

Handbook on Import Risk Analysis for Animals and Animal Products

Volume 2.

Quantitative risk assessment

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