Angles and the Unit Circle

Lesson 13-2

Lesson Objectives W Working with angles in standard position Local Standards: Finding coordinates of points on the unit circle

Vocabulary and Key Concepts

Cosine and Sine of an Angle Suppose an angle in standard position has measure θ .
The cosine of θ (cos θ) is the -coordinate of the point -1 $1x$
at which the terminal side of the angle intersects the unit circle. The sine of θ -1 , $(\sin \theta)$ is the -coordinate.
An angle is in standard position when Position Position
The initial side of the angle is side x side
The terminal side of the angle is side
Two angles in standard position are coterminal angles if Angles that have measures -225° x Angles that have measures 135° and -225° are
The unit circle is a circle that $circle = unit unit $

.

.

.

Examples

History The Aztec calendar stone has 20 divisions for the 20 days in each month of the Aztec year. An angle on the Aztec calendar shows the passage of 16 days. Find the measures of the two coterminal angles that coincide with the angle. The terminal side of the angle is of a full rotation from the initial side. $^{\circ} =$ To find a coterminal angle, subtract one full rotation. |° = Two coterminal angle measures for an angle on the Aztec calendar that shows ° and the passage of 16 days are **2** Finding Exact Values of Cosine and Sine Find the exact values of $\cos(-150^{\circ})$ and $\sin(-150^{\circ})$. **Step 1** Sketch an angle of -150° in standard position. Sketch a unit circle. x-coordinate = $\cos(-150^{\circ})$ y-coordinate = $\sin(-150^{\circ})$ **Step 2** Sketch a right triangle. Place the hypotenuse on the terminal side of the angle. Place one leg on the *x*-axis. P(x, y)(The other leg will be parallel to the y-axis.) The triangle contains angles of °. and **Step 3** Find the length of each side of the triangle. The hypotenuse is a hypotenuse =of the unit circle. The shorter leg is shorter leg =the hypotenuse. The longer leg is longer leg =times the shorter leg. Since the point lies in Quadrant both coordinates are The leg lies

x

 -150°

256

along the x-axis, so $\cos(-150^\circ) =$

and $\sin(-150^\circ) =$

Quick Check

- **1. a.** Find an angle coterminal with 198° by adding one full rotation.
 - **b.** Reasoning Are angles with measures of 40° and 680° coterminal? Explain.
- **c.** Make a Conjecture Generalize how the measures of two coterminal angles are related.

- **2. a.** Find the decimal values of $-\frac{1}{2}$ and $-\frac{\sqrt{3}}{2}$. Then use a calculator to find cos (-120°) and sin (-120°) . How do these values compare to each other? How do they compare to the exact values found in Example 2?
 - **b.** Find the exact values of cos 135° and sin 135°. Use properties of a 45°-45°-90° triangle. Use a calculator to find the decimal equivalents.
 - c. Find the exact values of $\cos 150^\circ$ and $\sin 150^\circ$.