

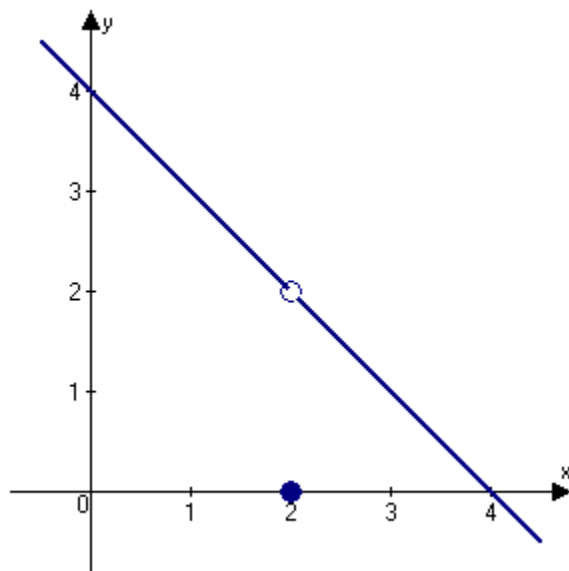
Name: _____ Date: _____

1. Let

$$f(x) = \begin{cases} 4-x, & x \neq 2 \\ 0 & x = 2 \end{cases}$$

Determine the following limit. (Hint: Use the graph of the function.)

$$\lim_{x \rightarrow 2} f(x)$$

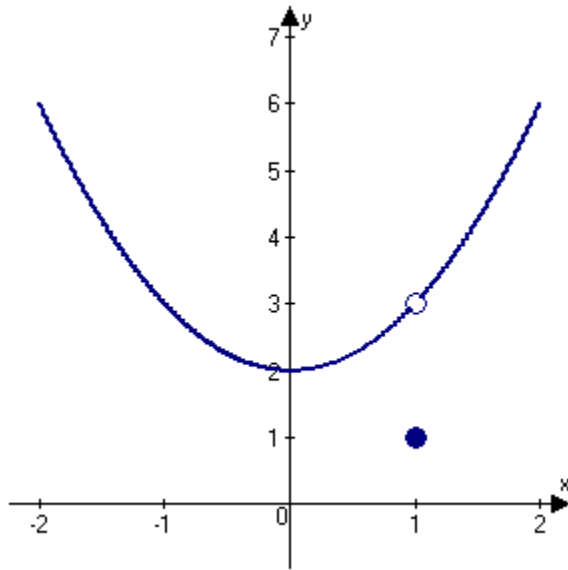


2. Let

$$f(x) = \begin{cases} x^2 + 2, & x \neq 1 \\ 1, & x = 1 \end{cases}$$

Determine the following limit. (Hint: Use the graph of the function.)

$$\lim_{x \rightarrow 1} f(x)$$



3. Let $f(x) = 4x + 3$ and $g(x) = x^3$. Find the limits:

(a) $\lim_{x \rightarrow 3} f(x)$ (b) $\lim_{x \rightarrow 5} g(x)$ (c) $\lim_{x \rightarrow 5} g(f(x))$

4. Let $f(x) = x^2 - 3$ and $g(x) = 2x$. Find the limits:

(a) $\lim_{x \rightarrow -1} f(x)$ (b) $\lim_{x \rightarrow -3} g(x)$ (c) $\lim_{x \rightarrow -4} g(f(x))$

5. Let $f(x) = 3 + x^2$ and $g(x) = \sqrt{x + 2}$. Find the limits:

(a) $\lim_{x \rightarrow 3} f(x)$ (b) $\lim_{x \rightarrow 3} g(x)$ (c) $\lim_{x \rightarrow 3} g(f(x))$

6. Let $f(x) = 4x^2 - 5x - 4$ and $g(x) = \sqrt[3]{x - 5}$. Find the limits:

(a) $\lim_{x \rightarrow 5} f(x)$ (b) $\lim_{x \rightarrow 1} g(x)$ (c) $\lim_{x \rightarrow 2} g(f(x))$

7. Find the limit:

$$\lim_{x \rightarrow \frac{5\pi}{6}} \sin x$$

8. Find the limit:

$$\lim_{x \rightarrow 2} \cos\left(\frac{\pi x}{3}\right)$$

9. Find the limit:

$$\lim_{x \rightarrow \pi} \tan\left(\frac{x}{6}\right)$$

10. Suppose that $\lim_{x \rightarrow c} f(x) = 7$ and $\lim_{x \rightarrow c} g(x) = 6$. Find the following limit:

$$\lim_{x \rightarrow c} [f(x)^{g(x)}]$$

11. Suppose that $\lim_{x \rightarrow c} f(x) = 15$ and $\lim_{x \rightarrow c} g(x) = -7$. Find the following limit:

$$\lim_{x \rightarrow c} [f(x) + g(x)]$$

12. Suppose that $\lim_{x \rightarrow c} f(x) = -12$ and $\lim_{x \rightarrow c} g(x) = -8$. Find the following limit:

$$\lim_{x \rightarrow c} [f(x) - g(x)]$$

13. Suppose that $\lim_{x \rightarrow c} f(x) = -8$ and $\lim_{x \rightarrow c} g(x) = 4$. Find the following limit:

$$\lim_{x \rightarrow c} [-9g(x)]$$

14. Suppose that $\lim_{x \rightarrow c} f(x) = 6$ and $\lim_{x \rightarrow c} g(x) = -2$. Find the following limit:

$$\lim_{x \rightarrow c} [f(x)g(x)]$$

15. Suppose that $\lim_{x \rightarrow c} f(x) = 11$ and $\lim_{x \rightarrow c} g(x) = -9$. Find the following limit:

$$\lim_{x \rightarrow c} \frac{f(x)}{g(x)}$$

16. Find the following limit (if it exists). Write a simpler function that agrees with the given function at all but one point.

$$\lim_{x \rightarrow -6} \frac{x^3 + 216}{x + 6}$$

17. Find the following limit (if it exists). Write a simpler function that agrees with the given function at all but one point.

$$\lim_{x \rightarrow 1} \frac{-3x^2 + 14x - 11}{x - 1}$$

18. Find the limit (if it exists):

$$\lim_{x \rightarrow -4} \frac{x + 4}{x^2 - 16}$$

19. Find the limit (if it exists):

$$\lim_{\Delta x \rightarrow 0} \frac{(x + \Delta x)^2 + (x + \Delta x) + 1 - (x^2 + x + 1)}{\Delta x}$$

20. Determine the limit (if it exists):

$$\lim_{x \rightarrow 0} \frac{\sin x (1 - \cos x)}{3x^6}$$

21. Determine the limit (if it exists):

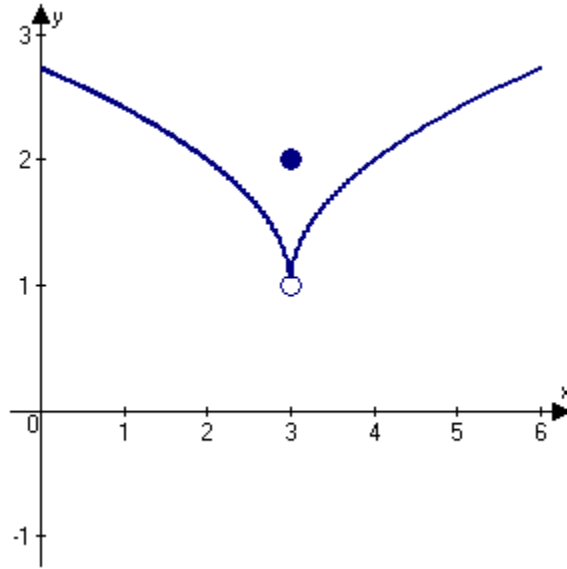
$$\lim_{x \rightarrow 0} \frac{-2(1 - \cos x)}{x^2}$$

22. Determine the limit (if it exists):

$$\lim_{x \rightarrow 0} \frac{\sin^6 x}{x^6}$$

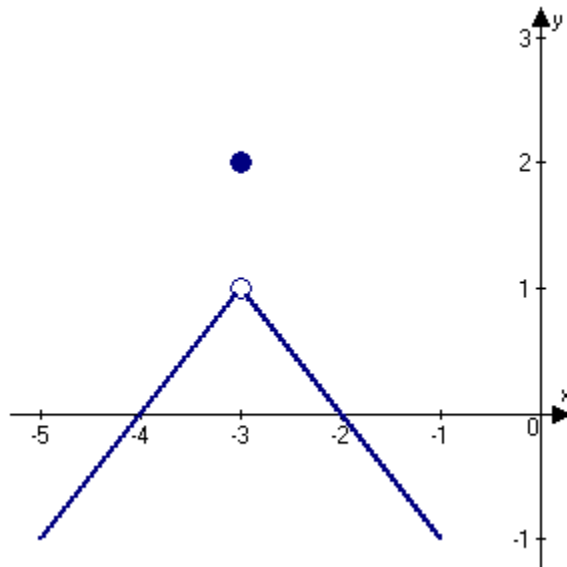
23. Use the graph as shown to determine the following limits, and discuss the continuity of the function at $x = 3$.

(i) $\lim_{x \rightarrow 3^+} f(x)$ (ii) $\lim_{x \rightarrow 3^-} f(x)$ (iii) $\lim_{x \rightarrow 3} f(x)$



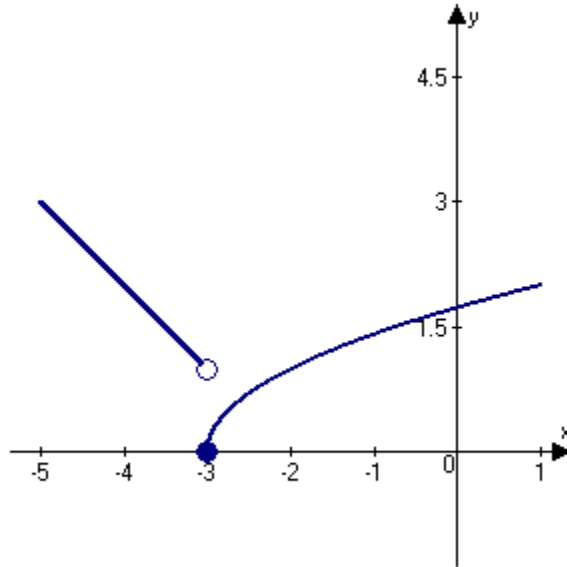
24. Use the graph as shown to determine the following limits, and discuss the continuity of the function at $x = -3$.

(i) $\lim_{x \rightarrow -3^+} f(x)$ (ii) $\lim_{x \rightarrow -3^-} f(x)$ (iii) $\lim_{x \rightarrow -3} f(x)$



25. Use the graph to determine the following limits, and discuss the continuity of the function at $x = -3$.

(i) $\lim_{x \rightarrow -3^+} f(x)$ (ii) $\lim_{x \rightarrow -3^-} f(x)$ (iii) $\lim_{x \rightarrow -3} f(x)$



26. Find the x -values (if any) at which the function $f(x) = -14x^2 - 14x - 9$ is not continuous. Which of the discontinuities are removable?

27. Find the x -values (if any) at which the function $f(x) = \frac{x}{x^2 - 49}$ is not continuous. Which of the discontinuities are removable?

28. Find the x -values (if any) at which the function $f(x) = \frac{x - 3}{x^2 - 9x + 18}$ is not continuous. Which of the discontinuities are removable?

29. Find constants a and b such that the function

$$f(x) = \begin{cases} 8, & x \leq -7 \\ ax + b, & -7 < x < 9 \\ -8, & x \geq 9 \end{cases}$$

is continuous on the entire real line.

30. Find the constant a such that the function

$$f(x) = \begin{cases} -7 \cdot \frac{\sin x}{x}, & x < 0 \\ a + 9x, & x \geq 0 \end{cases}$$

is continuous on the entire real line.

31. Find the vertical asymptotes (if any) of the function $f(x) = \frac{x^2 - 100}{x^2 + 4x - 60}$.

32. Find the vertical asymptotes (if any) of the function $f(x) = \frac{x^2 + 4x + 3}{x^3 - 7x^2 + 7x + 15}$.

33. Find the vertical asymptotes (if any) of the function $f(x) = \tan(-15x)$.

34. Find the limit:

$$\lim_{x \rightarrow 7^+} \frac{x + 10}{x - 7}$$

35. Find the limit:

$$\lim_{x \rightarrow 12} \frac{x^2 - 12x}{(x^2 + 144)(x - 12)}$$

36. Find the limit:

$$\lim_{x \rightarrow 0^+} \left(x^9 + \frac{1}{x} \right)$$