## Decision Trees Using TreePlan

### 15.1 TREEPLAN OVERVIEW

TreePlan is a decision tree add-in for Microsoft Excel 97-2007 for Windows and Macintosh.
TreePlan helps you build a decision tree diagram in an Excel worksheet using dialog boxes. Decision trees are useful for analyzing sequential decision problems under uncertainty. Your decision tree model may include various controllable alternatives (e.g., whether to introduce a new product, whether to bid on a new project) and uncontrollable uncertainties (e.g., possible demand for a product, whether you're awarded a contract), arranged in chronological order. TreePlan automatically includes formulas for summing cash flows to obtain outcome values and for calculating rollback values for determining the optimal strategy.

To use TreePlan, you
(1) open a new worksheet,
(2) choose Tools $\mid$ Decision Tree from Excel's menu,
(3) select a node to change the structure of your decision tree,
(4) enter branch names, cash flows, and probabilities, and
(5) determine the optimal strategy from TreePlan's results.

All of TreePlan's functionality, including its built-in help, is a part of the TreePlan XLA file. There is no separate setup file or help file. When you use TreePlan on a Windows computer, it does not create any Windows Registry entries (although Excel may use such entries to keep track of its add-ins).

### 15.2 HOW TO INSTALL AND UNINSTALL TREEPLAN

## EXE, ZIP, and XLA Files

The TreePlan add-in file is typically named tree170s.xla, where "tree" is an abbreviation of TreePlan, "170" indicates version 1.70, and "s" indicates standard license (and "t" indicates tryout license and "a" indicates academic license). Excel recognizes only the XLA file, not a ZIP file or an EXE file.

You may receive or download the add-in as a compressed ZIP file, e.g., tree170s.zip. To extract the XLA file using the Windows XP operating system, right-click the ZIP file, and choose Open With Compressed (zipped) Folder. Alternatively, download the WinZip evaluation version from www.winzip.com to extract the XLA file. On a Macintosh, extract using the free StuffIt Expander, available from www.stuffit.com.

TreePlan may be received as an executable program file with an EXE extension, e.g., tree170s.exe. The EXE file contains the TreePlan ZIP file and software to extract or "unzip" the ZIP file. To extract the XLA file using a Windows operating system, double-click the EXE file, or right-click and choose Open. On a Macintosh, extract using Stuffit Expander.

The TreePlan XLA file may be combined with the SensIt XLA or RiskSim XLA files in a single ZIP or EXE file, in which case the multiple XLA files are extracted.

There are several ways to install the TreePlan XLA file.

## Avoiding Security Warnings in Excel 2007

TreePlan is an unsigned macro file. To avoid a security warning each time you run Excel 2007, choose Office Button | Excel Options | Trust Center | Trust Center Settings | Add-ins, and uncheck all checkboxes, as shown in Figure 15.1.

Figure 15.1 Excel 2007 Trust Center Add-Ins Settings


## Occasional Use: Open the Add-In File

The simplest method of using TreePlan does not require any installation step. Start Excel, and use Excel's File | Open command to open the TreePlan XLA file from floppy or hard drive. In Excel 2007, choose Office Button | Open. This method is particularly useful when you want to use TreePlan temporarily on another computer. Do not try to open the XLA file by double-clicking.
When you use Excel to open the XLA file on Windows computers, if Excel's security level is set to High or Very High, you may see a warning similar to Figure 15.2.

Figure 15.2 Excel 2003 Security Warning With High Security Level

Since TreePlan is an Excel 4.0 macro, it is automatically disabled if Excel's security level is High or Very High. To use TreePlan, start Excel, choose Tools | Macro | Security | Security Level, click Medium, and click OK, as shown in Figure 15.3. Then open the TreePlan XLA file.

Figure 15.3 Excel 2003 Tools Macro Security Level


If the Security Level is set to Medium or Low when you open the TreePlan XLA file, you may see the warning shown in Figure 15.4. Click the Enable Macros button. To use TreePlan's features, choose the Decision Tree item on Excel's Tools menu.

Figure 15.4 Excel 2003 Security Warning With Medium Security Level


In summary, to use Excel's File | Open command to load the TreePlan XLA file, you must choose Tools | Macro | Security | Security Level \| Medium, and you must click the Enable Macros button in the Security Warning dialog box.

In Excel 2007, to use Excel's Office Button | Open command to load the TreePlan XLA file, first choose Office Button | Excel Options | Trust Center | Trust Center Settings | Macro Settings | Disable all macros with notification, as shown below, and click| OK | OK. You could also use the Office Button | Open command to load the XLA file if you choose "Enable all macros," but that setting is not recommended.

Figure 15.5 Excel 2007 Trust Center Macro Settings

| Trust Center |  |  |
| :---: | :---: | :---: |
| Trusted Publishers | Macro Settings |  |
| Trusted Locations <br> Add-ins <br> Active X Settings | For macros in documents not in a trusted location:Disable all macros without notificationDisable all macros with notificationDisable all macros except digitally signed macrosEnable all macros (not recommended; potentially dangerous code can run) |  |
| Macro Settings |  |  |
| Message Bar | Developer Macro Settings |  |
| External Content <br> Privacy Options | $\square$ Trust access to the VBA project object model |  |
|  | OK | Cancel |

When you use the "Disable all macros with notification" setting in Excel 2007 and open the XLA file, you will see security notice shown below. You must click Enable Macros if you wish to use TreePlan 's features.

Figure 15.6 Excel 2007 Security Notice

## Microsoft Office Excel Security Notice <br> $? x$

Microsoft Office has identified a potential security concern.

Warning: It is not possible to determine that this content came from a trustworthy source. You should leave this content disabled unless the content provides critical functionality and you trust its source.

File Path: C:|tree 170s.xla
Macros have been disabled. Macros might contain viruses or other security hazards. Do not enable this content unless you trust the source of this file.

More information
Enable Macros Disable Macros

In Excel 2007, to use TreePlan, use the Ctrl+Shift+T hotkey. Alternatively, in the Menu Commands area of the Add-Ins ribbon, choose Decision Tree.

## Selective Use: Add-In File in Library Folder

For Windows computers, copy the TreePlan XLA file to the Program Files $\backslash$ Microsoft Office $\backslash$ Office $\backslash$ Library folder of your hard drive. The next time you start Excel, TreePlan will automatically appear in Excel's add-in manager. Start Excel, and use Excel's Tools | Add-Ins command to load and unload TreePlan as needed by checking or unchecking the TreePlan checkbox, as shown in Figure 15.7.

Figure 15.7 Excel Add-In Manager


Since the Library folder is a trusted location, set the security level to High or Very High and avoid security warnings when TreePlan is loaded. Choose Tools | Macro | Security | Trusted Publishers, check the box for "Trust all installed add-ins and templates," and click OK, as shown in Figure 15.8. To run TreePlan during the same session when you change this setting, you may have to choose Tools $\mid$ Add-Ins, uncheck TreePlan in the list, click OK, choose Tools $\mid$ Add-Ins again, check TreePlan in the list, and click OK.

Figure 15.8 Excel 2003 Tools Macro Security Trusted Publishers


In summary, if you put the TreePlan XLA file in the Library folder on a Windows computer, you should choose Tools $\mid$ Macro $\mid$ Security $\mid$ Trusted Publishers, and check the box for "Trust all installed add-ins and templates."

For Macintosh, a folder similar to Library is usually found at Macintosh HD : Applications : Microsoft Office : Office : Add-Ins, but you will need to explicitly select the XLA file to install it, using the same procedure described below when you use an arbitrary folder.

In Excel 2007, copy the TreePlan XLA file to the Program Files $\backslash$ Microsoft Office $\backslash$ Office $\backslash$ Library folder. The next time you run Excel 2007, choose Office Button | Excel Options | Add-Ins, and you will see TreePlan listed as one of the inactive application add-ins, as shown below.

Figure 15.9 Excel 2007 Excel Options Add-Ins Dialog Box


In Excel 2007, to activate TreePlan, select Excel Add-ins in the Manage drop-down list shown above, and click the Go button. In the Add-In Manager dialog box, click to put a check in the checkbox for TreePlan, as shown in Figure 15.7, and click OK. To use TreePlan, in the Menu Commands area of the Add-Ins ribbon, choose Decision Tree.

Excel's add-in manager keeps track of the location of the XLA file. To uninstall TreePlan on Windows or Macintosh computers, first delete, move, or rename the XLA file so that Excel can no longer find it. After the XLA file no longer exists where Excel expects to find it, start Excel, choose Tools | Add-Ins, check or uncheck the TreePlan box, and answer the prompt for deleting the add-in from the list. To delete the missing add-in from the list in Excel 2007, choose Office Button | Excel Options | Add-Ins | Manage Excel Add-Ins | Go, select the TreePlan file name in the "Add-Ins available" list, and respond to the prompt to delete it from the list.

## Selective Use: Add-In File in Specified Folder

Copy the TreePlan XLA file to a folder of your choice on the hard drive. For Windows computers, start Excel, choose Tools $\mid$ Add-Ins $\mid$ Browse, navigate to the location of the TreePlan XLA file,
select it, and click OK. To navigate in Excel 2007, choose Office Button | Excel Options | Add-Ins | Manage Add-Ins | Go | Browse. Subsequently, use Excel's Tools | Add-Ins command to load and unload TreePlan as needed by checking or unchecking the TreePlan checkbox.

If you put the TreePlan XLA file in an arbitrary folder on a Windows computer and specify its location using Tools $\mid$ Add-Ins $\mid$ Browse, you should choose Tools $\mid$ Macro $\mid$ Security $\mid$ Trusted Publishers, and check the box for "Trust all installed add-ins and templates."

For Macintosh, start Excel, choose Tools $\mid$ Add-Ins | Select, navigate to the location of the TreePlan XLA file, select it, and click Open.

To uninstall TreePlan, first delete, move, or rename the XLA file, and then follow the same steps for the Library folder described above.

## Steady Use: Add-In File in XLStart Folder

For Windows computers, copy the TreePlan XLA file to the Program Files $\backslash$ Microsoft Office $\backslash$ Office $\backslash$ XLStart folder of your hard drive. The file will be opened every time you start Excel. Alternatively, copy the TreePlan XLA file to Documents and Settings $\backslash$ User name $\backslash$ Application Data $\backslash$ Microsoft $\backslash$ Excel $\backslash$ XLStart, where User name is your Windows user name.

If you put the TreePlan XLA file in an XLStart folder on a Windows computer, you should choose Tools | Macro | Security | Trusted Publishers, and check the box for "Trust all installed add-ins and templates."

For Macintosh, copy the TreePlan XLA file to the Macintosh HD : Applications : Microsoft Office : Office : Startup : Excel folder.

To uninstall TreePlan, delete the XLA file or move the XLA file from the Windows XLStart folder or from the Macintosh Startup : Excel folder.

### 15.3 BUILDING A DECISION TREE IN TREEPLAN

You can start TreePlan either by choosing Tools | Decision Tree from the menu bar or by pressing Ctrl+ Shift + T (hold down the Ctrl and Shift keys and press T). If the worksheet doesn't have a decision tree, TreePlan prompts you with a dialog box with three options; choose New Tree to begin a new tree. TreePlan draws a default initial decision tree with its upper left corner at the selected cell. For example, the figure below shows the initial tree when $\$ B \$ 2$ is selected. (Note that TreePlan writes over existing values in the spreadsheet: begin your tree to the right of the area where your data is stored, and do not subsequently add or delete rows or columns in the treediagram area.)

Figure 15.10 TreePlan Initial Default Decision Tree

|  | A | B |  |  | D | E | F | G | H | I |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 |  |  |  |  |  |  |  |  |  |  |
| 2 |  |  |  |  |  |  |  |  |  |  |
| 3 |  |  |  |  |  | Decision 1 |  |  |  |  |
| 4 |  |  |  |  |  |  |  |  | 0 |  |
| 5 |  |  |  |  |  | 0 | 0 |  |  |  |
| 6 |  |  |  | 1 |  |  |  |  |  |  |
| 7 |  |  |  |  |  |  |  |  |  |  |
| 8 |  |  |  |  |  | Decision 2 |  |  |  |  |
| 9 |  |  |  |  |  |  |  |  | 0 |  |
| 10 |  |  |  |  |  | 0 | 0 |  |  |  |
| 11 |  |  |  |  |  |  |  |  |  |  |

Build up a tree by adding or modifying branches or nodes in the default tree. To change the branch labels or probabilities, click on the cell containing the label or probability and type the new label or probability. To modify the structure of the tree (e.g., add or delete branches or nodes in the tree), select the node or the cell containing the node in the tree to modify, and choose Tools | Decision Tree or press Ctrl+Shift+T. TreePlan will then present a dialog box showing the available commands.

For example, to add an event node to the top branch of the tree shown above, select the square cell (cell G4) next to the vertical line at the end of a terminal branch and press Ctrl+Shift+T. TreePlan then presents this dialog box.

Figure 15.11 TreePlan Terminal Dialog Box


To add an event node to the branch, we change the selected terminal node to an event node by selecting Change to event node in the dialog box, selecting the number of branches (here two), and pressing OK. TreePlan then redraws the tree with a chance node in place of the terminal node.

Figure 15.12 Initial Decision Tree Diagram

|  | A | B | C |  | D | E | F |  | G | H | 1 | J | K | L | M |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 2 |  |  |  |  |  |  |  |  |  |  | 0.5 |  |  |  |  |
| 3 |  |  |  |  |  |  |  |  |  |  | Event 3 |  |  |  |  |
| 4 |  |  |  |  |  |  |  |  |  |  |  |  |  | 0 |  |
| 5 |  |  |  |  |  | Decision 1 |  |  |  |  | 0 | 0 |  |  |  |
| 6 |  |  |  |  |  |  |  |  | O |  |  |  |  |  |  |
| 7 |  |  |  |  |  | 0 |  | 0 |  | - | 0.5 |  |  |  |  |
| 8 |  |  |  |  | , |  |  |  |  | , | Event 4 |  |  |  |  |
| 9 |  |  |  | , |  |  |  |  |  |  |  |  |  | 0 |  |
| 10 |  |  |  | 1 |  |  |  |  |  |  | 0 | 0 |  |  |  |
| 11 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 12 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 13 |  |  |  |  |  | Decision 2 |  |  |  |  |  |  |  |  |  |
| 14 |  |  |  |  |  |  |  |  |  |  |  |  |  | 0 |  |
| 15 |  |  |  |  |  | 0 |  | 0 |  |  |  |  |  |  |  |
| 16 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |

The dialog boxes presented by TreePlan vary depending on what you have selected when you choose Tools $\mid$ Decision Tree or press Ctrl + Shift $+\mathbf{T}$. The dialog box shown below is presented when you press $\mathbf{C t r l}+\mathbf{S h i f t}+\mathbf{T}$ with an event node selected; a similar dialog box is presented when you select a decision node. If you want to add a branch to the selected node, choose Add branch and press OK. If you want to insert a decision or event node before the selected node, choose Insert decision or Insert event and press OK. To get a description of the available commands, click on the Help button.

Figure 15.13 TreePlan Event Dialog Box


The Copy subtree command is particularly useful when building large trees. If two or more parts of the tree are similar, you can copy and paste "subtrees" rather than building up each part separately. To copy a subtree, select the node at the root of the subtree and choose Copy subtree. This tells TreePlan to copy the selected node and everything to the right of it in the tree. To paste this subtree, select a terminal node and choose Paste subtree. TreePlan then duplicates the specified subtree at the selected terminal node.

Since TreePlan decision trees are built directly in Excel, you can use Excel's commands to format your tree. For example, you can use bold or italic fonts for branch labels: select the cells you want to format and change them using Excel's formatting commands. To help you, TreePlan provides a Select dialog box that appears when you choose Tools $\mid$ Decision Tree or press Ctrl+Shift+T without a node selected. You can also bring up this dialog box by pressing the Select button on the Node dialog box. From here, you can select all items of a particular type in the tree. For example, if you choose Probabilities and press OK, TreePlan selects all cells containing probabilities in the tree. You can then format all of the probabilities simultaneously using Excel's formatting commands. (Because of limitations in Excel, the Select dialog box will not be available when working with very large trees.)

### 15.4 ANATOMY OF A TREEPLAN DECISION TREE

An example of a TreePlan decision tree is shown below. In the example, a firm must decide (1) whether to prepare a proposal for a possible contract and (2) which method to use to satisfy the contract. The tree consists of decision nodes, event nodes and terminal nodes connected by branches. Each branch is surrounded by cells containing formulas, cell references, or labels pertaining to that branch. You may edit the labels, probabilities, and partial cash flows associated with each branch. The partial cash flows are the amount the firm "gets paid" to go down that branch. For the scenario with terminal value $\$ 30,000$, the firm pays $\$ 50,000$ if it decides to prepare the proposal, receives $\$ 250,000$ up front if awarded the contract, spends $\$ 50,000$ to try the electronic method, and spends $\$ 120,000$ on the mechanical method if the electronic method fails.

Figure 15.14 Nodes, Labels, Cash Flows, and Probabilities


The trees are "solved" using formulas embedded in the spreadsheet. The terminal values sum all the partial cash flows along the path leading to that terminal node. The tree is then "rolled back" by computing expected values at event nodes and by maximizing at decision nodes; the rollback $E V S$ appear next to each node and show the expected value at that point in the tree. The numbers in the decision nodes indicate which alternative is optimal for that decision. In the example, the "1" in the first decision node indicates that it is optimal to prepare the proposal, and the " 2 " in the second decision node indicates the firm should try the electronic method because that alternative leads to a higher expected value, $\$ 90,000$, than the mechanical method, $\$ 80,000$.

Figure 15.15 Terminal Values, Rollback EVs, and Choice Indicators


TreePlan has a few options that control the way calculations are done in the tree. To select these options, press the Options button in any of TreePlan's dialog boxes. The first choice is whether to Use Expected Values or Use Exponential Utility Function for computing certain equivalents. The default is to rollback the tree using expected values. If you choose to use exponential utilities, TreePlan will compute utilities of endpoint cash flows at the terminal nodes and compute expected utilities instead of expected values at event nodes. Expected utilities are calculated in the cell
below the certain equivalents. You may also choose to Maximize (profits) or Minimize (costs) at decision nodes; the default is to maximize profits. If you choose to minimize costs instead, the cash flows are interpreted as costs, and decisions are made by choosing the minimum expected value or certain equivalent rather than the maximum. See the Help file for details on these options.

### 15.5 TREEPLAN INPUTS AND FORMULAS

Figure 15.16 Influence Chart of TreePlan Inputs and Formulas


Figure 15.17 Explanation of Formulas

| Location | Formula |
| :--- | :--- |
| Terminal Node <br> Endpoint Value | SUM of branch cash flows |
| Event Node <br> Rollback Value | Check that probabilities SUM to <br> approximately one, then SUM <br> products of probabilities times <br> subsequent rollback values |
| Decision Node <br> Rollback Value | MAX or MIN of subsequent <br> rollback values |
| Decision Node <br> Choice Indicator | Nested IF functions |

### 15.6 STEP-BY-STEP TREEPLAN TUTORIAL

A decision tree can be used as a model for a sequential decision problems under uncertainty. A decision tree describes graphically the decisions to be made, the events that may occur, and the
outcomes associated with combinations of decisions and events. Probabilities are assigned to the events, and values are determined for each outcome. A major goal of the analysis is to determine the best decisions.

Decision tree models include such concepts as nodes, branches, terminal values, strategy, payoff distribution, certain equivalent, and the rollback method. The following problem illustrates the basic concepts.

## DriveTek Problem

DriveTek Research Institute discovers that a computer company wants a new storage device for a proposed new computer system. Since the computer company does not have research people available to develop the new storage device, it will subcontract the development to an independent research firm. The computer company has offered a fee of $\$ 250,000$ for the best proposal for developing the new storage device. The contract will go to the firm with the best technical plan and the highest reputation for technical competence.
DriveTek Research Institute wants to enter the competition. Management estimates a cost of $\$ 50,000$ to prepare a proposal with a fifty-fifty chance of winning the contract.
However, DriveTek's engineers are not sure about how they will develop the storage device if they are awarded the contract. Three alternative approaches can be tried. The first approach is a mechanical method with a cost of $\$ 120,000$, and the engineers are certain they can develop a successful model with this approach. A second approach involves electronic components. The engineers estimate that the electronic approach will cost only $\$ 50,000$ to develop a model of the storage device, but with only a 50 percent chance of satisfactory results. A third approach uses magnetic components; this costs $\$ 80,000$, with a 70 percent chance of success.

DriveTek Research can work on only one approach at a time and has time to try only two approaches. If it tries either the magnetic or electronic method and the attempt fails, the second choice must be the mechanical method to guarantee a successful model.
The management of DriveTek Research needs help in incorporating this information into a decision to proceed or not.
[Source: The storage device example is adapted from Spurr and Bonini, Statistical Analysis for Business Decisions, Irwin.]

## Nodes and Branches

Decision trees have three kinds of nodes and two kinds of branches. A decision node is a point where a choice must be made; it is shown as a square. The branches extending from a decision node are decision branches, each branch representing one of the possible alternatives or courses of action available at that point. The set of alternatives must be mutually exclusive (if one is chosen, the others cannot be chosen) and collectively exhaustive (all possible alternatives must be included in the set).

There are two major decisions in the DriveTek problem. First, the company must decide whether or not to prepare a proposal. Second, if it prepares a proposal and is awarded the contract, it must decide which of the three approaches to try to satisfy the contract.

An event node is a point where uncertainty is resolved (a point where the decision maker learns about the occurrence of an event). An event node, sometimes called a "chance node," is shown as a circle. The event set consists of the event branches extending from an event node, each branch
representing one of the possible events that may occur at that point. The set of events must be mutually exclusive (if one occurs, the others cannot occur) and collectively exhaustive (all possible events must be included in the set). Each event is assigned a subjective probability; the sum of probabilities for the events in a set must equal one.

The three sources of uncertainty in the DriveTek problem are: whether it is awarded the contract or not, whether the electronic approach succeeds or fails, and whether the magnetic approach succeeds or fails.

In general, decision nodes and branches represent the controllable factors in a decision problem; event nodes and branches represent uncontrollable factors.
Decision nodes and event nodes are arranged in order of subjective chronology. For example, the position of an event node corresponds to the time when the decision maker learns the outcome of the event (not necessarily when the event occurs).

The third kind of node is a terminal node, representing the final result of a combination of decisions and events. Terminal nodes are the endpoints of a decision tree, shown as the end of a branch on hand-drawn diagrams and as a triangle on computer-generated diagrams.

The following table shows the three kinds of nodes and two kinds of branches used to represent a decision tree.

Figure 15.18 Nodes and Symbols

| Type of Node | Written Symbol | Computer Symbol | Node Successor |
| :---: | :---: | :---: | :---: |
| Decision | square | square | decision branches |
| Event | circle | circle | event branches |
| Terminal | endpoint | triangle or bar | terminal value |

## Terminal Values

Each terminal node has an associated terminal value, sometimes called a payoff value, outcome value, or endpoint value. Each terminal value measures the result of a scenario: the sequence of decisions and events on a unique path leading from the initial decision node to a specific terminal node.

To determine the terminal value, one approach assigns a cash flow value to each decision branch and event branch and then sum the cash flow values on the branches leading to a terminal node to determine the terminal value. In the DriveTek problem, there are distinct cash flows associated with many of the decision and event branches. Some problems require a more elaborate value model to determine the terminal values.

The following diagram shows the arrangement of branch names, probabilities, and cash flow values on an unsolved tree.

Figure 15.19 DriveTek Decision Tree Diagram


To build the decision tree, you use TreePlan's dialog boxes to develop the structure. You enter a branch name, branch cash flow, and branch probability (for an event) in the cells above and below the left side of each branch. As you build the tree diagram, TreePlan enters formulas in other cells.

## Building the Tree Diagram

1. Start with a new worksheet. (If no workbook is open, choose File |New. If a workbook is open, choose Insert | Worksheet.)
2. Select cell A1. From the Tools menu, choose Decision Tree. In the TreePlan New dialog box, click the New Tree button. A decision node with two branches appears.

Figure 15.20 TreePlan New Dialog Box


Figure 15.21 Initial Decision Tree Diagram

|  | A | B | C | D | E | F | G |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 |  |  |  |  |  |  |  |
| 2 |  |  |  | Decision 1 |  |  |  |
| 3 |  |  |  |  |  |  | 0 |
| 4 |  |  |  | 0 | 0 |  |  |
| 5 |  |  |  |  |  |  |  |
| 6 |  |  | $\rangle$ |  |  |  |  |
| 7 |  |  |  | Decision 2 |  |  |  |
| 8 |  |  |  |  |  |  | 0 |
| 9 |  |  |  | 0 | 0 |  |  |

3. Do not type the quotation marks in the following instructions. Select cell D2, and enter Prepare proposal. Select cell D4, and enter $\mathbf{- 5 0 0 0 0}$. Select cell D7, and enter Don't prepare proposal.

Figure 15.22 Branch Names and Cash Flow

|  | A | B | C | D | E | F | G |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 |  |  |  |  |  |  |  |
| 2 |  |  |  | Prepare prop | sal |  |  |
| 3 |  |  |  |  |  |  | -50000 |
| 4 |  |  | - | -50000 | -50000 |  |  |
| 5 |  |  | , |  |  |  |  |
| 6 |  |  | - |  |  |  |  |
| 7 |  |  | , | Don't prepa | proposal |  |  |
| 8 |  |  |  |  |  |  | 0 |
| 9 |  |  |  | 0 | 0 |  |  |

4. Select cell F3. From the Tools menu, choose Decision Tree. In the TreePlan Terminal dialog box, select Change To Event Node, select Two Branches, and click OK. The tree is redrawn.

Figure 15.23 TreePlan Terminal Dialog Box

| TreePlan...Terminal |  | ? |
| :---: | :---: | :---: |
| Change to decision node <br> Change to event node <br> Paste subtree <br> Remove previous branch |  | Branches <br> $C$ One <br> © Two <br> $C$ Three <br> $C$ Four <br> $C$ Five |
|  |  |  |
|  |  |  |
|  |  |  |
|  |  |  |
| OK | Options... |  |
| Cancel | Help | Select... |

Figure 15.24 Initial Event Branches

|  | A | B |  | C | D | E | F | G | H | 1 | J | K |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 |  |  |  |  |  |  |  |  | 0.5 |  |  |  |
| 2 |  |  |  |  |  |  |  |  | Event 3 |  |  |  |
| 3 |  |  |  |  |  |  |  |  |  |  |  | -50000 |
| 4 |  |  |  |  | Prepare prop | sal |  |  | 0 | -50000 |  |  |
| 5 |  |  |  |  |  |  | ) |  |  |  |  |  |
| 6 |  |  |  | / | -50000 | -50000 |  | > | 0.5 |  |  |  |
| 7 |  |  |  | - |  |  |  | , | Event 4 |  |  |  |
| 8 |  |  | , |  |  |  |  |  |  |  |  | -50000 |
| 9 |  |  | 2 |  |  |  |  |  | 0 | -50000 |  |  |
| 10 |  |  |  |  |  |  |  |  |  |  |  |  |
| 11 |  |  |  |  |  |  |  |  |  |  |  |  |
| 12 |  |  |  | , | Don't prepa | proposal |  |  |  |  |  |  |
| 13 |  |  |  |  |  |  |  |  |  |  |  | 0 |
| 14 |  |  |  |  | 0 | 0 |  |  |  |  |  |  |

5. Select cell H2, and enter Awarded contract. Select cell H4, and enter 250000. Select cell H7, and enter Not awarded contract.

Figure 15.25 Event Branches With Names and Cash Flow

|  | A | B | C | D | E | F | G | H | 1 | J | K |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 |  |  |  |  |  |  |  | 0.5 |  |  |  |
| 2 |  |  |  |  |  |  |  | Awarded con | ract |  |  |
| 3 |  |  |  |  |  |  |  |  |  |  | 200000 |
| 4 |  |  |  | Prepare prop |  |  | - | 250000 | 200000 |  |  |
| 5 |  |  |  |  |  | ) |  |  |  |  |  |
| 6 |  |  |  | -50000 | 75000 |  | , | 0.5 |  |  |  |
| 7 |  |  | - |  |  |  | , | Not awarde | contract |  |  |
| 8 |  |  | , |  |  |  |  |  |  |  | -50000 |
| 9 |  | 1 |  |  |  |  |  | 0 | -50000 |  |  |
| 10 | 75000 |  | , |  |  |  |  |  |  |  |  |
| 11 |  |  | , |  |  |  |  |  |  |  |  |
| 12 |  |  |  | Don't prepa | proposal |  |  |  |  |  |  |
| 13 |  |  |  |  |  |  |  |  |  |  | 0 |
| 14 |  |  |  | 0 | 0 |  |  |  |  |  |  |

6. Select cell J3. From the Tools menu, choose Decision Tree. In the TreePlan Terminal dialog box, select Change To Decision Node, select Three Branches, and click OK. The tree is redrawn.

Figure 15.26 Subsequent Decision Branches

|  | A | B | C | D | E | F | G | H | 1 | J | K | L | M | N | 0 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 2 |  |  |  |  |  |  |  |  |  |  |  | Decision 5 |  |  |  |
| 3 |  |  |  |  |  |  |  |  |  |  |  |  |  |  | 200000 |
| 4 |  |  |  |  |  |  |  |  |  |  |  | 0 | 200000 |  |  |
| 5 |  |  |  |  |  |  |  |  |  |  | - |  |  |  |  |
| 6 |  |  |  |  |  |  |  | 0.5 |  |  | - |  |  |  |  |
| 7 |  |  |  |  |  |  |  | Awarded co | ract |  |  | Decision 6 |  |  |  |
| 8 |  |  |  |  |  |  |  |  |  | 1 |  |  |  |  | 200000 |
| 9 |  |  |  |  |  |  |  | 250000 | 200000 |  |  | 0 | 200000 |  |  |
| 10 |  |  |  |  |  |  | 1 |  |  |  | , |  |  |  |  |
| 11 |  |  |  |  |  |  | \% |  |  |  | , |  |  |  |  |
| 12 |  |  |  | Prepare pro |  |  |  |  |  |  |  | Decision 7 |  |  |  |
| 13 |  |  |  |  |  | O |  |  |  |  |  |  |  |  | 200000 |
| 14 |  |  | - | -50000 | 75000 |  |  |  |  |  |  | 0 | 200000 |  |  |
| 15 |  |  | 1 |  |  |  | , |  |  |  |  |  |  |  |  |
| 16 |  |  | , |  |  |  | , | 0.5 |  |  |  |  |  |  |  |
| 17 |  |  |  |  |  |  |  | Not awarde | contract |  |  |  |  |  |  |
| 18 |  | 1 |  |  |  |  |  |  |  |  |  |  |  |  | -50000 |
| 19 | 75000 |  |  |  |  |  |  | 0 | -50000 |  |  |  |  |  |  |
| 20 |  |  | , |  |  |  |  |  |  |  |  |  |  |  |  |
| 21 |  |  | , |  |  |  |  |  |  |  |  |  |  |  |  |
| 22 |  |  |  | Don't prepa | proposal |  |  |  |  |  |  |  |  |  |  |
| 23 |  |  |  |  |  |  |  |  |  |  |  |  |  |  | 0 |
| 24 |  |  |  | 0 | 0 |  |  |  |  |  |  |  |  |  |  |

7. Select cell L2, and enter Use mechanical method. Select cell L4, and enter $\mathbf{- 1 2 0 0 0 0}$. Select cell L7, and enter Try electronic method. Select cell L9, and enter-50000. Select cell L12, and enter Try magnetic method. Select cell L14, and enter $\mathbf{- 8 0 0 0 0}$.

Figure 15.27 Subsequent Decision Branches With Names and Cash Flows

|  | A | B | C | D | E | F | G | H | 1 | J | K | L | M | N | 0 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 2 |  |  |  |  |  |  |  |  |  |  |  | Use mecha | al metho |  |  |
| 3 |  |  |  |  |  |  |  |  |  |  |  |  |  |  | 80000 |
| 4 |  |  |  |  |  |  |  |  |  |  |  | -120000 | 80000 |  |  |
| 5 |  |  |  |  |  |  |  |  |  |  | - |  |  |  |  |
| 6 |  |  |  |  |  |  |  | 0.5 |  |  | / |  |  |  |  |
| 7 |  |  |  |  |  |  |  | Awarded co | ract |  |  | Try electron | method |  |  |
| 8 |  |  |  |  |  |  |  |  |  | 2 |  |  |  |  | 150000 |
| 9 |  |  |  |  |  |  | , | 250000 | 150000 |  |  | -50000 | 150000 |  |  |
| 10 |  |  |  |  |  |  | 1 |  |  |  | , |  |  |  |  |
| 11 |  |  |  |  |  |  | / |  |  |  | , |  |  |  |  |
| 12 |  |  |  | Prepare prop |  |  |  |  |  |  |  | Try magnetio | method |  |  |
| 13 |  |  |  |  |  | $\bigcirc$ |  |  |  |  |  |  |  |  | 120000 |
| 14 |  |  | - | -50000 | 50000 |  |  |  |  |  |  | -80000 | 120000 |  |  |
| 15 |  |  | - |  |  |  | , |  |  |  |  |  |  |  |  |
| 16 |  |  | / |  |  |  | , | 0.5 |  |  |  |  |  |  |  |
| 17 |  |  |  |  |  |  |  | Not awarded | contract |  |  |  |  |  |  |
| 18 |  | 1 |  |  |  |  |  |  |  |  |  |  |  |  | -50000 |
| 19 | 50000 |  |  |  |  |  |  | 0 | -50000 |  |  |  |  |  |  |
| 20 |  |  | $\checkmark$ |  |  |  |  |  |  |  |  |  |  |  |  |
| 21 |  |  | , |  |  |  |  |  |  |  |  |  |  |  |  |
| 22 |  |  |  | Don't prepa | proposal |  |  |  |  |  |  |  |  |  |  |
| 23 |  |  |  |  |  |  |  |  |  |  |  |  |  |  | 0 |
| 24 |  |  |  | 0 | 0 |  |  |  |  |  |  |  |  |  |  |

8. Select cell N8. From the Tools menu, choose Decision Tree. In the TreePlan Terminal dialog box, select Change To Event Node, select Two Branches, and click OK. The tree is redrawn.

Figure 15.28 Branches for Electronic Method Uncertainty

9. Select cell P7, and enter Electronic success. Select cell P12, and enter Electronic failure. Select cell P14, and enter $\mathbf{- 1 2 0 0 0 0}$.

Figure 15.29 Branch Names and Cash Flows for Electronic Method Uncertainty

10. Select cell N18. From the Tools menu, choose Decision Tree. In the TreePlan Terminal dialog box, select Change To Event Node, select Two Branches, and click OK. The tree is redrawn.

Figure 15.30 Branches for Magnetic Method Uncertainty

11. Select cell P16, and enter .7. Select cell P17, and enter Magnetic success. Select cell P21, and enter .3. Select cell P22, and enter Magnetic failure. Select cell P24, and enter -120000 .

Figure 15.31 Complete Diagram Before Formatting

12. Double-click the sheet tab (or right-click the sheet tab and choose Rename from the shortcut menu), and enter Original. Save the workbook.

## Interpreting the Results

The $\$ 30,000$ terminal value on the far right of the diagram in cell S13 is associated with the following scenario:

Figure 15.32 Evaluation of a Scenario

| Branch Type |  | Branch Name |  |
| :--- | :--- | :--- | :--- |
| Decision | Prepare proposal Flow |  |  |
| Event |  | Awarded contract | $\$ 50,000$ |
| Decision | Try electronic method | $\$ 250,000$ |  |
| Event | Electronic failure (Use mechanical method) |  | $-\$ 50,000$ |
|  | Terminal value | $\$ 30,000$ |  |
|  |  | $\$ 30,000$ |  |

TreePlan put the formula $=\mathrm{SUM}(\mathrm{P} 14, \mathrm{~L} 11, \mathrm{H} 12, \mathrm{D} 20)$ into cell S13 for determining the terminal value.
Other formulas, called rollback formulas, are in cells below and to the left of each node. These formulas are used to determine the optimal choice at each decision node.

In cell B26, a formula displays 1, indicating that the first branch is the optimal choice. Thus, the initial choice is to prepare the proposal. In cell J11, a formula displays 2, indicating that the second branch (numbered 1,2 , and 3 , from top to bottom) is the optimal choice. If awarded the
contract, DriveTek should try the electronic method. A subsequent chapter provides more details about interpretation.

## Formatting the Tree Diagram

The following steps show how to use TreePlan and Excel features to format the tree diagram. You may choose to use other formats for your own tree diagrams.
13. From the Edit menu, choose Move or Copy Sheet (or right-click the sheet tab and choose Move Or Copy from the shortcut menu). In the lower left corner of the Move Or Copy dialog box, check the Create A Copy box, and click OK.
14.On sheet Original (2), select cell H9. From the Tools menu, choose Decision Tree. In the TreePlan Select dialog box, verify that the option button for Cells with Probabilities is selected, and click OK. With all probability cells selected, click the Align Left button.

Figure 15.33 TreePlan Select Dialog Box

15. Select cell H12. From the Tools menu, choose Decision Tree. In the TreePlan Select dialog box, verify that the option button for Cells with Partial Cash Flows is selected, and click OK. With all partial cash flow cells selected, click the Align Left button. With those cells still selected, choose Format $\mid$ Cells. In the Format Cells dialog box, click the Number tab. In the Category list box, choose Currency; type 0 (zero) for Decimal Places; select \$ in the Symbol list box; select -\$1,234 for Negative Numbers. Click OK.

Figure 15.34 Excel Format Cells Dialog Box

16. Select cell I12. From the Tools menu, choose Decision Tree. In the TreePlan Select dialog box, verify that the option button for Cells with Rollback EVs/CEs is selected, and click OK. With all rollback cells selected, choose Format | Cells. Repeat the Currency formatting of step 16 above.
17. Select cell S3. From the Tools menu, choose Decision Tree. In the TreePlan Select dialog box, verify that the option button for Cells with Terminal Values is selected, and click OK. With all terminal value cells selected, choose Format | Cells. Repeat the Currency formatting of step 16 above.

Figure 15.35 Complete DriveTek Decision Tree

|  | A | B | C | D | E | F | G | H | 1 | $J$ | K | L | M | N | 0 | P | Q | R | S |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 2 |  |  |  |  |  |  |  |  |  |  |  | Use mecha | al method |  |  |  |  |  |  |
| 3 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  | \$80,000 |
| 4 |  |  |  |  |  |  |  |  |  |  |  | -\$120,000 | \$80,000 |  |  |  |  |  |  |
| 5 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 6 |  |  |  |  |  |  |  |  |  |  | - |  |  |  |  | 0.5 |  |  |  |
| 7 |  |  |  |  |  |  |  |  |  |  | , |  |  |  |  | Electronic | cess |  |  |
| 8 |  |  |  |  |  |  |  |  |  |  | - |  |  |  |  |  |  |  | \$150,000 |
| 9 |  |  |  |  |  |  |  | 0.5 |  |  | , | Try electron | method |  | - | \$0 | \$150,000 |  |  |
| 10 |  |  |  |  |  |  |  | Awarded c | tract |  |  |  |  | O |  |  |  |  |  |
| 11 |  |  |  |  |  |  |  |  |  | 2 |  | -\$50,000 | \$90,000 |  | , | 0.5 |  |  |  |
| 12 |  |  |  |  |  |  |  | \$250,000 | \$90,000 |  |  |  |  |  |  | Electronic | ure |  |  |
| 13 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  | \$30,000 |
| 14 |  |  |  |  |  |  | - |  |  |  | , |  |  |  |  | -\$120,000 | \$30,000 |  |  |
| 15 |  |  |  |  |  |  | - |  |  |  | , |  |  |  |  |  |  |  |  |
| 16 |  |  |  |  |  |  | , |  |  |  | $\bigcirc$ |  |  |  |  | 0.7 |  |  |  |
| 17 |  |  |  |  |  |  | - |  |  |  |  |  |  |  |  | Magnetic s | cess |  |  |
| 18 |  |  |  | Prepare p | sal |  |  |  |  |  |  |  |  |  |  |  |  |  | \$120,000 |
| 19 |  |  |  |  |  | $\bigcirc$ |  |  |  |  |  | Try magne | method |  | 1 | \$0 | \$120,000 |  |  |
| 20 |  |  |  | -\$50,000 | \$20,000 |  |  |  |  |  |  |  |  | , |  |  |  |  |  |
| 21 |  |  | - |  |  |  |  |  |  |  |  | -\$80,000 | \$84,000 |  | , | 0.3 |  |  |  |
| 22 |  |  | - |  |  |  | - |  |  |  |  |  |  |  | , | Magnetic fa |  |  |  |
| 23 |  |  | , |  |  |  | , |  |  |  |  |  |  |  |  |  |  |  | \$0 |
| 24 |  |  | , |  |  |  | - |  |  |  |  |  |  |  |  | -\$120,000 | \$0 |  |  |
| 25 |  | , |  |  |  |  | $\bigcirc$ |  |  |  |  |  |  |  |  |  |  |  |  |
| 26 |  | 1. |  |  |  |  |  | 0.5 |  |  |  |  |  |  |  |  |  |  |  |
| 27 | \$20,000 |  |  |  |  |  |  | Not award | contract |  |  |  |  |  |  |  |  |  |  |
| 28 |  |  | - |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  | -\$50,000 |
| 29 |  |  | $\bigcirc$ |  |  |  |  | \$0 | -\$50,000 |  |  |  |  |  |  |  |  |  |  |
| 30 |  |  | $\bigcirc$ |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 31 |  |  | , |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 32 |  |  |  | Don't prep | proposal |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 33 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  | \$0 |
| 34 |  |  |  | \$0 | \$0 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |

18. Double-click the Original (2) sheet tab (or right-click the sheet tab and choose Rename from the shortcut menu), and enter Formatted. Save the workbook.

## Displaying Model Inputs

When you build a decision tree model, you may want to discuss the model and its assumptions with co-workers or a client. For such communication it may be preferable to hide the results of formulas that show rollback values and decision node choices. The following steps show how to display only the model inputs.
19. From the Edit menu, choose Move or Copy Sheet (or right-click the sheet tab and choose Move Or Copy from the shortcut menu). In the lower left corner of the Move Or Copy dialog box, check the Create A Copy box, and click OK.
20. On sheet Formatted (2), select cell B1. From the Tools menu, choose Decision Tree. In the TreePlan Select dialog box, verify that the option button for Columns with Nodes is selected, and click OK. With all node columns selected, choose Format | Cells | Number. In the Category list box, select Custom. Select the entry in the Type edit box, and type ;;; (three semicolons). Click OK.

Figure 15.36 Excel Format Cells Dialog Box


Explanation: A custom number format has four sections of format codes. The sections are separated by semicolons, and they define the formats for positive numbers, negative numbers, zero values, and text, in that order. When you specify three semicolons without format codes, Excel does not display positive numbers, negative numbers, zero values, or text. The formula remains in the cell, but its result is not displayed. Later, if you want to display the result, you can change the format without having to enter the formula again. Editing an existing format does not delete it. All formats are saved with the workbook unless you explicitly delete a format.
21. Select cell A27. From the Tools menu, choose Decision Tree. In the TreePlan Select dialog box, verify that the option button for Cells with Rollback EVs/CEs is selected, and click OK. With all rollback values selected, choose Format | Cells | Number. In the Category list box, select Custom. Scroll to the bottom of the Type list box, and select the three-semicolon entry. Click OK.
22. Double-click the Formatted (2) sheet tab (or right-click the sheet tab and choose Rename from the shortcut menu), and enter Model Inputs. Save the workbook.

## Printing the Tree Diagram

23. In the Name Box list box, select TreeDiagram (or select cells A1:S34).
24. To print the tree diagram from Excel, with the tree diagram range selected choose File | Print Area $\mid$ Set Print Area. Choose File \| Page Setup. In the Page Setup dialog box, click the Page tab; for Orientation click the option button for Landscape, and for Scaling click the option button for Fit To 1 Page Wide By 1 Page Tall. Click the Header/Footer tab; in the Header list box select None, and in the Footer list box select None (or select other appropriate headers and footers). Click the Sheet tab; clear the check box for Gridlines, and clear the check box for Row And Column Headings. Click OK. Choose File | Print and click OK.
25. To print the tree diagram from Word, clear the check boxes for Gridlines and for Row And Column Headings on Excel's Page Setup dialog box Sheet tab. Select the tree diagram range. Hold down the Shift key and from the Edit menu choose Copy Picture. In the Copy Picture dialog box, click the option button As Shown When Printed, and click OK. In Word select the location where you want to paste the tree diagram and choose Edit | Paste.

Figure 15.37 DriveTek Without Rollback Values


## Alternative Model

If you want to emphasize that the time constraint forces DriveTek to use the mechanical approach if they try either of the uncertain approaches and experience a failure, you can change the terminal nodes in cells R13 and R23 to decision nodes, each with a single branch.

Figure 15.38 Alternative DriveTek Decision Tree


### 15.7 EXPONENTIAL UTILITY AND TREEPLAN

TreePlan's default is to rollback the tree using expected value (probability-weighted average) at an event node and maximum of successor values at a decision node. If you choose to use exponential utilities in TreePlan's Options dialog box, TreePlan will redraw the decision tree diagram with formulas for computing the utility and certain equivalent at each node.

Figure 15.39 TreePlan Options Dialog Box


For the Maximize option with exponential utility, the rollback formulas are $\mathrm{U}=\mathrm{A}-\mathrm{B}^{*} \operatorname{EXP}(\mathrm{X} / \mathrm{RT})$ and $\mathrm{CE}=-\mathrm{LN}((\mathrm{A}-\mathrm{EU}) / \mathrm{B}) * \mathrm{RT}$, where X and EU are cell references. For the Minimize option with exponential utility, the formulas are $\mathrm{U}=\mathrm{A}-\mathrm{B}^{*} \mathrm{EXP}(\mathrm{X} / \mathrm{RT})$ and $\mathrm{CE}=\mathrm{LN}((\mathrm{A}-\mathrm{EU}) / \mathrm{B}) * \mathrm{RT}$.

TreePlan uses the name RT to represent the risk tolerance parameter of the exponential utility function. The names A and B determine scaling. If the names $\mathrm{A}, \mathrm{B}$, and RT don't exist on the worksheet when you choose to use exponential utility, they are initially defined as $A=1, B=1$, and RT=999999999999. You can change the values of the names using the Insert | Name | Define command.

### 15.8 ACKNOWLEDGEMENT

TreePlan was developed by Professor Michael R. Middleton at the University of San Francisco and modified for use at Fuqua (Duke University) by Professor James E. Smith.

