











page 7 of21

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 $x = \frac{1}{\sqrt{2}}$ y = 0,ff FREE Download Study Package from website: www.TekoClasses.com & www.MathsBySuhag.com $= \int_{-\pi}^{\sqrt{5}} \left(\frac{-3x + \sqrt{5 - x^2}}{5} - \frac{-3x - \sqrt{5 - x^2}}{5} \right) dx$ Required area $=\frac{2}{5}\int_{\sqrt{5}}^{\sqrt{5}}\sqrt{5-x^2}\,dx$ $=\frac{4}{5}\int_{0}^{\sqrt{5}}\sqrt{5-x^2}dx$ Put x = $\sqrt{5} \sin \theta$: dx = $\sqrt{5} \cos \theta d\theta$ $L.L: x = 0 \Rightarrow \theta = 0$ U.L: x = $\sqrt{5} \Rightarrow \theta = \frac{\pi}{2}$ $= \frac{4}{5} \int_{-\infty}^{2} \sqrt{5 - 5\sin^2 \theta} \sqrt{5} \cos \theta d\theta$ $=4\int_{1}^{2}\cos^{2}\theta d\theta = 4\frac{1}{2}\frac{\pi}{2} = \pi$ Let A (m) be area bounded by parabola $y = x^2 + 2x - 3$ and the line y = mx + 1. Find the least area Example : A(m). Solution. Solving we obtain x^{2} + (2 – m) x – 4 = 0 Let α,β be roots $\Rightarrow \alpha + \beta = m - 2, \alpha\beta =$ $\int (mx+1-x^2-2x+3)dx$ A(m) = $\int_{\infty} (-x^2 + (m-2)x + 4) dx$ $= \left(-\frac{x^{3}}{3} + (m-2)\frac{x^{2}}{2} + 4x \right)^{\beta}$ $= \left| \frac{\alpha^{3} - \beta^{3}}{3} + \frac{m - 2}{2} (\beta^{2} - \alpha^{2}) + 4 (\beta - \alpha) \right|$ $= |\beta - \alpha|. \left| -\frac{1}{3}(\beta^2 + \beta\alpha + \alpha^2) + \frac{(m-2)}{2}(\beta + \alpha) + 4 \right|$ $= \sqrt{(m-2)^2 + 16} \left| -\frac{1}{3} \left((m-2)^2 + 4 \right) + \frac{(m-2)}{2} (m-2) + 4 \right|$ $=\sqrt{(m-2)^2+16}$ $\left|\frac{1}{6}(m-2)^2+\frac{8}{3}\right|$ A(m) = $\frac{1}{6} ((m-2)^2 + 16)^{3/2}$ Leas A(m) = $\frac{1}{6}$ (16)^{3/2} = $\frac{32}{3}$.

Self Practice Problems				
٤ ^{1.}	Find the area between curve $y = x^2 - 3x + 2$ and x-axis			page 8 of21
0.	(i) bounded between $x = 1$ and $x = 2$.	Ans.	$\frac{1}{6}$	pa
ıhag	(ii) bound between $x = 0$ and $x = 2$.	Ans.	1	559.
၂၃ ၃	Find the area included between curves $y = 2x - x^2$ and $y + 3 = 0$.			260
hsBy	Ans. $\frac{32}{3}$			r 9009
.Mat ™	Find area between curves $y = x^2$ and $y = 3x - 2$ from $x = 0$ to $x = 2$. Ans. 1			Numbe
Å4. Å	Curves y = sinx and y = cosx intersect at infinite number of points forming region them calculate area of one such region.	s of equ	al area betw	een ddys
ଷ	Ans. $2\sqrt{2}$			Vhat
www.TekoClasses.com & www.MathsBySuhag.com ه	Find the area of the region bounded by the parabola $(y - 2)^2 = (x - 1)$ and the tang and x-axis. Ans. 9	ent to it	at ordinate y	الله الله الله الله الله الله الله الله
asse 9	Find the area included between $y = \tan^{-1}x$, $y = \cot^{-1}x$ and y -axis. Ans. $\ell n2$			98930
0 _{7.}	Find area common to circle $x^2 + y^2 = 2$ and the parabola $y^2 = x$.			
v.Tel	Ans. $\frac{\pi}{3} - \frac{\sqrt{3}}{2} - \frac{2}{3}$			00 00
¥8.	Find the area included between curves $y = \frac{4 - x^2}{4 - x^2}$ and $5y = 3 x - 6$.		U	55) 32
m website:	Ans. $2\pi - \frac{8}{5}$	1		hone : (075
≥ _{9.}	Find the area bounded by the curve $ y + \frac{1}{2} = e^{- x }$.			a.IF
ron	Ans. $2(1-ln2)$			Shop
ີ ຢູ 10.	Find the area of loop $y^2 = x (x - 1)^2$.			sir), E
icka	Ans. $\frac{8}{15}$			R. K.
°C 11. ∑	Find the area enclosed by $ x + y \le 3$ and $xy \ge 2$. Ans. $3-4\ell n2$			iya (S.
0 N 12.	Find are bounded by $x^2 + y^2 \le 2ax$ and $y^2 \ge ax$, $x \ge 0$.			Kari
oad S	Ans. $\left(\frac{3\pi-8}{6}\right)a^2$.			hag R.
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