Episode: "Obsession"

NUMB3RS Activity: Telling Time with the Sun Episode: "Obsession"

Topic: Uses of Trigonometry **Grade Level**: 7 - 10

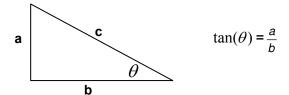
Objective: Be able to use values of tangent to compute angles in a right triangle.

Time: 10 - 15 minutes

Materials: Calculator, protractor, ruler

Introduction

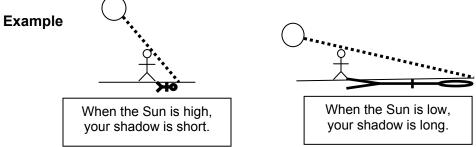
Trigonometry is the study of triangle measurements and has been used by mathematicians for centuries to accurately determine distances without having to physically measure them. More importantly, it can help to calculate angles that would otherwise be very difficult to measure. In this activity, students estimate the angle of elevation using the tangent ratio. In a right triangle, the tangent of an angle is the ratio of the side opposite the angle to the side adjacent to the angle, excluding the hypotenuse.



Discuss with Students

NUMB3RS Example In "Obsession," Charlie has a photograph that shows a basketball hoop and its shadow from the sun. He then uses trigonometry to determine the sun's angle of elevation. Knowing the sun's elevation and the time of day, Charlie could then figure out *where* the photograph was taken.

If you know where the photograph was taken but you don't know when, you might be able to figure out the angle of elevation of the sun if the photo contains enough information. As the sun moves across the sky, its angle of elevation changes—it first increases and then decreases before setting. Because the sun is moving, your shadow looks different at different times of the day. Your shadow is longer when the sun is low in the sky and is shortest when the sun is at its peak.

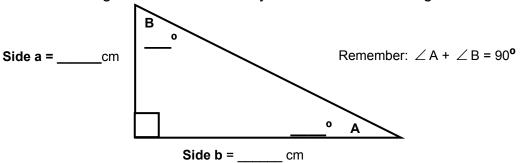


Student Page Answers: **1**. a = 3.5 cm, a = 7 cm, angle $B = 64^{\circ}$, angle $A = 26^{\circ}$, so $a \div b = 0.50$ **2**. 0.49 **3**. they are equal (or very close) **4**. **a**. check drawing **b**. 23/33 = 0.697 **c**. $\approx 35^{\circ}$ **d**. 34.9° **e**. less than 45° **f**. Answers will vary. For example, he could find the height of a suspect if he knows the shadow length and the angle of elevation. Note: Answers may change if the size of the figure changes.

Name: _____ Date: ____

NUMB3RS Activity: Telling Time with the Sun

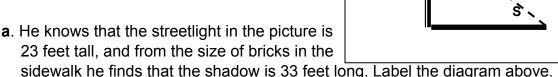
Explore the tangent of angles: Using a ruler and protractor, measure the labeled sides and angles of the right triangle to the nearest tenth of a centimeter and the nearest degree. Be sure to label your answers in the diagram.



- **1**. Give the value of the ratio $\frac{a}{b}$ (to the hundredths place):
- 2. Use your calculator to find the tangent (TAN) of ∠A: _____
- **3**. What is the relationship between the tangent of $\angle \mathbf{A}$ and the ratio of sides a and b?

Use tangent to find angles: You can use tangent to find angles without measuring them. In the problem below, the drawing is *not to scale.*

4. Charlie has a photograph and is asked to determine what time of day the photograph was taken. If he can figure out the sun's angle of elevation, he can determine the time.



- **b**. Angle **S** in the diagram is the angle of elevation of the sun. Use the ratios of the sides from part **a** to find the tangent of \angle **S**.
- c. To find the measure of \angle S, choose an angle between 0° and 90°, then find the tangent of that angle by pressing **TAN** on your calculator. Compare that measurement to the one you found for part b. What is your best estimate for the measure of \angle S?

NUMB3RS Activity Student Page 2

Name:		Date:	
d . You can also calculator. Ve (23/33).	o find the measure of \angle S crify that your answer to pa	by using the TAN⁻¹ function art c is correct by pressing	n on your TAN -1
e. For what and height?	gles of elevation would you	ur shadow be longer than y	our actual
f. Describe and solve a crime		lie would use the tangent r	atio to help

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NUMB3RS Activity Episode: "Obsession"

The goal of this activity is to give your students a short and simple snapshot into a very extensive math topic. TI and NCTM encourage you and your students to learn more about this topic using the extensions provided below and through your own independent research.

Extensions

Activity: Make a Sundial

Introduction

In "Obsession," Charlie and Larry use two photographs of the same scene, taken at different times. By comparing the two photographs and using spherical geometry and trigonometry, they are able to determine the location of where the photos were taken. For an example closer to home, measure the length of the shadow of your school's flagpole (you must know its height) at two different times of day, on the same day (record the time to the nearest second). Then, you can use spherical geometry to compute the latitude and longitude of the flagpole. The formula needed is:

$$\sin \alpha = \sin \varphi \sin \delta + \cos \delta \cos \varphi (\tau - e_{\delta} - \lambda)$$

lpha = the sun's angle of elevation, φ = the geographic latitude, δ = the sun's declination (determined by the date), τ = the standard time as an angle, e_{δ} = the equation of time (determined completely by the date), and λ = the longitude difference from the central meridian of your time zone. To obtain the value of the rest of the necessary variables, here is a website, which gives the sun's declination and the equation of time, and standard time as an angle: http://www.jgiesen.de/deceot/

For the Student

Explain why you need to take latitude and longitude into consideration when you build a sundial. Think about the extreme examples of living on one of the poles or at the equator. How would this affect your construction?

Resources

http://www.rbduncan.com/sn4a2.doc.htm An instructional guide to building a sundial.

http://www.qwerty.co.za/sundials/howto/steps.html Another instructional guide to building a sundial.

http://www.astrosociety.org/education/publications/tnl/31/arch2.html Learn how the ancient astronomers determined the elevation angle.

Related Topic

Most students study Euclidean Geometry which is based on a 2-dimensional plane. However, there are other types of geometries as well. In the show, Charlie uses spherical geometry, or geometry based on a sphere to determine the latitude and longitude of a photograph's subject based on the comparison of two photos. More advanced students can learn more about spherical geometry. A good starting point is the website:

http://www.math.uncc.edu/~droyster/math3181/notes/hyprgeom/node5.html