<u>7.Math.1.1</u> Proportional reasoning involves comparisons and multiplicative relationships among ratios

Essential Questions - 21st Century Skills and Readiness Competencies:	Evidence Outcomes:
1. What information can be determined from a relative comparison that cannot be determined from an absolute comparison?	1. Analyze proportional relationships and use them to solve real-world and mathematical problems.
2. What comparisons can be made using ratios?	2. Compute unit rates associated with ratios of fractions, including ratios of lengths, areas and other quantities measured in like or different units.
3. How do you know when a proportional relationship exists?	3. Identify and represent proportional relationships between quantities.
4. How can proportion be used to argue fairness?	a. Determine whether two quantities are in a proportional relationship.
5. When is it better to use an absolute comparison?	b. Identify the constant of proportionality
6. When is it better to use a relative comparison?	diagrams, and verbal descriptions of proportional relationships.
7. How does using ratios, rates, and proportions allow for sound decision-making in daily life?	c. Represent proportional relationships by equations.
8. What information can we get from ratios, rates, and proportions?	d. Explain what a point (x, y) on the graph of a proportional relationship means in terms of the situation, with special attention to the points $(0, 0)$ and $(1, r)$
9. How is proportional reasoning used in the work place?	4. Use proportional relationships to solve multi-step ratio and percent problems.
	a. Estimate and compute unit cost of consumables (to include unit conversions if necessary) sold in quantity to make purchase decisions based on cost and practicality.
	b. Solve problems involving percent of a number, discounts, taxes, simple interest, percent increase, and percent decrease.

Academic Vocabulary:	Assessment:
	All assessments are found in the suggested
proportion	activities links, correlating with their
ratio	numbers, unless listed below.
unit rate	
percent	1. Assess this lesson with the activity Design
rate	on a Dime performance task, pp. 27-32.
unit cost	
absolute comparison	2. Use the What's Your Rate worksheets and
equation	assessment questions included in the lesson.
unit conversion	2 Aggaggment will be reasonableness of the
interest	3. Assessment will be reasonableness of the
tax	allswel.
	4 Use the In Your Shadow worksheets and
	assessment questions included in the lesson
	ussessment questions metuded in the resson.
	5. Assessments of Ratio, Rate, and Proportion
	are located in lesson plans, pp. 5-14.
	6. Use the Thirsty for Ratios Assessment link.
	2. What's Your Rate
	4. In Your Shadow
	6 Thirsty for Ratios Assessment
Suggested Activities/Strategies:	Bosourcos/Tachnology:
Suggesteu Activities/Strategies.	Resources/rechnology.
For all activities listed below the links are	PARCC offers instructional and assessment
numbered to correlate with each activity.	support. Click on the tab "In the Classroom"
	and at the model frameworks for math.
1. Use the Proportion Unit Lesson Plan where	
students will discover how everyday situations	Illustrative Mathematics contains examples of
can be represented mathematically through	tasks designed by the makers of the CCSS-M
proportional relationships.	(Common Core State Standards of
	Mathematics.)
2. Use the Measure Up: What's Your	
Rate? Activity where students learn to write	Inside Mathematics has tasks, rubrics, and
and solve proportions by gathering data and	discussion questions that correlate with
calculating unit rates.	PARCC and Smarter Balance.
	Math Animum has soul (i. 1. i.
5. Use the Figure 1 his Activity where	<u>Initian Arizona</u> has explanations and overviews
and their arms	nor now the mathematics strands progress from
	one year to the next.
3. Use the Figure This Activity where individuals measure the length of their nose and their arms.	Math Arizona has explanations and overviews for how the mathematics strands progress from one year to the next.

4. In the Measure Up: In Your Shadow Lesson, students extend their knowledge of proportions to solve problems of similarity.	Math Shell is Mathematics Assessment Resource Service (MARS) from the Shell Centre in Nottingham, England and it contains a number of performance tasks.
5. Use the Ratio, Rate, Proportion Lesson Plan for students to compare quantities using ratios, rates, and proportions.6. In the Thirsty for Ratios Lesson Plan, the students will learn what a ratio is and how it	<u>Achieve the Core</u> is from Student Achievement Partners, a nonprofit organization that assembles educators and researchers to design actions based in evidence that will substantially improve student achievement.
can be used in comparison. 7. Use the Ratio/Rate Lesson Plan to teach how a ratio expresses the comparison between two quantities.	Balanced Assessments is a site with free performance tasks to use in your classroom.
8. If you have a Smart Board or Airliner, go to Smart Exchange and choose from a selection of free lessons.	Brain Camp Interactive Game Site Slope and Rate of Change Rate of Change Practice Problems
9. Go to <u>Share My Lesson</u> and choose from a variety of lessons over Percent, Ratios, Rates, etc.	Straight Line and Slope Unit Rate Interactive Games Math Games
1. Proportion Unit Lesson Plan	Proportional Reasoning Lesson Plan Review of Ratios Math Village
2. What's Your Rate 3. Figure This 4. In Your Shadow	Radio Blaster Ratio Game Link to Multiple Games Math Games with Ratios
 5. Ratio, Rate, Proportion Lesson Plan 6. Thirsty for Ratios 6. Thirsty for Ratios: Scaling Ratios 	Better Lesson Site with Multiple Resources Percent Practice Problems Video on Percent Problems
6. Thirsty for Ratios: Proper Mixtures 7. Ratio/Rate Lesson Plan 8. Smart Exchange	
9. Share My Lesson	

<u>7.Math.1.2</u> Formulate, represent, and use algorithms with rational numbers flexibly, accurately, and efficiently

accurately, and efficiently	
Essential Questions - 21st Century Skills	Evidence Outcomes:
and Readiness Competencies:1. How do operations with rational numbers compare to operations with integers?	1. Apply understandings of addition and subtraction to add and subtract rational numbers including integers.
2. How do you know if a computational strategy is sensible?3. How is 0.9 equal to one? How is 0.9 not equal to one?	a. Represent addition and subtraction on a horizontal or vertical number line diagram.b. Describe situations in which opposite
 4. How do you know whether a fraction can be represented as a repeating or terminating decimal? 5. How can we formulate, represent, and use algorithms with rational numbers flexibly, accurately, and efficiently? 6. Why is zero always the sum of a number 	 quantities combine to make zero. c. Demonstrate p + q as the number located a distance q from p, in the positive or negative direction depending on whether q is positive or negative. d. Show that a number and its opposite have a sum of zero (are additive inverses).
 and its opposite? 7. How can you represent addition and subtraction on a horizontal or vertical number line diagram? 8. How can you demonstrate p + q as the number located a distance <i>IqI</i> from p in the positive or posetive direction depending on 	e. Interpret sums of rational numbers by describing real-world contexts. f. Demonstrate subtraction of rational numbers as adding the additive inverse, p - q = p + (-q).
 positive or negative direction depending on whether it is positive or negative? 9. How can you demonstrate subtraction of rational numbers by adding the additive inverse? 10. How can you use long division to convert 	 g. Show that the distance between two rational numbers on the number line is the absolute value of their difference and apply this principle in real-world contexts. h. Apply properties of operations as strategies to add and subtract rational
a fraction to a decimal?	numbers.

	2. Apply and extend previous understandings of multiplication and division and of fractions to multiply and divide rational numbers including integers.
	a. Apply properties of operations to multiplication of rational numbers.
	b. Interpret products of rational numbers by describing real-world contexts.
	c. Apply properties of operations to divide integers.
	d. Apply properties of operations as strategies to multiply and divide rational numbers.
	e. Convert a rational number to a decimal using long division.
	f. Show that the decimal form of a rational number terminates in zeros or eventually repeats.
	3. Solve real-world and mathematical problems involving the four operations with rational numbers.
Academic Vocabulary:	Assessment:
	All assessments are found in the suggested
additive inverse	activities links, correlating with their
negative number	numbers, unless listed below.
number line diagram	
sum	1. Use the Elevator Arithmetic as assessment
rauonai number	2 & 3 Grade the worksheats as assessment
fraction	
integer	4. Create and grade worksheets
properties of operations	made using the worksheet maker link in
variables	Resources.
irrational numbers	
	5. Use the Zip, Zilch, Zero Game Assessment.
	6. There are multiple opportunities throughout the PowerPoint to assess students.

	7 & 8. Assessments are built into each lesson.
	1. Elevator Arithmetic Assessment
	5. Zip, Zilch, Zero Assessment
Suggested Activities/Strategies:	Resources/Technology:
For all activities listed below, the links are numbered to correlate with each activity. 1. Use the Elevator Arithmetic Lesson Plan where students will use the vertical movement	PARCC offers instructional and assessment support. Click on the tab "In the Classroom" and at the model frameworks for math.
of an elevator to evaluate signed number expressions.	tasks designed by the makers of the CCSS-M (Common Core State Standards of Mathematics.)
2. Demonstrate addition and subtraction on a number line.	Inside Mathematics has tasks, rubrics, and discussion questions that correlate with
3. Use Drill and Practice Worksheets for extra practice. Several would work for homework and/or extra classwork.	PARCC and Smarter Balance. <u>Math Arizona</u> has explanations and overviews for how the mathematics strands progress
4. Play the Zip, Zilch, Zero Game for adding and subtracting integers.	from one year to the next.
5. Use the Multiplication/Division of Integers PowerPoint to introduce how to multiply and divide integers.	Math Shell is Mathematics Assessment Resource Service (MARS) from the Shell Centre in Nottingham, England and it contains a number of performance tasks.
6. Go to <u>Smart Exchange</u> and choose from a variety of free lessons.	<u>Achieve the Core</u> is from Student Achievement Partners, a nonprofit organization that assembles educators and
7. Go to <u>Share My Lesson</u> and choose from several lessons over these standards.	researchers to design actions based in evidence that will substantially improve student achievement.
 <u>1. Elevator Arithmetic Lesson Plan</u> <u>2. Number Line Activity</u> <u>3. Drill and Practice Worksheet Website</u> 	Balanced Assessments is a site with free performance tasks to use in your classroom.
4. Zip, Zilch, Zero Game	
5. Integer PowerPoint	
6. Smart Exchange	Math Games
7. Share My Lesson	Math is Fun Integer Game
	Integers Worksheets

Integer Interactive Game
YouTube Video on Adding/Subtracting
Integers
YouTube Video on Changing Rational
Numbers to Decimals
Examples of Rational Numbers to Decimals
How to Convert Rational Numbers
Examples of Real World Problems
Real World Problems Video
Adding and Subtracting Integers

<u>7.Math.2.1</u> Properties of arithmetic can be used to generate equivalent expressions

<u>7. Wath.2.1</u> Properties of antimetic can be used to generate equivalent expressions		
Essential Questions - 21st Century Skills	Evidence Outcomes:	
and Readiness Competencies:		
	1. Use properties of operations to generate	
1 How do symbolic transformations affect an	equivalent expressions	
equation or expression?		
equation of expression.	a Apply properties of operations as	
2. How is it dotomained that two alcohoois	a. Apply properties of operations as	
2. How is it determined that two algebraic	strategies to add, subtract, factor, and	
expressions are equivalent?	expand linear expressions with rational	
	coefficients.	
3. How can the property of arithmetic be used		
to generate equivalent expressions?	b. Demonstrate that rewriting an	
	expression in different forms in a	
4 How can rewriting a problem in a different	problem context can shed light on the	
form help to understand a problem hetter?	problem and how the quantities in it are	
form help to understand a problem better?	related	
Academic Vocabulary:	Assessment:	
	All assessments are found in the suggested	
coefficients	activities links, correlating with their	
equivalent	numbers, unless listed below.	
factor		
linear expressions	1. Create and use worksheets for assessment.	
algebraic expressions		
associative property	2. The Calendar Fun Assessment is in the	
commutative property	Lesson Plan	
identity monorty		
distributive property	$3, 4, 5, \alpha$ 6. Assessments are located within	
	the different lessons.	
	<u>1. Worksheet Maker</u>	
	2. Calendar Fun	
Suggested Activities/Strategies:	Resources/Technology:	
For all activities listed below, the links are	PARCC offers instructional and assessment	
numbered to correlate with each activity	support Click on the tab "In the Classroom"	
	support. Click on the tab in the Classiooni	
	and at the model frameworks for math.	
1. Conduct Drill and Practice with worksheets.		
	<u>Illustrative Mathematics</u> contains examples	
2. Use the Calendar Fun Order of Operations	of tasks designed by the makers of the CCSS-	
Activity to help students evaluate numerical	M (Common Core State Standards of	
expressions by using order of operations.	Mathematics.)	
3 Go to Smart Exchange and choose from a	Inside Mathematics has tasks rubrics and	
variety of free lessons	discussion questions that correlate with	
	and a solution of the content of the	

4. Go to Share My Lesson and choose from a	PARCC and Smarter Balance.
 variety of lessons. 5. Use the Water Park Lesson Plan where students create a blueprint for a water park. 6. Use the Amazing Profit Lesson Plan. Students will use equations to determine eBay profit on new technology. 	Math Arizona has explanations and overviews for how the mathematics strands progress from one year to the next. Math Shell is Mathematics Assessment Resource Service (MARS) from the Shell Centre in Nottingham, England and it contains a number of performance tasks.
 Links to Multiple Worksheets Algebra Worksheets Calendar Fun Smart Exchange Share My Lesson Water Park Lesson Amazing Profit Lesson Plan 	Achieve the Core is from Student Achievement Partners, a nonprofit organization that assembles educators and researchers to design actions based in evidence that will substantially improve student achievement. Balanced Assessments is a site with free performance tasks to use in your classroom.
	Math GamesCombining Terms VideoApply Operations ResourcesYouTube Video on Expanding LinearEquationsYouTube Video #2 Combining Like TermsLinear Equation Graphic OrganizerInteractive Number Line GameInteractive Equation SolverOrder of Operations ToolOrder of Operations Tool with IntegersThink Pair Share Video ActivityMultiple ResourcesLinks for How to Rewrite Problems

<u>7.Math.2.2</u> Equations and expressions model quantitative relationships and phenomena

Essential Questions - 21st Century Skills and	Fyidence Outcomes:
Poodinoss Compotoncios:	Evidence Outcomes.
Readiness Competencies.	1. Solve multi-step real life and methometical
1. Do algebraic properties work with numbers or just symbols? Why?	rational numbers in any form, using tools strategically.
2. Why are there different ways to solve	
equations?	2. Apply properties of operations to calculate with numbers in any form, convert between
3. How are properties applied in other fields of study?	forms as appropriate, and assess the reasonableness of answers using mental computation and estimation strategies.
4. Why might estimation be better than an exact	
answer?	3. Use variables to represent quantities in a real-world or mathematical problem, and
5. When might an estimate be the only possible answer?	construct simple equations and inequalities to solve problems by reasoning about the quantities.
6. What is the difference between an algebraic	
solution and an authentic solution?	4. Fluently solve word problems leading to equations of the form $px + q = r$ and $p(x + q)$
7. How can you graph the solution set of an inequality?	= r , where p , q , and r are specific rational numbers.
8. When shopping for large ticket items (car, house, etc.) how would you determine interest, payments, etc.?	5. Compare an algebraic solution to an arithmetic solution, identifying the sequence of the operations used in each approach.
9. How could you solve a real life word problem using the $px + q = r$ format?	6. Solve word problems leading to inequalities of the form $px + q > r$ or $px + q < r$, where p , q , and r are specific rational numbers.
	7. Graph the solution set of the inequality and interpret it in the context of the problem.
Academic Vocabulary:	Assessment:
	All assessments are found in the suggested
positive numbers	activities links, correlating with their
negative numbers	numbers, unless listed below.
rational numbers	
estimate	1. Use link below for an Order of Operations
variable	Quiz.
inequalities	
equations	2. The Order of Operation Bingo has

symbol	assessments on the site. Use the Bingo sheets below as well.
	3. The BrainPop site has assessments. Create an assessment to follow the other two videos listed, if you do not have a subscription to BrainPop.
	4. In the Tic-Tac-Toe Game, assess as the students correctly solve the problems.
	5. In Skate Party, the single variable real world problems assessment is located within the lesson.
	6 & 7. Assessments are built into the lessons.
	1. Order of Operations Quiz
	2. Bingo Cards
	5. Skate Party Assessment
Suggested Activities/Strategies:	Resources/Technology:
For all activities listed below, the links are numbered to correlate with each activity. 1. Make your own Order of Operations	<u>PARCC</u> offers instructional and assessment support. Click on the tab "In the Classroom" and at the model frameworks for math.
 2. Play Order of Operations Bingo. Instead of calling numbers to play Bingo, call (and students write) expressions to be evaluated for 	Inustrative Mathematics contains examples of tasks designed by the makers of the CCSS- M (Common Core State Standards of Mathematics.)
the numbers on the Bingo cards.	Inside Mathematics has tasks, rubrics, and discussion questions that correlate with
Movie, but you must have a subscription. Or watch the Order Of Operations Video from the	Math Arizona has explanations and overviews for how the mathematics strands
mathplayground.com link below.	progress from one year to the next.
mathplayground.com link below. 4. Play the Tic-Tac-Toe Game as a new approach to working with variables and equations.	Math Shell_is Mathematics Assessment Resource Service (MARS) from the Shell Centre in Nottingham, England and it

6. On the Share My Lesson site, there are numerous multi-step word problem lessons from which to choose.7. Smart Exchange has several free lessons from which to choose.	Achieve the Core is from Student Achievement Partners, a nonprofit organization that assembles educators and researchers to design actions based in evidence that will substantially improve student achievement.
1 Create Your Own Worksheets	Balanced Assessments is a site with free performance tasks to use in your classroom.
<u>1. Make Your Own Worksheets</u>	
2. Order of Operations Bingo Lesson Plan <u>3. BrainPop Link</u> <u>3. Math Playground Video</u>	Site for Word Problems <u>Teacher Resource for Order of Operations</u> Fridge Formula Activity
 <u>3. Kahn Academy Order of Operations Video</u> <u>4. Tic-Tac-Toe Lesson Plan</u> <u>5. Skate Party Lesson</u> 	<u>Math Games</u> <u>YouTube Video on Solving Real World</u> Equations
<u>6. Share My Lesson</u> <u>7. Smart Exchange</u>	Multiple Links to Games Algebra to Arithmetic

<u>7.Math.3.1</u> Statistics can be used to gain information about populations by examining samples

<u>7.Wath.5.1</u> Statistics can be used to gain mornation about populations by examining samples				
Essential Questions - 21st Century Skills	Evidence Outcomes:			
and Readiness Competencies:				
1. How might the sample for a survey affect the results of the survey?	1. Use random sampling to draw inferences about a population.			
2. How do you distinguish between random and biased samples?	2. Explain that generalizations about a population from a sample are valid only if the sample is representative of that population.			
3. How can you declare a winner in an election before counting all the ballots?	3. Explain that random sampling tends to produce representative samples and support valid inferences.			
4. How can statistics be used to gain information?5. How can random campling produce	4. Use data from a random sample to draw inferences about a population with an unknown abaracteristic of interest			
representative samples and support valid inferences?	5. Generate multiple samples (or simulated samples) of the same size to gauge the			
6. How do visuals help you to understand the mathematical differences in representations of two populations?	variation in estimates or predictions. 6. Draw informal comparative inferences about			
7 What is the difference hot week measure of	two populations.			
center and measure of variability for numerical data?	7. Informally assess the degree of visual overlap of two numerical data distributions with similar variabilities, measuring the difference between the centers by expressing it as a multiple of a measure of variability.			
	8. Use measures of center and measures of variability for numerical data from random samples to draw informal comparative inferences about two populations.			
Academic Vocabulary:	Assessment: All assessments are found in the suggested			
inference	activities links, correlating with their			
	numbers, unless listed below.			
generalization				
sampling				
data				
sample				

 Evaluate whether each student's bar graphs are properly constructed and properly display the survey responses. Ask students to write a paragraph discussing their findings and describing how this new information should be incorporated into community planning. Determine that the measurements are accurate and the map is to scale. 4, & 5. Questions in the lesson will be answered orally or in writing.
6 & 7. Assessments are built into each lesson.
Resources/Technology:
Resources/Technology:PARCC offers instructional and assessmentsupport. Click on the tab "In the Classroom"and at the model frameworks for math.Illustrative Mathematics contains examples oftasks designed by the makers of the CCSS-M(Common Core State Standards ofMathematics has tasks, rubrics, anddiscussion questions that correlate withPARCC and Smarter Balance.Math Arizonahas explanations and overviewsfor how the mathematics strands progress fromone year to the next.Math Shellis Mathematics AssessmentResource Service (MARS) from the ShellCentre in Nottingham, England and itcontains a number of performance tasks.Achieve the Coreis from StudentAchieve the Coreis from Student

5. Use the Population Sampling Lab Activity. To get a better understanding of the community of organisms living within an ecosystem, ecologists take random samples to gain a representation of what relationships exist in a certain area.	Balanced Assessments is a site with free performance tasks to use in your classroom.
 6. There are a variety of free lessons to choose from at <u>Smart Exchange</u>. 7. The <u>Share My Lesson</u> site has multiple 21st Century lessons. 	<u>Math Games</u> <u>Measure of Center Worksheet</u> <u>Measure of Center PowerPoint</u>
 <u>1. Community Survey Activity</u> <u>2. School Survey Activity</u> <u>3. Population Sampling Activity</u> <u>4. Backpack Activity</u> <u>5. Population Sampling Lab Activity</u> <u>6. Smart Exchange</u> <u>7. Share My Lesson</u> 	

<u>7.Math.3.2</u> Mathematical models are used to determine probability

Essential Questions - 21st Century Skills and Readiness Competencies:	Evidence Outcomes:		
1. Why is it important to consider all of the possible outcomes of an event?	a. Explain that the probability of a chance event is a number between 0 and 1 that expresses the likelihood of the event occurring.		
 Is it possible to predict the future? How? What are some situations in which probability cannot be used? How can you determine probability using mathematical models? 	b. Approximate the probability of a chance event by collecting data on the chance process that produces it and observing its long-run relative frequency, and predict the approximate relative frequency given the probability		
5. What is the probability of a chance event?	c. Develop a probability model and use it to find probabilities of events.		
 6. How can you use a probability model to help find the probability of an event? 7. How can organized lists, tables, tree diagrams, and simulations help find the probabilities of compound events? 	d. Compare probabilities from a model to observed frequencies; if the agreement is not good, explain possible sources of the discrepancy.		
probabilities of compound events?8. What are compound events?	e. Develop a uniform probability model by assigning equal probability to all outcomes, and use the model to determine probabilities of events.		
	f. Develop a probability model (which may not be uniform) by observing frequencies in data generated from a chance process.		
	g. Find probabilities of compound events using organized lists, tables, tree diagrams, and simulation.		
	h. Explain that the probability of a compound event is the fraction of outcomes in the sample space for which the compound event occurs.		
	i. Represent sample spaces for compound events using methods such as organized lists, tables and tree diagrams.		

	j. For an event described in everyday language identify the outcomes in the sample space which compose the event.				
	K. Design and use a simulation to generate frequencies for compound events.				
Academic Vocabulary: compound event probability relative frequency model discrepancy outcome sample spaces simulation	 Assessment: All assessments are found in the suggested activities links, correlating with their numbers, unless listed below. 1. Some games have assessments included. 2. Use the online probability quiz (CRCT). 3 Students will write a paragraph on 				
	 probability after experimenting with the virtual roll of the die program. A rubric is included for grading paragraphs. 4. Use the online probability quiz (Bitesize). 5 & 6. Assessments are located within each lesson. 2. Online Probability Quiz (CRCT) 3. Paragraph Rubric 4. Online Probability Quiz (Bitesize) 				
Suggested Activities/Strategies:	Resources/Technology:				
For all activities listed below, the links are numbered to correlate with each activity. 1. Play the Probability Games. To make	<u>PARCC</u> offers instructional and assessment support. Click on the tab "In the Classroom" and at the model frameworks for math.				
lessons on probability more amusing, figure out ways to relate probability projects to familiar games with which children can identify.	<u>Illustrative Mathematics</u> contains examples of tasks designed by the makers of the CCSS-M (Common Core State Standards of Mathematics.)				
2. Watch the Compound Events Video. In this lesson, students learn how to find the probability of compound events by watching an online video, taking an online quiz, and playing a fun online game.	Inside Mathematics has tasks, rubrics, and discussion questions that correlate with PARCC and Smarter Balance.				

3. Experiment with a virtual roll of the die. In	Math Arizona has explanations and overviews
this interactive, there is a strong explanation of	for how the mathematics strands progress
how probability works under the graph.	from one year to the next.
4. Play a probability game on Bitesize.	Math Shell is Mathematics Assessment
5 If and a function of the Airlinean of the	Resource Service (MARS) from the Shell
5. If you have a Smart Board of Alriner, go to	Centre in Nottingnam, England and it
Smart Exchange and choose from variety of	contains a number of performance tasks.
lessons on probability.	Achieve the Core is from Student
6. Go to Share My Lesson and choose from a	Achievement Partners, a nonprofit
variety of probability lessons	organization that assembles educators and
variety of probability lessons.	researchers to design actions based in
	evidence that will substantially improve
	student achievement.
1. Probability Games (Multiple Examples)	
2 Compound Probability of Events Video	Balanced Assessments is a site with free
3 Experiment with the Boll of a Die	performance tasks to use in your classroom.
Interactive	
4. Bitesize Probability Game	
5. Smart Exchange	Math Games
6. Share My Lesson	Probability Games
	Probability PowerPoint
	Probability Tree Diagram Handout
	YouTube Video on Compound Probability
	Multiple Games
	YouTube Video on Developing Probability
	Models
	Multiple Interactive Links

<u>7.Math.4.1</u> Modeling geometric figures and relationships leads to informal spatial reasoning and proof

und proof	
Essential Questions - 21st Century Skills and Readiness Competencies:	Evidence Outcomes:
 Is there a geometric figure for any given set of attributes? 	a. Draw, construct, and describe geometrical figures and describe the relationships between them.
2. How does scale factor affect length, perimeter, angle measure, area, and volume?3. How do you know when a proportional relationship exists?	b. Solve problems involving scale drawings of geometric figures, including computing actual lengths and areas from a scale drawing and reproducing a scale drawing at a different scale.
4. How can you describe two-dimensional figures that result from slicing three-dimensional figures?	c. Draw (freehand, with ruler and protractor, and with technology) geometric shapes with given conditions.
5. How can you construct triangles from three measures of angles or sides?6. What does drawing to scale mean?	d. Construct triangles from three measures of angles or sides, noticing when the conditions determine a unique triangle, more than one triangle, or no triangle.
7. What type of conditions determine a unique triangle, more than one triangle, or no triangle based on measurements?	e. Describe the two-dimensional figures that result from slicing three-dimensional figures, as in plane sections of right rectangular prisms and right rectangular pyramids.
Academic Vocabulary: plane section attributes geometrical figures scale drawings protractor rectangular prisms rectangular pyramids	 Assessment: All assessments are found in the suggested activities links, correlating with their numbers, unless listed below. 1. Polygon Activity interactive rubric for poster 2. Cross Sections of 3D Shapes worksheet
	 Teacher assessment throughout lesson
	4. Drawing Your Body to scale is the assessment
	5. Triangle assessment
	6. The students will be assessed based on the

	accuracy of answers given on the lesson attachment.
	 <u>1. Polygon Poster Rubric</u> <u>2. Cross Sections of 3-D Shapes Worksheet</u> <u>4. Drawing Your Body to Scale Rubric</u> <u>5. Investigating Triangles</u> <u>6. Triangle Assessment</u>
Suggested Activities/Strategies:	Resources/Technology:
For all activities listed below, the links are numbered to correlate with each activity. 1. In the Polygon Activity, the student will be able to create a poster comprised of at least	PARCC offers instructional and assessment support. Click on the tab "In the Classroom" and at the model frameworks for math. <u>Illustrative Mathematics</u> contains examples of
 Use the Cross Sections of 3D Shapes Lesson for developing the concepts of cross- sections of three-dimensional models and to demonstrate the derivation of two-dimensional shapes 	tasks designed by the makers of the CCSS-M (Common Core State Standards of Mathematics.) Inside Mathematics has tasks, rubrics, and discussion questions that correlate with PARCC and Smarter Balance
3. Use Play-Doh Activity to teach volume.Uses Play-Doh to create 3D shapes to measure figures and to find the volume.	Math Arizona has explanations and overviews for how the mathematics strands progress from one year to the next.
4. Use the Body to Scale Lesson Plan. Students use scale factors to draw their bodies to scale.5. The Investigating Triangles Activity is for recognizing and understanding the properties.	Math Shell is Mathematics Assessment Resource Service (MARS) from the Shell Centre in Nottingham, England and it contains a number of performance tasks.
 of triangles and their positions in space. 6. Use the Constructing Triangles Lesson Plan. The purpose of this lesson is to help students investigate the relationships of the lengths of the sides of a triangle in order to discover the three triangle inequality theorems. 	Achieve the Core is from Student Achievement Partners, a nonprofit organization that assembles educators and researchers to design actions based in evidence that will substantially improve student achievement. Balanced Assessments is a site with free performance tasks to use in your classroom.

1. Polygon Activity	Math Games
2. Cross Sections of 3-D Shapes	Geometric Patterns
3. Play-Doh Activity	Drawing Geometric Shapes Video
4. Drawing Your Body to Scale	Visualizing Geometry Video
5. Investigating Triangles	Drawing Triangles with a Compass and
6. Constructing Triangles Lesson Plan	Straight Edge Animation
	Scale Drawing
	Drawing to Scale Lessons
	Interactive Triangles Site
	Constructing Triangles Site

7.Math.4.2 Li	inear measure,	angle measure,	area,	and volume	are funda	mentally	different	and
require differe	ent units of mea	asure						

Essential Questions - 21st Century Skills	Evidence Outcomes:			
and Readiness Competencies:				
1. How can geometric relationships among lines and angles be generalized, described, and quantified?	a. State the formulas for the area and circumference of a circle and use them to solve problems.			
2. How do line relationships affect angle relationships?	b. Give an informal derivation of the relationship between the circumference and area of a circle.			
3. Can two shapes have the same volume but different surface areas? Why?	c. Use properties of supplementary, complementary, vertical, and adjacent angles			
4. Can two shapes have the same surface area but different volumes? Why?	in a multi-step problem to write and solve simple equations for an unknown angle in a figure.			
5. Compare and Contrast Surface Area and Volume.	d. Solve real-world and mathematical problems involving area, volume and surface			
6. What do surface area and volume tell about an object?	composed of triangles, quadrilaterals, polygons, cubes, and right prisms.			
7. How are one-, two-, and three-dimensional units of measure related?				
8. Why is pi an important number?				
Academic Vocabulary:	Assessment:			
area circumference derivation	All assessments are found in the suggested activities links, correlating with their numbers, unless listed below.			
supplementary angles complementary angles	1. In an "A" Peeling Problem, the assessment is in the lesson (pp. 6-7).			
adjacent angles	2. Online circle and angle tools have "Exploration" questions above them that may be used as assessment and discussion.			
	3. In the Getting "A-Round" Area Teacher Notes, answers to the Student Activity could be used as the assessment			
	4. Nifty Nets Rubric for assessment			

	5. Interactive online assessment of 3D shapes			
	6. Assessment throughout lesson			
	7. Ping Pong Rubric			
	8. Teacher observation as the assessment			
Suggested Activities/Strategies:	3. Getting "A-Round" Area Teacher Notes 4. Nifty Nets Rubric 5. Interactive 3-D Shapes 7. Ping Pong Rubric			
Suggested Activities/Strategies.	Resources/reclinology.			
For all activities listed below, the links are numbered to correlate with each activity.	<u>PARCC</u> offers instructional and assessment support. Click on the tab "In the Classroom" and at the model frameworks for math.			
1. An "A" Peeling Problem Lesson covers the area of circles and spheres.	<u>Illustrative Mathematics</u> contains examples of tasks designed by the makers of the CCSS-M			
2. Use online tools to explore circles and angles.	(Common Core State Standards of Mathematics.)			
3. Getting "A-Round" Area contains a useful animation for teaching the area of a circle. Student activity sheet is included.	<u>Inside Mathematics</u> has tasks, rubrics, and discussion questions that correlate with PARCC and Smarter Balance.			
4. Nifty Nets is a lesson on the volume and surface area of prisms.	Math Arizona has explanations and overviews for how the mathematics strands progress from one year to the next.			
5. Interactive 3D shapes contains both online and print and fold options.	Math Shell is Mathematics Assessment			
6. Use the Play-Doh Activity to explore volume.	Centre in Nottingham, England and it contains a number of performance tasks.			
7. Use the Ping Pong Madness to teach volume.	<u>Achieve the Core</u> is from Student Achievement Partners, a nonprofit			
8. Play 3D Shapes Dominoes.	organization that assembles educators and researchers to design actions based in evidence that will substantially improve student achievement.			

9. Smart Exchange has multiple lessons to	Balanced Assessments is a site with free
choose from if you have a SmartBoard or	performance tasks to use in your classroom.
Airliner.	
10. Share My Lesson has multiple lessons from which to choose.	Math Games Net Worksheets Net PowerPoint
	3-D Shapes PowerPoint
1. An A-Peeling Problem	Mini-Surface Area Unit
2. Angle Tool	whin-Surface Area Onit
2. Circle Tool	
3. Getting "A-Round" Area Student Activity	
3. Getting "A-Round" Area Animation and	
Lesson	
4. Nifty Nets	
4. Nifty Nets Project Guide	
5. Interactive 3-D Shapes	
6. Play-Doh Activity to Teach Volume	
7. Ping Pong Packages	
8. Nets Dominoes	
9. Smart Exchange	
10. Share My Lesson	