

# 6-3 Study Guide and Intervention

## Square Root Functions and Inequalities

**Square Root Functions** A function that contains the square root of a variable expression is a **square root function**. The domain of a square root function is those values for which the radicand is greater than or equal to 0.

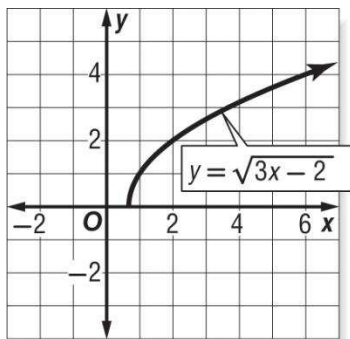
**Example:** Graph  $y = \sqrt{3x - 2}$ . State its domain and range.

Since the radicand cannot be negative, the domain of the function is  $3x - 2 \geq 0$  or  $x \geq \frac{2}{3}$ .

The  $x$ -intercept is  $\frac{2}{3}$ . The range is  $y \geq 0$ .

Make a table of values and graph the function.

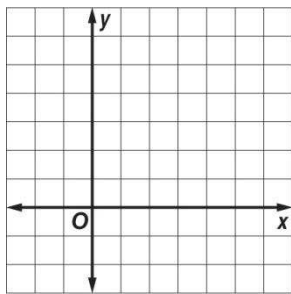
$x$	$y$
$\frac{2}{3}$	0
1	1
2	2
3	$\sqrt{7}$



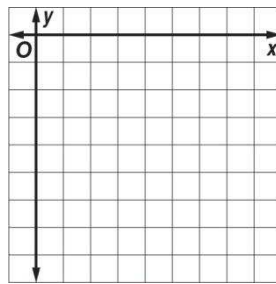
### Exercises

Graph each function. State the domain and range.

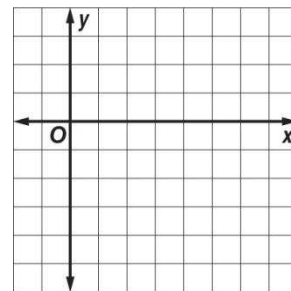
1.  $y = \sqrt{2x}$



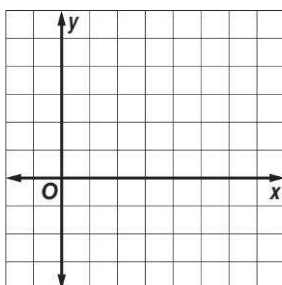
2.  $y = -3\sqrt{x}$



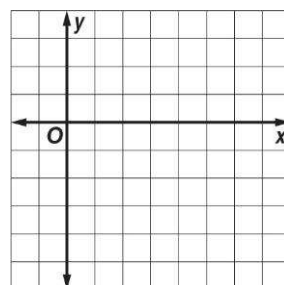
3.  $y = -\sqrt{\frac{x}{2}}$



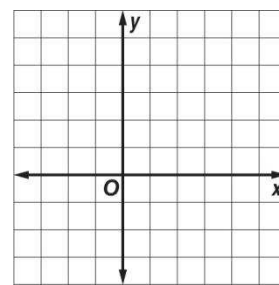
4.  $y = 2\sqrt{x - 3}$



5.  $y = -\sqrt{2x - 3}$



6.  $y = \sqrt{2x + 5}$



# 6-3 Study Guide and Intervention *(continued)*

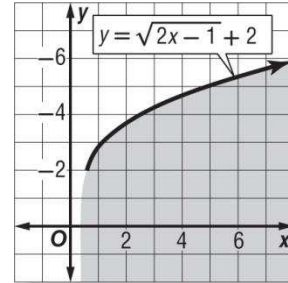
## Square Root Functions and Inequalities

**Square Root Inequalities** A square root inequality is an inequality that contains the square root of a variable expression. Use what you know about graphing square root functions and graphing inequalities to graph square root inequalities.

**Example:** Graph  $y \leq \sqrt{2x - 1} + 2$ .

Graph the related equation  $y = \sqrt{2x - 1} + 2$ . Since the boundary should be included, the graph should be solid.

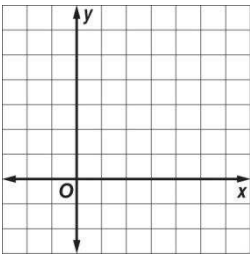
The domain includes values for  $x \geq \frac{1}{2}$ , so the graph is to the right of  $x = \frac{1}{2}$ .



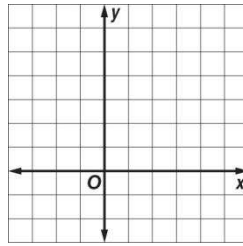
### Exercises

Graph each inequality.

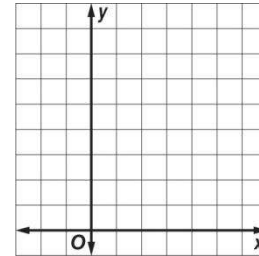
1.  $y < 2\sqrt{x}$



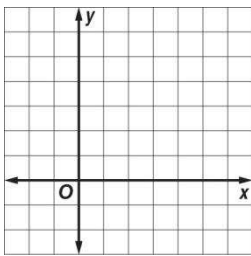
2.  $y > \sqrt{x + 3}$



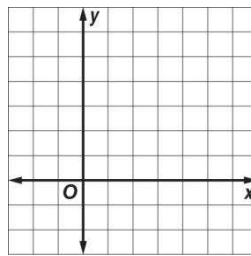
3.  $y < 3\sqrt{2x - 1}$



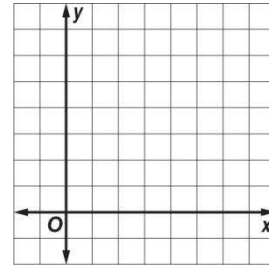
4.  $y < \sqrt{3x - 4}$



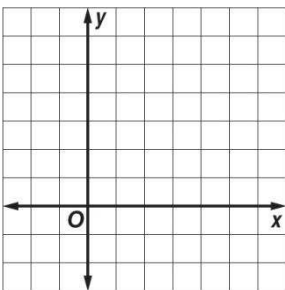
5.  $y \geq \sqrt{x + 1} - 4$



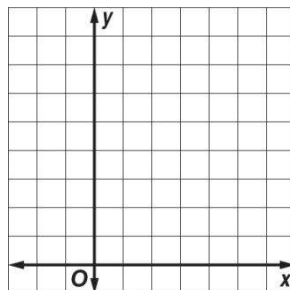
6.  $y > 2\sqrt{2x - 3}$



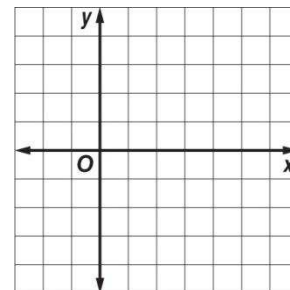
7.  $y \geq \sqrt{3x + 1} - 2$



8.  $y \leq \sqrt{4x - 2} + 1$



9.  $y < 2\sqrt{2x - 1} - 4$

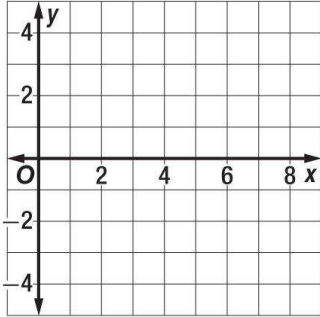


# 6-3 Skills Practice

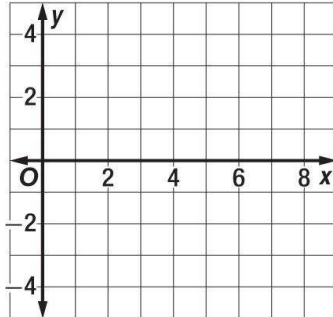
## Square Root Functions and Inequalities

Graph each function. State the domain and range of each function.

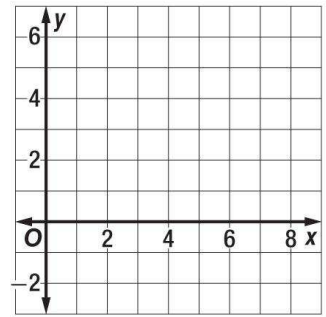
1.  $y = \sqrt{2x}$



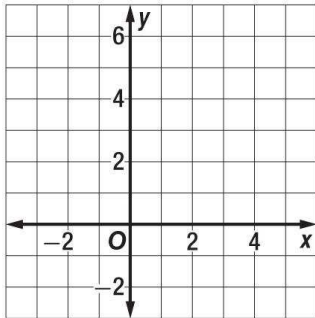
2.  $y = -\sqrt{3x}$



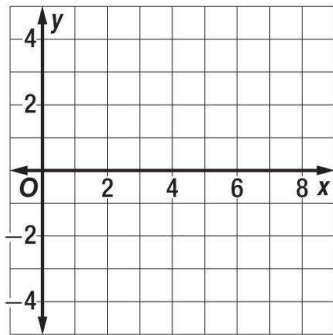
3.  $y = 2\sqrt{x}$



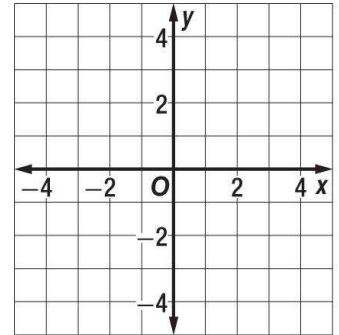
4.  $y = \sqrt{x + 3}$



5.  $y = -\sqrt{2x - 5}$

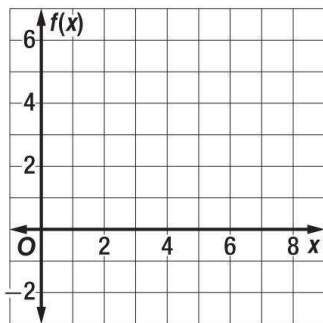


6.  $y = \sqrt{x + 4} - 2$

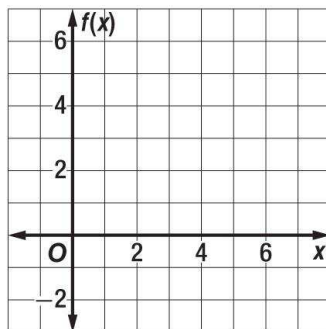


Graph each inequality.

7.  $f(x) < \sqrt{4x}$



8.  $f(x) \geq \sqrt{x + 1}$



9.  $f(x) \leq \sqrt{4x - 3}$

