

7-6 Skills Practice

Common Logarithms

Use a calculator to evaluate each expression to the nearest ten-thousandth.

1. $\log 6$

2. $\log 15$

3. $\log 1.1$

4. $\log 0.3$

Solve each equation or inequality. Round to the nearest ten-thousandth.

5. $3^x > 243$

6. $16^v \leq \frac{1}{4}$

7. $8^p = 50$

8. $7^y = 15$

9. $5^{3b} = 106$

10. $4^{5k} = 37$

11. $12^{7p} = 120$

12. $9^{2m} = 27$

13. $3^{r-5} = 4.1$

14. $8^{y+4} > 15$

15. $7.6^{d+3} = 57.2$

16. $0.5^{t-8} = 16.3$

17. $42^{x^2} = 84$

18. $5^{x^2+1} = 10$

Express each logarithm in terms of common logarithms. Then approximate its value to the nearest ten-thousandth.

19. $\log_3 7$

20. $\log_5 66$

21. $\log_2 35$

22. $\log_6 10$

23. Use the formula $\text{pH} = -\log [H^+]$ to find the pH of each substance given its concentration of hydrogen ions. Round to the nearest tenth.

a. gastric juices: $[H^+] = 1.0 \times 10^{-1}$ mole per liter

b. tomato juice: $[H^+] = 7.94 \times 10^{-5}$ mole per liter

c. blood: $[H^+] = 3.98 \times 10^{-8}$ mole per liter

d. toothpaste: $[H^+] = 1.26 \times 10^{-10}$ mole per liter

7-6 Practice

Common Logarithms

Use a calculator to evaluate each expression to the nearest ten-thousandth.

1. $\log 101$

2. $\log 2.2$

3. $\log 0.05$

Use the formula $\text{pH} = -\log [H^+]$ to find the pH of each substance given its concentration of hydrogen ions. Round to the nearest tenth.

4. milk: $[H^+] = 2.51 \times 10^{-7}$ mole per liter

5. acid rain: $[H^+] = 2.51 \times 10^{-6}$ mole per liter

6. black coffee: $[H^+] = 1.0 \times 10^{-5}$ mole per liter

7. milk of magnesia: $[H^+] = 3.16 \times 10^{-11}$ mole per liter

Solve each equation or inequality. Round to the nearest ten-thousandth.

8. $2^x < 25$

9. $5^a = 120$

10. $6^z = 45.6$

11. $9^m \geq 100$

12. $3.5^x = 47.9$

13. $8.2^y = 64.5$

14. $2^{b+1} \leq 7.31$

15. $4^{2x} = 27$

16. $2^{a-4} = 82.1$

17. $9^z - 2 > 38$

18. $5^{w+3} = 17$

19. $30^{x^2} = 50$

20. $5^{x^2-3} = 72$

21. $4^{2x} = 9^{x+1}$

22. $2^{n+1} = 5^{2n-1}$

Express each logarithm in terms of common logarithms. Then approximate its value to the nearest ten-thousandth.

23. $\log_5 12$

24. $\log_8 32$

25. $\log_{11} 9$

26. $\log_2 18$

27. $\log_9 6$

28. $\log_7 \sqrt{8}$

29. HORTICULTURE Siberian irises flourish when the concentration of hydrogen ions $[H^+]$ in the soil is not less than 1.58×10^{-8} mole per liter. What is the pH of the soil in which these irises will flourish?

30. ACIDITY The pH of vinegar is 2.9 and the pH of milk is 6.6. Approximately how many times greater is the hydrogen ion concentration of vinegar than of milk?

31. BIOLOGY There are initially 1000 bacteria in a culture. The number of bacteria doubles each hour. The number of bacteria N present after t hours is $N = 1000(2)^t$. How long will it take the culture to increase to 50,000 bacteria?

32. SOUND An equation for loudness L in decibels is given by $L = 10 \log R$, where R is the sound's relative intensity. An air-raid siren can reach 150 decibels and jet engine noise can reach 120 decibels. How many times greater is the relative intensity of the air-raid siren than that of the jet engine noise?