

Production and Cost in the Long Run

Learning Objectives

After reading Chapter 9 and working the problems for Chapter 9 in the textbook and in this Workbook, you should be able to:

- Draw a graph of a typical production isoquant and use the definition of an isoquant to explain why isoquants must be downward sloping.
- Discuss the properties of an isoquant.
- Construct isocost curves for a given level of expenditure on inputs.
- Apply the theory of optimization to find the optimal input combination.
- Show graphically that the conditions for minimizing the total cost of producing a given level of output are the same conditions for maximizing the level of output for a given level of total cost.
- Construct an expansion path.
- Construct a long-run total cost curve from an expansion path.
- Define economies of scale and diseconomies of scale.
- Discuss the various reasons for economies and diseconomies of scale.
- Describe the nature of constant costs.
- Define and explain the importance of minimum efficient scale (MES).
- Define and explain economies of scope using the concept of a multiproduct total cost function.
- Discuss the various reasons for economies of scope.
- Explain how purchasing economies of scale arise and how they impact long-run average costs.
- Define learning or scale economies and discuss the effect of learning on long-run average costs.
- Show the relation between long-run and short-run cost curves.
- Distinguish between long-run and short-run expansion paths.
- Explain why costs are generally lower in the long run than in the short run.

Essential Concepts

1. In long-run analysis of production, all inputs are variable and isoquants are used to study production decisions. An *isoquant* is a curve showing all possible input combinations capable of producing a given level of output.
2. Isoquants are downward sloping because if greater amounts of labor are used, then less capital is required to produce a given level of output. The *marginal rate of technical substitution (MRTS)* is the slope of an isoquant and measures the rate at which the two inputs can be substituted for one another while maintaining a constant level of output

$$MRTS = -\frac{\Delta K}{\Delta L}$$

The minus sign is added in order to make *MRTS* a positive number since $\Delta K / \Delta L$, the slope of the isoquant, is negative.

3. The marginal rate of technical substitution can be expressed as the ratio of two marginal products:

$$MRTS = \frac{MP_L}{MP_K}$$

As labor is substituted for capital, MP_L declines and MP_K rises causing *MRTS* to diminish.

4. *Isocost curves* show the various combinations of inputs that may be purchased for a given level of expenditure (\bar{C}) at given input prices (w and r). The equation of an isocost curve is given by

$$K = \frac{\bar{C}}{r} - \frac{w}{r}L$$

The slope of an isocost curve is the negative of the input price ratio ($-w/r$). The K -intercept is \bar{C}/r , which represents the amount of capital that may be purchased when all \bar{C} dollars are spent on capital (i.e., zero labor is purchased).

5. A manager can minimize the total cost of producing \bar{Q} units of output by choosing the input combination on the isoquant for \bar{Q} which is just tangent to an isocost curve. Since the optimal input combination occurs at the point of tangency between the isoquant and an isocost curve, the two slopes are equal in equilibrium. Mathematically, the equilibrium condition may be expressed as

$$\frac{MP_L}{MP_K} = \frac{w}{r} \quad \text{or} \quad \frac{MP_L}{w} = \frac{MP_K}{r}$$

6. In order to maximize output for a given level of expenditure on inputs, a manager must choose the combination of inputs that equates the marginal rate of technical substitution and the input price ratio, which requires choosing an input combination satisfying exactly the same conditions set forth above for minimizing cost.

7. The *expansion path* is the curve that gives the efficient (least-cost) input combinations for every level of output. The expansion path is derived for a specific set of input prices. Along an expansion path, the input-price ratio is constant and equal to the marginal rate of technical substitution.

8. Long-run total cost (LTC) for a given level of output \bar{Q} is given by

$$LTC = wL^* + rK^*$$

where w and r are the prices of labor and capital, respectively, and L^* and K^* is the input combination on the expansion path that minimizes the total cost of producing \bar{Q} units of output.

9. Long-run average cost (LAC) measures the cost per unit of output when the manager can adjust production so that the optimal amount of each input is employed: $LAC = LTC/Q$. LAC is U-shaped.

10. Long-run marginal cost (LMC) measures the rate of change in long-run total cost as output changes along the expansion path: $LMC = \Delta LTC/\Delta Q$. LMC is U-shaped. LMC lies below (above) LAC when LAC is falling (rising). LMC equals LAC at LAC 's minimum value.

11. When LAC is decreasing (increasing), (*dis*)*economies of scale* are present. See Figure 9.11 in your textbook.

12. The most fundamental reason for economies of scale is that larger-scale firms are able to take greater advantage of opportunities for specialization and division of labor. A second cause of scale economies arises when quasi-fixed costs are spread over more units of output causing LAC to fall. And a variety of technological factors can also contribute to falling LAC .

13. When a firm experiences neither economies nor diseconomies of scale, it faces *constant costs* in the long run and its LAC curve is flat and equal to LMC at all output levels.

14. The *minimum efficient scale* of operation (MES) is the lowest level of output needed to reach the minimum value of long-run average cost.

15. When economies of scope exist: (1) The total cost of producing goods X and Y by a multiproduct firm is less than the sum of the costs for specialized, single-product firms to produce these goods: $LTC(X,Y) < LTC(X,0) + LTC(0,Y)$, and (2) Firms already producing good X can add production of good Y at lower cost than a single-product firm can produce Y : $LTC(X,Y) - LTC(X,0) < LTC(0,Y)$. Economies of scope arise when firms produce joint products or when firms employ common inputs in production.

16. *Purchasing economies of scale* arise when large-scale purchasing of raw materials enables large buyers to obtain lower input prices through quantity discounts.

17. Workers, managers, engineers, and even input suppliers in these industries “learn by doing” or “learn through experience.” As total *cumulative* output increases, *learning or experience economies* cause long-run average cost to fall at every output level.

18. The relations between long-run cost and short-run cost can be summarized by the following points:

a. LMC intersects LAC when the latter is at its minimum point.

- b. At each output where a particular *ATC* is tangent to *LAC*, the relevant *SMC* equals *LMC*.
 - c. For all *ATC* curves, the point of tangency with *LAC* is at an output less (greater) than the output of minimum *ATC* if the tangency is at an output less (greater) than that associated with minimum *LAC*.
19. Because managers have the greatest flexibility to choose inputs in the long run, costs are lower in the long run than in the short run for all output levels except the output level for which the fixed input is at its optimal level. Thus, the firm's short-run costs can generally be reduced by adjusting the fixed inputs to their optimal long-run levels when the long-run opportunity to adjust fixed inputs arises.
20. Since the long-run cost structure shows the lowest-possible costs a firm can achieve, business decision makers and industry analysts are keenly interested in long-run costs.

Matching Definitions

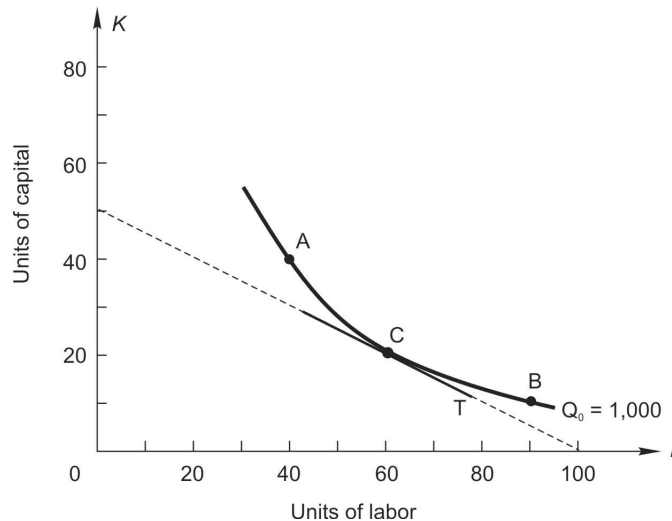
common or shared inputs	learning or experience economies
constant costs	long-run average cost
diseconomies of scale	long-run marginal cost
economies of scale	marginal rate of technical substitution
economies of scope	minimum efficient scale (MES)
expansion path	multiproduct total cost function
isocost curve	purchasing economies of scale
isoquant	short-run expansion path
joint products	specialization and division of labor

1. _____ A curve that displays all the various combinations of inputs that will produce a given amount of output.
2. _____ The rate at which one input is substituted for another along an isoquant.
3. _____ Line that shows all the possible combinations of inputs that can be purchased for a given total cost.
4. _____ A curve showing all of the cost-minimizing levels of input usage for various levels of output.
5. _____ The most fundamental reason for economies of scale
6. _____ Lowest production level that will minimize long-run average cost.
7. _____ Gives the minimum total cost of producing various combinations of good *X* and good *Y*.
8. _____ Cost per unit in the long run.
9. _____ The change in long-run total cost per unit change in output.
10. _____ When long-run average cost falls as output increases.
11. _____ When long-run average cost increases with increases in output.

12. _____ Long-run average and marginal costs are equal for all levels of output.
13. _____ The situation in which the joint cost of producing two goods is less than the sum of the separate costs of producing the two goods.
14. _____ Horizontal line showing the cost-minimizing input combinations for various output levels when capital is fixed in the short run.
15. _____ When the production of one good causes one or more other good to be produced as by-products at zero marginal cost.
16. _____ Large-scale input buyers get lower input prices due to quantity discounts.
17. _____ Cumulative increases in output cause long-run average cost to shift downward.
18. _____ Inputs that contribute to production of several goods or services.

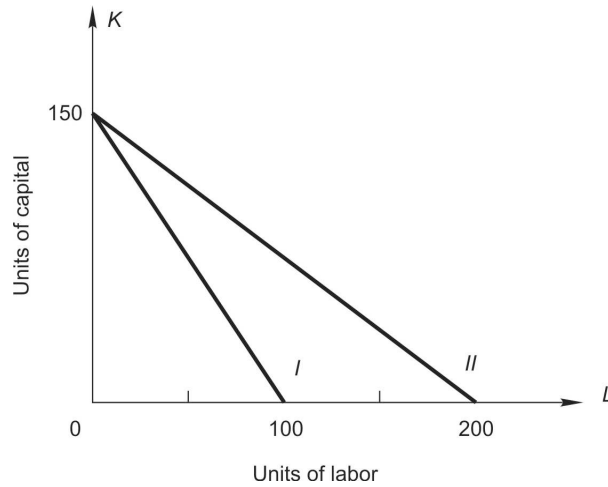
Study Problems

1. In the following figure, isoquant Q_0 is the isoquant for 1,000 units of output.

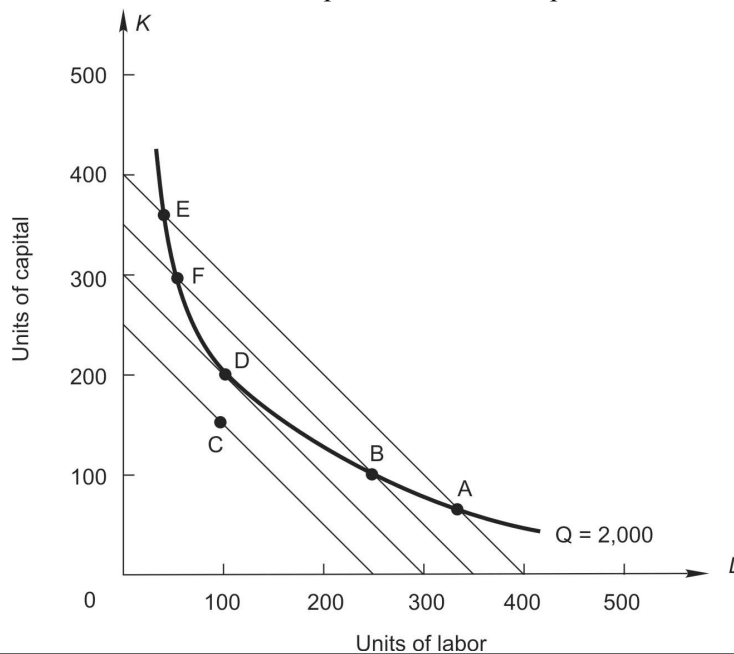


- a. Marginal rate of technical substitution between points A and C is _____.
- b. Marginal rate of technical substitution between points C and B is _____.
- c. Marginal rate of technical substitution at point C is _____.

2. The following graph shows two isocost curves. The price of capital is \$100.

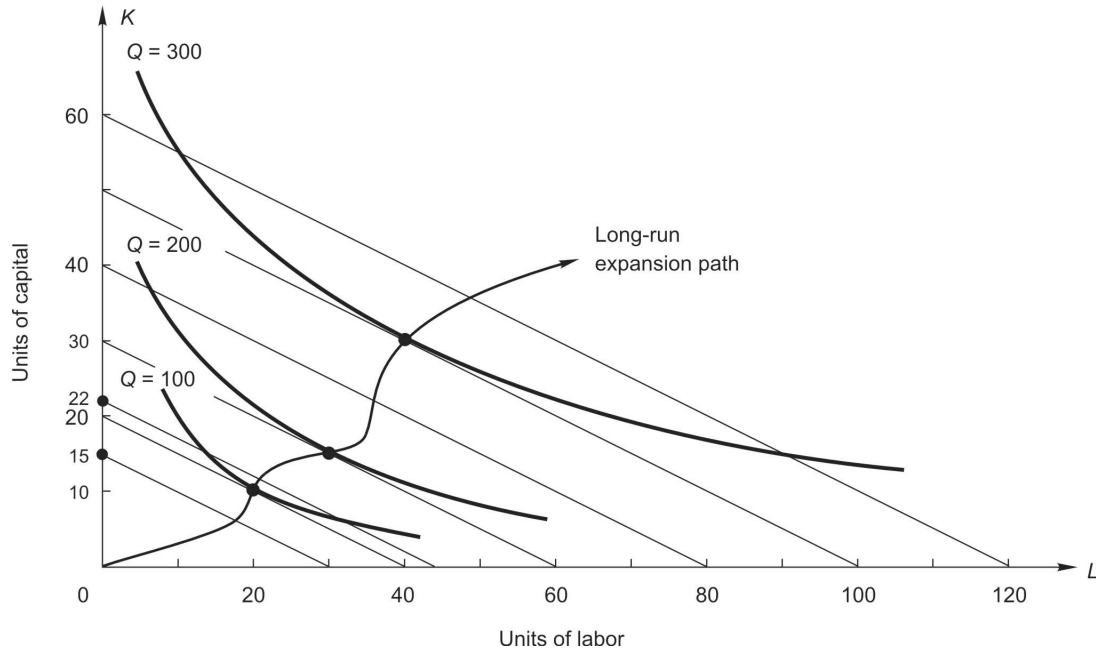


- The total cost associated with isocost *I* is \$_____, and the price of labor is \$_____.
 - The equation for isocost *I* is _____. With isocost *I* the firm must give up _____ units of capital to purchase one more unit of labor in the market.
 - The total cost associated with isocost *II* is \$_____, and the price of labor is \$_____.
 - The equation for isocost *II* is _____. With isocost *II* the firm must give up _____ units of capital to purchase one more unit of labor in the market.
3. The following figure shows a firm's isoquant for producing 2,000 units of output and four isocost curves. Labor and capital each cost \$50 per unit.



- a. At point *A*, the *MRTS* is _____ (less than, greater than, equal to) the input price ratio, w/r . The total cost of producing 2,000 units of output with input combination *A* is \$ _____.
 - b. By moving from *A* to *B*, the firm _____ (increases, decreases) labor usage and _____ (increases, decreases) capital usage. At point *B* the *MRTS* is _____ (greater than, less than, equal to) the input price ratio, w/r . The movement from *A* to *B* _____ (increased, decreased) total cost by \$ _____.
 - c. At Point *D* the firm _____ (minimizes, maximizes) the cost of producing 2,000 units of output. The *MRTS* is _____ (greater than, less than, equal to) the input price ratio, w/r .
 - d. The optimal input combination is _____ units of labor and _____ units of capital. At this combination, the total cost of producing 2,000 units is \$ _____.
 - e. At point *E*, the *MP* per dollar spent on _____ is less than the *MP* per dollar spent on _____. The total cost of producing 2,000 units of output with input combination *E* is \$ _____.
 - f. The movement from *E* to *F* reduces the *MP* per dollar spent on _____ and increases the *MP* per dollar spent on _____. This movement _____ (increased, decreased) total cost by \$ _____.
 - g. At input combination *D*, the *MP* per dollar spent on labor is _____ (greater than, less than, equal to) the *MP* per dollar spent on capital.
 - h. Input combination *C* costs \$ _____. The firm would not use this combination to produce 2,000 units of output because _____.
4. Your firm produces clay pots entirely by hand even though a pottery machine exists that can make clay pots faster than a human. Workers cost \$100 per day and each additional worker can produce 20 more pots per day (i.e., marginal product is constant and equal to 20). Installation of the first pottery machine would increase output by 300 pots per day. Currently your firm produces 1,200 pots per day.
- a. Your financial analysis department estimates that the price of a pottery machine is \$2,000 per day. Can you reduce the cost of producing 1,200 pots per day by adding a pottery machine to your production process and reducing the amount of labor? Explain why or why not.
 - b. If a labor union negotiates higher wages so that labor costs rise to \$150 per day, does this change your answer to part *a*? Explain.
 - c. Suppose your firm wants to expand output to 2,500 pots per day and input prices are \$100 and \$2,000 per day for labor and capital, respectively. Is it efficient to hire more labor or more capital? Explain using the ratio of marginal products and input prices.

5. The figure below shows a portion of the expansion path for a firm. The price of labor is \$75.



- The price of capital is \$ _____. Along the expansion path, the marginal rate of technical substitution is equal to _____.
- To produce 100 units in the long run, a manager would use _____ units of labor and _____ units of capital. The long-run total cost of producing 100 units is \$ _____.
- To produce 200 units in the long run, a manager would use _____ units of labor and _____ units of capital. The long-run total cost of producing 200 units is \$ _____.
- To produce 300 units in the long run, a manager would use _____ units of labor and _____ units of capital. The long-run total cost of producing 300 units is \$ _____.
- The firm currently operates with 15 units of capital equipment. In the figure above, construct the firm's short-run expansion path and label it "Short-run expansion path."
- To produce 100 units in the short run, a manager would use _____ units of labor and _____ units of capital. The short-run total cost of producing 100 units is \$ _____, which is _____ (more than, less than, the same as) the long-run total cost of producing 100 units.
- To produce 200 units in the short run, a manager would use _____ units of labor and _____ units of capital. The short-run total cost of producing 200 units is \$ _____, which is _____ (more than, less than, the same as) the long-run total cost of producing 200 units.
- To produce 300 units in the short run, a manager would use _____ units of labor and _____ units of capital. The short-run total cost of producing 300 units is \$ _____, which is _____ (more than, less than, the same as) the long-run total cost of producing 300 units.

- i. If the firm is producing 100 units in the short run, it can restructure its production in the long-run and reduce its costs of producing 100 units by \$_____.
 - j. If the firm is producing 300 units in the short run, it can restructure its production in the long-run and reduce its costs of producing 300 units by \$_____.
 - k. Only when the firm wishes to produce _____ units in the short run will the manager be unable to restructure production in the long run and reduce costs. Explain.
6. Explain carefully each of the following characteristics of an expansion path:
- a. Along an expansion path, the input price ratio is constant.
 - b. Along an expansion path, the marginal rate of technical substitution is constant.
 - c. An increase in the price of one input always causes a shift in the expansion path.
 - d. An equiproportionate increase in the price of both labor and capital does not shift the expansion path.
7. You are a management consultant hired by the Rio Loco Vineyards to estimate the costs of raising grapes in an arid region of New Mexico. If labor costs \$6,000 per man-year and capital costs \$200 per unit annually, you determine that the least-cost input combinations for various levels of grape production are:

<i>Output</i> <i>(bushels/year)</i>	<i>Labor</i> <i>(man-years)</i>	<i>Capital</i> <i>(units/year)</i>
100,000	30	100
200,000	51	270
300,000	56	420
400,000	60	600
500,000	62	640
600,000	84	1,080

- a. Complete the table below:

<i>Output</i>	<i>LTC</i>	<i>LAC</i>	<i>LMC</i>
100,000	\$_____	\$_____	xx
200,000	_____	_____	\$_____
300,000	_____	_____	_____
400,000	_____	_____	_____
500,000	_____	_____	_____
600,000	_____	_____	_____

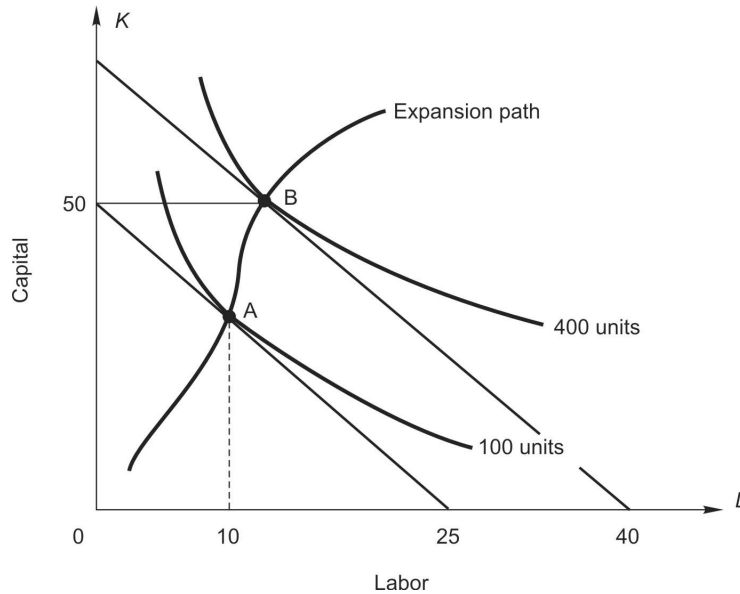
- b. Over what range of output do economies of scale exist in the production of grapes?
- c. Over what range of output do diseconomies of scale exist in the production of grapes?
8. Small, local artisan jewelry makers in the American Southwest design, manufacture, and sell silver rings (R) and bracelets (B) to tourists. The multiproduct total costs for various combinations of rings and bracelets (measured in units per month) is given in the table below:

R	B	$LTC(R, B)$
50	0	\$ 5,000
75	0	11,250
0	80	25,600
0	100	40,000
50	80	28,600
75	100	47,500
50	100	42,500
75	80	33,850

- a. If a silver jeweler specializes in ring production, does the firm experience economies of scale in ring production over the range of 50 to 75 rings per month? Explain.
- b. If a silver jeweler specializes in bracelet production, does the firm experience economies of scale in bracelet production over the range of 80 to 100 rings per month? Explain.
- c. Suppose tourists demand 50 rings and 80 bracelets per month. At this level of ring and bracelet production, are there economies of scope in ring and bracelet production. Why or why not?
- d. If a jeweler is currently producing 50 rings and 100 bracelets, what is the jeweler's marginal cost of increasing ring production to 75 rings? Does this indicate the presence of scope economies? Explain carefully.

Multiple Choice / True-False

For questions 1–5, consider the expansion path illustrated below. The price of capital is \$2.



1. What is the price of labor?
 - a. \$1
 - b. \$2
 - c. \$2.50
 - d. \$3.00
 - e. \$4

2. The efficient amount of capital for producing 100 units of output is
 - a. 10 units of capital.
 - b. 20 units of capital.
 - c. 30 units of capital.
 - d. 40 units of capital.

3. The marginal rate of technical substitution at point B is _____.
 - a. 0.5
 - b. 0.25
 - c. 1
 - d. 2
 - e. 4

4. The average cost of producing 400 units is
 - a. \$1.
 - b. \$0.10.
 - c. \$4.
 - d. \$0.40.
 - e. \$0.50.

5. The efficient amount of labor for producing 400 units of output is
 - a. 5.
 - b. 10.
 - c. 15.
 - d. 25.
 - e. 50.

6. A U-shaped long-run average cost (*LAC*) curve represents
 - a. increasing returns and diminishing returns.
 - b. fixed costs and variable costs.
 - c. economies and diseconomies of scale.
 - d. average fixed costs and average variable costs.

7. At any output at which *ATC* is tangent to *LAC*,
 - a. $LMC = SMC$.
 - b. economies of scale must be present.
 - c. long-run total cost (*LTC*) equals short-run total cost (*TC*).
 - d. both *a* and *c*.
 - e. all of the above.

Questions 8–11 refer to the following:

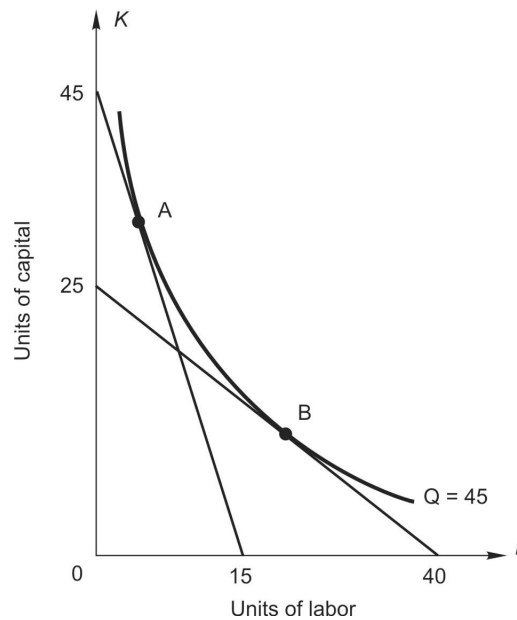
The price of labor is \$20 per unit and the price of capital is \$40 per unit.

<i>Output</i>	<i>Optimal input combination</i>		<i>LTC</i>	<i>LAC</i>	<i>LMC</i>
	<i>L*</i>	<i>K*</i>			
10	20	8	\$_____	\$_____	xx
20	_____	12	_____	_____	\$24
30	32	_____	_____	48	_____
40	50	_____	2,040	_____	_____

8. When output is 10 units, what is long-run average cost?
 - a. \$24
 - b. \$48
 - c. \$60
 - d. \$72

9. When output is 20 units, how many units of labor will the firm use?
- 22
 - 24
 - 30
 - 50
10. How much does the 30th unit add to long-run total cost?
- \$24
 - \$48
 - \$60
 - \$72
11. When output is 40 units, how many units of capital will the firm use?
- 22
 - 24
 - 26
 - 30

The next three questions refer to the following:



12. What is the marginal rate of technical substitution at point *A*?
- 0.3
 - 1
 - 1.125
 - 1.67
 - none of the above

13. As you move from point A to point B ,
- output is unchanged.
 - cost is unchanged.
 - the rate at which the firm can substitute labor for capital while holding output constant decreases.
 - both a and b .
 - both a and c .
14. If the firm continues to produce 45 units of output and moves from the combination at A to the combination at B , it must be true that
- the price of labor decreased relative to the price of capital.
 - the price of capital decreased relative to the price of labor.
 - the cost of producing 45 units decreased.
 - both b and c .
 - none of these are true.
15. A sofa manufacturer currently is using 50 workers and 30 machines to produce 5,000 sofas a day. The wage rate is \$200 and the rental rate for a machine is \$1,000. At these input levels, another worker adds 200 sofas, while another machine adds 500 sofas. If the firm uses 45 workers and 31 machines instead,
- then its cost will be unchanged, and its output will decrease by 500 units.
 - then its cost will be unchanged, and its output will increase by 300 units.
 - then its cost will be unchanged, and its output will increase by 500 units.
 - then its output will be unchanged, and its cost will decrease by \$800.
 - none of the above.
16. Economies of scope in the production of goods R and B exist if
- $LTC(R, B) < LTC(R, 0) + LTC(0, B)$
 - $LTC(R, B) > LTC(R, 0) - LTC(0, B)$
 - $LTC(R, B) - LTC(R, 0) < LTC(0, B)$
 - both a and c
 - both b and c
17. If there are no fixed costs in the long run, how can it be said that economies of scale arise from spreading fixed costs over more units of output?
- Economies of scale is a short run phenomenon, and so diminishing returns is the root cause of scale economies.
 - It is the cost of quasi-fixed inputs that gets spread over more units of output and drives down average cost in the long run.
 - Average fixed costs decline continuously as output rises.
 - Long-run average cost falls because all fixed costs are sunk.

18. Learning economies differ from economies of scale because
- the former involves rising average costs and the latter involves falling average costs as a result of higher output levels.
 - the former involves *cumulative* production and the latter involves *rate* of production per period.
 - the former involves output in a single period of production and the latter involves cumulative output.
 - the first is a short-run phenomenon and the second is a long-run phenomenon.
19. Economies of SCALE can arise because
- the cost of purchasing and installing larger machines is usually proportionately LESS than for smaller machines.
 - there is usually a qualitative change in the type of capital equipment employed as the scale of operation increases.
 - common or shared resources can be employed as the scale of operation increases, up to the point of minimum efficient scale (MES).
 - Both *a* and *b*
 - All of the above
20. Many businesses treat their costs as if they are constant, even though their costs are NOT actually constant. As a result of this simplifying assumption,
- managers can safely ignore the law of diminishing marginal product.
 - managers will treat long-run marginal and average costs as constant and equal, which simplifies cost analysis considerably.
 - Managerial decision making will not be adversely affected if long-run fixed costs are avoidable.
 - all of the above
21. When economies of scope are strong,
- large-scale, single-product firms will be able to reach minimum efficient scale (MES) more quickly.
 - multiproduct firms will enjoy a cost advantage because they have the opportunity to divide their pool of workers into small groups that will specialize in the production of one particular product.
 - new firms entering the market are likely to be multiproduct firms.
 - new firm entering the market are likely to be single-product firms.
22. T F An increase in input prices causes a downward shift in each isoquant.
23. T F The expansion path gives the input combinations that minimize the average cost of producing various levels of output.
24. T F The efficient input combination is the one that maximizes output and minimizes total cost.
25. T F Economies of scale occur when input prices fall as output rises.

Answers

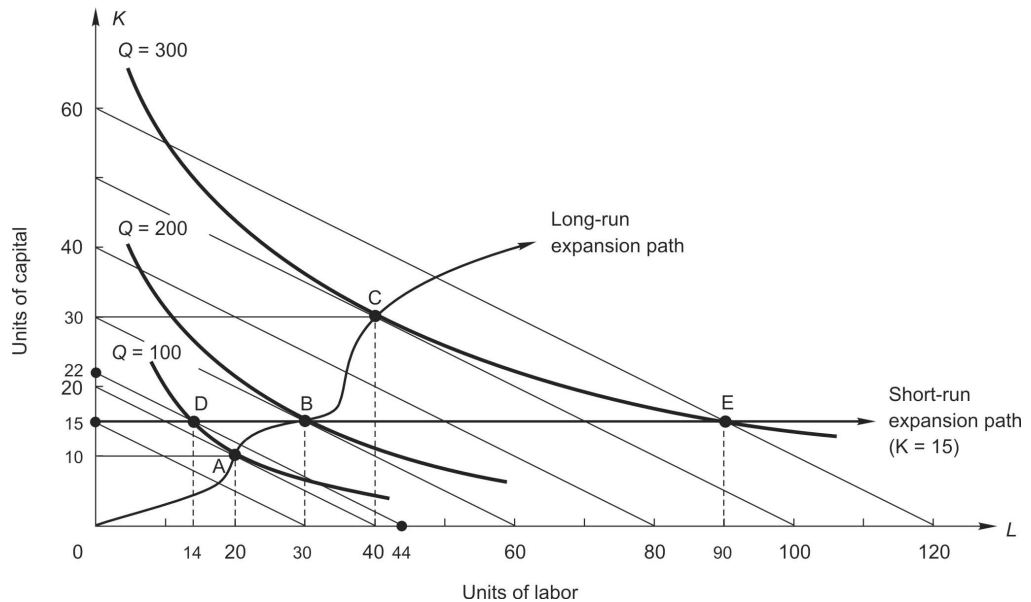
MATCHING DEFINITIONS

1. isoquant
2. marginal rate of technical substitution
3. isocost curve
4. expansion path
5. specialization and division of labor
6. minimum efficient scale (MES)
7. multiproduct total cost function
8. long-run average cost
9. long-run marginal cost
10. economies of scale
11. diseconomies of scale
12. constant costs
13. economies of scope
14. short-run expansion path
15. joint products
16. purchasing economies of scale
17. learning or experience economies
18. common or shared inputs

STUDY PROBLEMS

1.
 - a. $1 (= -\frac{20-40}{60-40})$, which is the slope over the interval from *A* to *C*.
 - b. $0.33 (= -\frac{10-20}{90-60})$, which is the slope over the interval from *C* to *B*.
 - c. $0.5 (= -\frac{-50}{100})$, which is the slope of the tangent line at point *C*.
2.
 - a. 15,000; 150. The *K*-intercept is 150, so the isocost curve represents a cost of \$15,000 ($= 150 \times \100). The *L*-intercept is 100, so $w = \$150 (= 15,000/100)$.
 - b. $K = 150 - 1.5L$ (or $K = 150 - (150/100)L$ or $15,000 = 150L + 100K$); 1.5
 - c. 15,000; \$75. The price of labor decreases and causes an outward rotation of the isocost curve.
 - d. $K = 150 - 0.75L$ (or $K = 150 - (150/200)L$ or $15,000 = 75L + 100K$); 0.75
3.
 - a. less than; \$20,000 ($= \50×400)
 - b. decreases; increases; less than; decreased; \$2,500 [$= (400-350) \times \50]. [Note: For the last part of this answer, you must decide visually that the isocost curve passing through point *B* intersects the *L* or *K*-intercepts at 350. Do not panic, your instructor knows this.]
 - c. minimizes; equal
 - d. 100; 200; \$15,000 ($= 300 \times \50)
 - e. capital; labor; \$20,000
 - f. labor; capital; decreased; \$2,500 (see answer to part *b* above)
 - g. equal to
 - h. \$12,500 ($= 250 \times \50); this combination lies below the 2,000 unit isoquant and so 2,000 units cannot be produced with combination *C*.

4. a. By purchasing one pottery machine, which would increase output by 300 units, 15 laborers could be fired and output would remain exactly equal to 1,200 units per day. This reduces the cost of labor by $15 \times \$100 = \$1,500$. The cost of capital increases by \$2,000. Clearly, substituting the machine for an equally productive amount of labor (i.e., the 15 workers) increases the total cost of producing 1,200 clay pots per day.
- b. Yes, at \$150 per worker, the reduction in wage expense is now $15 \times 150 = \$2,250$, which is more than the cost of the machine (\$2,000 per day). Thus, the higher wages make buying a machine efficient.
- c. $MP_L/w = 20/100 = 0.2$ additional pots per additional dollar spent on labor
 $MP_K/r = 300/2,000 = 0.15$ additional pots per extra dollar spent on capital
 Since each additional dollar spent on labor increases output by more than an additional dollar spent on capital, it is less costly to expand output by hiring more labor than by buying pottery machines.
5. a. The price of capital is \$150. You can discover this by noting in the figure that the slope of the isocost curves is $1/2$. Since the slope of isocost curves equals w/r and you are told that $r = \$150$, you can see that $75/r = 1/2$ and thus $r = 150$. At every tangency point along the (long-run) expansion path, the slope of the isoquant equals the slope of the isocost line. Since the isocost lines are always parallel, their slopes are constant along the expansion path and equal to $MRTS$, which must be $1/2$ in this case.



- b. 20; 10; \$3,000. At point A in the figure above, you can see that the tangency occurs at 20 units of labor and 10 units of capital, which costs \$3,000 ($= \150×20 or $\$75 \times 20 + 150 \times 10$).
- c. 30; 15; \$4,500. At point B in the figure above, you can see that the tangency occurs at 30 units of labor and 15 units of capital, which costs \$4,500 ($= \150×30 or $\$75 \times 30 + 150 \times 15$).
- d. 40; 30; \$7,500. At point C in the figure above, you can see that the tangency occurs at 40 units of labor and 30 units of capital, which costs \$7,500 ($= \150×50 or $\$75 \times 40 + 150 \times 30$).
- e. The short-run expansion path is a horizontal line at 15 units of capital, which is

designated in the figure above as “Short-run expansion path.”

- f. 14; 15; \$3,300; more than. At point *D* in the figure above, you can see that the 100-unit isoquant is reached with 15 units of capital by employing 14 units of labor at a cost of \$3,300 ($= \150×22 or $\$75 \times 14 + 150 \times 15$), which is more than the long-run cost of \$3,000.
- g. 30; 15; \$4,500; the same as. At point *B* in the figure above, you can see that the 200-unit isoquant is reached with 15 units of capital by employing 30 units of labor, which costs \$4,500 ($= \150×30 or $\$75 \times 30 + 150 \times 15$), which is the same as the long-run cost of \$4,500.
- h. 90; 15; \$9,000; more than. At point *E* in the figure, you can see that the 300-unit isoquant is reached with 15 units of capital by employing 90 units of labor at a cost of \$9,000 ($= \150×60 or $\$75 \times 90 + 150 \times 15$), which is more than the long-run cost of \$7,500.
- i. \$300; This is the difference between the short-run and long-run total costs of producing 100 units ($= \$3,300 - \$3,000$).
- j. \$1,500; This is the difference between the short-run and long-run total costs of producing 300 units ($= \$9,000 - \$7,500$).
- k. 200; When 200 units are produced in the short-run, the fixed amount of capital (15 units) happens also to be the long-run optimal level of capital, so the costs are equal in the long-run and short-run for 200 units of output.
6. a. An expansion path is derived for a given set of input prices. Thus the input price ratio is constant for every point on an expansion path.
- b. The expansion path is a locus of efficient input combinations for each level of output. The efficient input combinations satisfy the condition that $MRTS =$ the input price ratio. Since the input price ratio is constant for all Q along an expansion path, then $MRTS$ must also be constant.
- c. An increase in one input price must alter the input price ratio. Thus a different set of input combinations becomes efficient at every level of output, and the expansion path shifts.
- d. An equiproportional increase (or decrease) in input prices leaves the input price ratio unchanged. The same capital-labor combination is efficient for every output level.
7. a. Your table should look like this:

Q	LTC	LAC	LMC
100,000	\$200,000	\$2.00	xx
200,000	360,000	1.80	\$1.60
300,000	420,000	1.40	0.60
400,000	480,000	1.20	0.60
500,000	500,000	1.00	0.20
600,000	720,000	1.20	2.20

- b. Economies of scale occur over the output range 100,000 to 500,000 bushels/year.
- c. Diseconomies of scale set in at outputs greater than 500,000 bushels/year.
8. a. No, there are diseconomies of SCALE over the range 50 to 75 rings:
 $LAC(50,0) = LTC(50,0)/50 = \$5,000/50 = \$100$ per ring

$$LAC(75,0) = LTC(75,0)/75 = \$11,250/75 = \$150 \text{ per ring}$$

∴ diseconomies of SCALE exist in ring production over this range of R since LAC rises as ring production increases.

- b. No, there are diseconomies of SCALE over the range 80 to 100 bracelets:

$$LAC(0,80) = LTC(0,80)/80 = \$25,600/80 = \$320 \text{ per bracelet}$$

$$LAC(0,100) = LTC(0,100)/100 = \$40,000/100 = \$400 \text{ per bracelet}$$

∴ diseconomies of SCALE exist in ring production over this range of B since LAC rises as bracelet production increases.

- c. Apply the definition of scope economies to find:

$$LTC(50,0) + LTC(0,80) > LTC(50,80)$$

$$5,000 + 25,600 = \$31,600 > \$28,600 \rightarrow \text{economies of SCOPE}$$

- d. In this part of problem 8, you will be applying alternative definition of scope economies: Firms already producing good X can add production of good Y at lower cost than a single-product firm can produce Y :

The marginal cost of adding 80 bracelets when a firm is already making 50 rings is \$23,600 [= $LTC(50,80) - LTC(50,0) = \$28,600 - \$5,000$].

Since a single-product jeweler producing only 80 bracelets incurs total costs of \$25,600 [= $LTC(0,80)$], it is less costly for a multiproduct jeweler to produce 80 bracelets. ∴ economies of SCOPE exist here.

MULTIPLE CHOICE / TRUE-FALSE

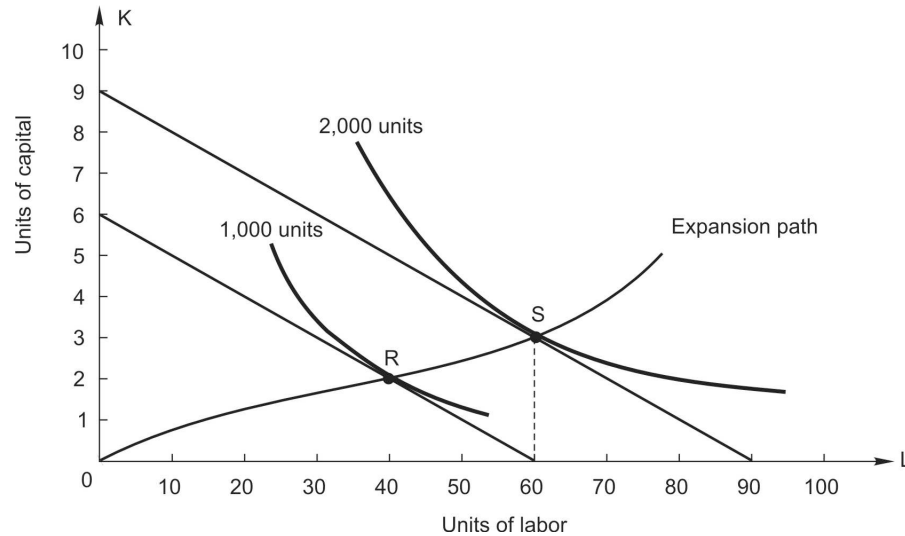
1. e From the figure, the isocost curves can be seen to have a slope of 2. Since r is given to be \$2, $w/2 = 2 \Rightarrow w = \4 .
2. c Input combination A costs \$100 (= $\$4 \times 25$ or $\$2 \times 50$). Since input combination A has 10 units of labor, which cost \$40 to buy, \$60 remains to be spent on capital. Thus, 30 (= $\$60/\2) units of capital are used to produce 100 units of output.
3. d At every point on the expansion path, $MRTS$ = the slope of the isocost curve. Since the isocost curves have a slope equal to 2, $MRTS$ must also equal 2.
4. d Total cost of 400 units is \$160 (= $\$4 \times 40$), so average cost is $\$160/400 = \0.40 .
5. c \$100 is being spent on 50 units of capital, leaving \$60 to purchase labor. Since $w = \$4$, 15 units of labor can be purchased (input bundle B).
6. c When LAC falls, economies of scale exist. If LAC rises, diseconomies of scale exist.
7. d When $ATC = LAC$ at a given Q , LTC must equal TC . It is also true that $LMC = SMC$ at the point of tangency between LAC and ATC .
8. d $LAC_{10} = \$720/10 = \72
9. b Since $MC = 24$ for each of the ten extra units (10 units to 20 units), total cost must rise by \$240 (= $\$24 \times 10$). Thus $TC_{Q=20}$ must equal $TC_{Q=10} + \$240$ or $\$720 + \$240 = \$960$. Once 12 units of capital are purchased by the firm, \$480 of the \$960 has been spent on capital, leaving \$480 to spend on labor. Thus the amount of labor is $\$480/\$20 = 24$ units of labor.
10. b $LMC = \Delta LTC/\Delta Q = (1,440 - 960)/(30 - 20) = \48 . Each of the units in the interval

20 – 30 cost (on average) an additional \$48 to produce. Thus, the 30th unit adds \$48 to total cost.

11. c 50 units of labor and 26 units of capital cost \$2,040.
12. e $MRTS$ at point $A = 45/15 = 3$.
13. e Moving from point A to B leaves output unchanged and decreases $MRTS$.
14. a To induce managers to move from A to B , labor must become cheaper relative to capital. Note that the slope of the isocost curve ($= w/r$) is smaller at B than at A .
15. a 45 workers and 31 machines cost the same as 50 workers and 30 machines. Even though cost is the same, output falls since MP_L/w exceeds MP_K/r .
16. d Both a and d are true when there are economies of scope in production of goods R and B .
17. b Technically speaking, it is incorrect to say that economies of scale result from spreading fixed costs. The only kind of fixed cost that could be spread over more output in the long run is quasi-fixed cost, because there are no fixed costs in the long-run production period.
18. b Learning or experience economies arise as cumulative production rises, while economies of scale arise as the firm's production rate (e.g., output per day, month, or year) increases.
19. d Both a and b are correct, while choice c is simply a mixture of unrelated terms.
20. b Assuming costs are constant may be factually incorrect, but it substantially simplifies cost analysis because $LAC = LMC$ for all output levels. This assumption may not adversely affect decision making IF long-run average and marginal costs are very nearly equal at most output levels.
21. c Because scope economies confer a cost advantage on multiproduct firms, new entrants are likely to be multiproduct firms. Single-product firms, facing a cost disadvantage will be more likely to exit the industry or face merger/acquisition attempts.
22. F Isoquants do not shift with changes in input prices. Isocost curves do rotate if the relative input price ratio changes, and isocost curves shift parallel if cost changes.
23. F The expansion path is the locus of input combinations that minimize total (not average) cost.
24. F This statement is meaningless. The manager can either minimize total cost for a given output or maximize output for a given total cost.
25. F Input prices are assumed to be constant along the LAC curve.

Homework Exercises

1. Answer the following questions using the expansion path illustrated below. The price of labor is \$4 per unit.

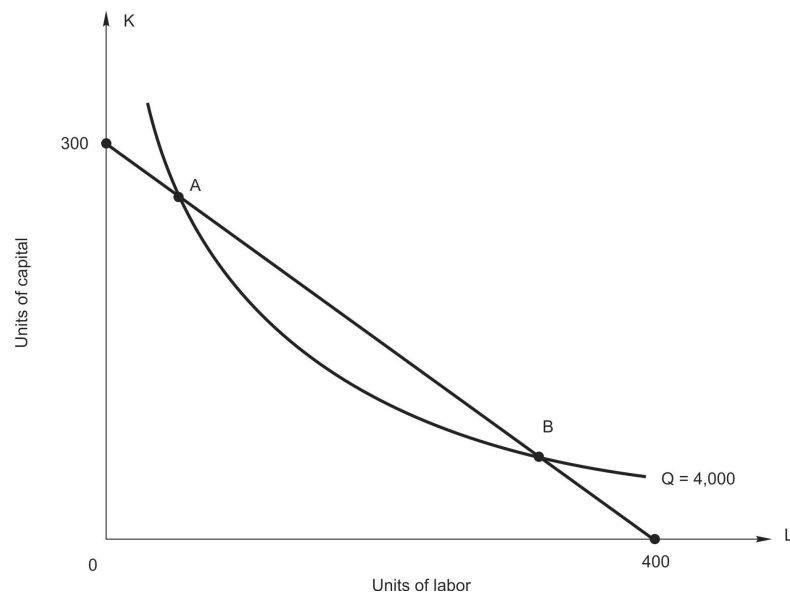


- The price of capital is \$_____.
- In the long run, 1,000 units of output is produced at the lowest possible total cost by employing _____ units of labor.
- The marginal rate of technical substitution at point *S* is _____.
- When producing 2,000 units in the long run, the marginal product of the 60th unit of labor (MP_L) is 5. The marginal product of capital (MP_K) must equal _____.
- The equation of the isocost curve passing through point *R* is

$$K = \underline{\hspace{2cm}}$$
- In the long run, 2,000 units of output is produced at the lowest possible total cost by employing _____ units of capital.
- Is input combination *R* technically efficient? Explain.
- Is input combination *R* economically efficient? Explain.

- i. Over the range of output from 1,000 units to 2,000 units, does the firm experience economies or diseconomies of scale? Explain.
- j. Construct the short-run expansion path when capital is fixed at 2 units.
- k. In the short run with capital fixed at 2 units, 2,000 units can be produced by employing _____ units of labor. The short-run total cost of producing 2,000 units is \$ _____. By restructuring its costs in the long run, the firm can _____ (reduce, increase) its total cost of producing 2,000 by \$ _____.

2. The following graph shows one of a firm's isocost curves and isoquants:



- a. Combination *A* is not an economically efficient method of producing 4,000 units of output because, at *A*, _____ exceeds _____ or in other words, _____ exceeds _____. The firm should increase _____ and decrease _____.
- b. Combination *B* is not an economically efficient method of producing 4,000 units of output because, at *B*, _____ exceeds _____, or in other words, _____ exceeds _____. The firm should increase _____ and decrease _____.
- c. At the economically efficient method of producing 4,000 units of output the *MRTS* will equal _____.