our experiments in Set III, has a better correlation with the natural word classes obtained. On the other hand, the Dandapat *et al.* tagset scores poorly on this dimension, primarily because of the finer distinctions made for the verbs and pronouns based on their function. Nevertheless, advanced stages of NLP like chunking and other applications might require such finer distinctions that are not apparent from the natural word classes.

6. Conclusion

In this work, we presented a principled and systematic approach to understand the syntactic structure of Bengali and induce the natural word classes of this language. We summarize below our salient observations.

- The degree distribution of the network follows a power-law behavior reflecting a hierarchy of the words with respect to their syntactic ambiguities.
- The clustering coefficient of the network is significantly higher than that of the random graphs pointing to the presence of strong community structures that are representative of the natural word classes.
- Clustering splits the network into word classes representing different lexical categories and the cluster size distribution follows a power-law. There are a very few giant clusters consisting of many ambiguous words and a large number of medium to small size clusters consisting of mostly unambiguous words.
- The results obtained for all the different graph construction and clustering algorithms are very close to each other implying the underlying robustness of the distributional hypothesis. However, the size of the corpus has a strong effect on the quality of the emerging clusters.
- We note that morphology plays a significant role in defining the syntactic clusters of Bengali. However, it may be harmful to start with the assumption proposed in (Dasgupta and Ng, 2007) that each morphological category defines a syntactic class. In particular, we do observe possessive nouns and finite, non-finite and infinitive verbs forming separate clusters, but we also observe that presence of plural markers (e.g. *der*, *rA*) or accusative or locative inflections for nouns need not essentially mark a separate syntactic category.

In conclusion, the pen and paper based linguistic analysis technique for identification of lexical categories might well be automated in a principled manner by exploiting the concept of distributional hypothesis. Cross-linguistic study of the topology of the word networks can reveal several universal properties as well as typological variations in the linguistic systems. Apart from providing insights into the natural word classes leading to the design of appropriate tagsets, the study of these networks can significantly increase our understanding of the evolution of syntax.

Size	Example Words	Remarks
596	*aruNa, buddhabAbu, saurabha, rAkesha, siddhArtha*	Proper nouns (names of person)
352	*golamAlera* 'of problem', *dAbira* 'of demand', *phalera* 'of result', *Agunera* 'of fire', *dUShaNera* 'of pollution'	Nouns with possessive marker
133	*badalAno* 'to change', *AmAnya* 'disregard', *AkramaNa* 'attack', *sAhAyya* 'help',*guli* 'bullet',	Nouns/verbal nouns that form compound verbs with 'do' or 'be'
44	*sAtaTi* 'seven', *tinaTe* 'three', *anekguli* 'many', *3Ti* 'three', *11Ti* 'eleven'	Quantifiers (mainly cardinal)
13	*adhibeshane* 'during the session', *bhAShaNe* 'in the speech', *baktRRitAYa* 'in the speech', *dalei* 'in the party', *pratibedane* 'in a report'	A semantic cluster related to parliamentary affairs

Table 3: Examples of clusters from the ${}^{fr,b}G_{17M,50}$ using CW algorithm.

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