1

Simplify the expression by using the definition and properties of logarithms.

$$\log_{10} 9000 - \log_{10} 9$$

#### Problem code:

copc06.05.04.01

2 Simplify the expression by using the definition and properties of logarithms.

$$\log_{10} 400 + \log_{10} \left(\frac{5}{2}\right)$$

#### Problem code:

copc06.05.04.02

3 Simplify the expression by using the definition and properties of logarithms.

$$\ln e^3 - \ln e$$

### Problem code:

copc06.05.04.06

4 Write the expression as a single logarithm with a coefficient of 1.

$$\log_{10} 40 + \log_{10} 4$$

a. 
$$\log_{10}$$
 44 b.  $\log_{10}$  166 c.  $\log_{10}$  160 d.  $\log_{160}$  10 e.  $\log_{10}$  36

## Problem code:

copc06.05.04.11m

5 Write the expression as a single logarithm with a coefficient of 1.

$$2\log_{10} x - 5\log_{10} y$$

a. 
$$-3 \log_{10} \left(\frac{x}{y}\right)$$
 c.  $\log_{10} \frac{x^2}{y^5}$  e.  $\log_{10} (2x - 5y)$ 

c. 
$$\log_{10} \frac{x^2}{y^5}$$

e. 
$$\log_{10} (2x - 5y)$$

b. 
$$\log_{10} \left( x^2 - y^5 \right)$$
 d.  $\log_{10} \frac{2x}{5y}$ 

d. 
$$\log_{10} \frac{2x}{5y}$$

Problem code:

copc06.05.04.12m

6

Write the quantity using sums and differences of simpler logarithmic expressions. Express the answer so that logarithms of products, quotients, and powers do not appear.

$$\ln \frac{x^7}{\sqrt[3]{1+x^7}}$$

a. 
$$7 \ln x - \frac{1}{3} \ln \left( 1 + x^7 \right)$$

d. 
$$\frac{2 \ln x}{\ln \left(1 + x^{7}\right)}$$

b. 
$$9 \ln x - 7 \ln (1 + x)$$

e. 
$$2 \ln x + 3 \ln (1 + x^7)$$

c. 
$$7 \ln x^{-7} - 3 \ln (1 + x^{-7})$$

### Problem code:

copc06.05.04.21m

7

Write the quantity using sums and differences of simpler logarithmic expressions. Express the answer so that logarithms of products, quotients, and powers do not appear.

$$\ln \frac{x \sqrt[9]{8x + 1}}{4x + 1}$$

a. 
$$\frac{9 \ln x + \ln (8x + 1)}{\ln (4x + 1)}$$

d. 
$$\frac{1}{9} \ln x + \ln (8x) + \frac{1}{9(4x + 1)}$$

b. 
$$\ln x + \frac{1}{9} \ln (8x + 1) - \ln \frac{1}{4x + 1}$$

e. 
$$\ln x + \ln \frac{8x + 1}{9} - \ln (4x + 1)$$

c. 
$$\ln x + \frac{1}{9} \ln (8x + 1) - \ln (4x + 1)$$

Problem code:

copc06.05.04.22m

Suppose that  $\log_{10} A = a$ ,  $\log_{10} B = b$ , and  $\log_{10} C = c$ . Express the following logarithms in terms of a, b, and c. 8

$$\log_{10}\left(10A/\sqrt[4]{BC}\right)$$

a. 
$$2 + 4a - b - a$$

c. 
$$\frac{4a}{bc}$$

a. 
$$2 + 4a - b - c$$
 c.  $\frac{4a}{bc}$  e.  $1 + a - \frac{1}{4}b - \frac{1}{4}c$ 

b. 
$$10 + a + \frac{1}{4}b + c$$
 d.  $\frac{1 \cdot a}{\sqrt[4]{b \cdot c}}$ 

d. 
$$\frac{1 \cdot a}{\sqrt[4]{b \cdot c}}$$

Problem code:

copc06.05.04.37m

9 Solve the equation. Express the answer in terms of natural logarithms.

$$5 = 2e^{2x - 1}$$

a. 
$$x = \ln 2 + \ln 5 +$$

a. 
$$x = \ln 2 + \ln 5 + 1$$
 c.  $x = \frac{\ln 5 - \ln 2 + 1}{2}$  e.  $x = \ln 5 - \ln 2 + 1$ 

e. 
$$x = \ln 5 - \ln 2 + 1$$

b. 
$$x = \left(\frac{\ln 5}{2} + 1\right) \div 2$$
 d.  $x = \frac{\ln 2 + \ln 5 + 1}{4}$ 

d. 
$$x = \frac{\ln 2 + \ln 5 + 1}{4}$$

Problem code: copc06.05.04.43m

10 Solve the equation. Express the answer in terms of natural logarithms.

$$5e^{3+t} = 3$$

a. 
$$t = \ln 5 - \ln 3 + 1$$

a. 
$$t = \ln 5 - \ln 3 + 3$$
 c.  $t = -\frac{\ln 3 + 3}{5}$  e.  $t = \frac{\ln 3}{5} - 3$ 

e. 
$$t = \frac{\ln 3}{5} - 3$$

b. 
$$t = \ln 3 - \ln 5 - 3$$
 d.  $t = \frac{\ln 5 - 3}{3}$ 

d. 
$$t = \frac{\ln 5 - 3}{3}$$

Problem code:

copc06.05.04.44m

Class:\_\_\_\_

Date: \_\_\_\_\_

Express the quantity in terms of base 10 logarithms.

 $\log_2 7$ 

a. 
$$\log_{10} 7 + \log_{10} 2$$
 c.  $\log_{10} 7 - \log_{10} 2$  e.  $\log_{10} 14$ 

c. 
$$\log_{10} 7 - \log_{10} 2$$

b. 
$$(\log_{10} 7)(\log_{10} 2)$$

d. 
$$\frac{\log_{10} 7}{\log_{10} 2}$$

Problem code:

copc06.05.04.51m

12 Express the quantity in terms of base 10 logarithms.

$$\log_6 10$$

a. 
$$1 - \log_{10} 6$$
 b.  $\log_{10} 6$  c.  $1 + \log_{10} 6$ 

b. 
$$\log_{10} 6$$

d. 
$$\frac{1}{\log_{10} 6}$$

e. log <sub>10</sub> 60

Problem code:

copc06.05.04.52m

13 Express the quantity in terms of natural logarithms.

e. 
$$\frac{\ln 5}{\ln 10}$$

d. 
$$\ln 5 + \ln 10$$

Problem code:

copc06.05.04.57m

# ANSWER KEY

# Homework 5.4 Math 3 Fall 2006, Bauerle

1.3 2.3 3.2 4.c 5.c 6.a 7.c 8.e 9.c 10.b 11.d 12.d 13.e