## CHAPTER 2 Measurements

## Opening Essay

Data suggest that a male child will weigh $50 \%$ of his adult weight at about 11 years of age. However, he will reach $50 \%$ of his adult height at only 2 years of age. It is obvious, then, that people eventually stop growing up but continue to grow out. Data also suggest that the average human height has been increasing over time. In industrialized countries, the average height of people increased 5.5 inches from 1810 to 1984. Most scientists attribute this simple, basic measurement of the human body to better health and nutrition.


Source: Chart courtesy of Centers for Disease Control and Prevention, http://www.cdc.gov/nchs/nhanes.htm\#Set\ 1.

In 1983, an Air Canada airplane had to make an emergency landing because it unexpectedly ran out of fuel; ground personnel had filled the fuel tanks with a certain number of pounds of fuel, not kilograms of fuel. In 1999, the Mars Climate Orbiter spacecraft was lost attempting to orbit Mars because the thrusters were programmed in terms of English units, even though the engineers built the spacecraft using metric units. In 1993, a nurse mistakenly administered 23 units of morphine to a patient rather than the " $2-3$ " units prescribed. (The patient ultimately survived.) These incidents occurred because people weren't paying attention to quantities.

Chemistry, like all sciences, is quantitative. It deals with quantities, things that have amounts and units. Dealing with quantities is very important in chemistry, as is relating quantities to each other. In this chapter, we will discuss how we deal with numbers and units, including how they are combined and manipulated.

## 1. EXPRESSING NUMBERS

## LEARNINGOBJECTIVE

1. Learn to express numbers properly.

Quantities have two parts: the number and the unit. The number tells "how many." It is important to be able to express numbers properly so that the quantities can be communicated properly.

Standard notation is the straightforward expression of a number. Numbers such as 17, 101.5, and 0.00446 are expressed in standard notation. For relatively small numbers, standard notation is fine. However, for very large numbers, such as $306,000,000$, or for very small numbers, such as 0.000000419 , standard notation can be cumbersome because of the number of zeros needed to place nonzero numbers in the proper position.

Scientific notation is an expression of a number using powers of 10 . Powers of 10 are used to express numbers that have many zeros:

| $10^{0}$ | $=1$ |
| :--- | :--- |
| $10^{1}$ | $=10$ |
| $10^{2}$ | $=100=10 \times 10$ |
| $10^{3}$ | $=1,000=10 \times 10 \times 10$ |
| $10^{4}$ | $=10,000=10 \times 10 \times 10 \times 10$ |

and so forth. The raised number to the right of the 10 indicating the number of factors of 10 in the original number is the exponent. (Scientific notation is sometimes called exponential notation.) The exponent's value is equal to the number of zeros in the number expressed in standard notation.

Small numbers can also be expressed in scientific notation but with negative exponents:

| $10^{-1}$ | $=0.1=1 / 10$ |
| :--- | :--- |
| $10^{-2}$ | $=0.01=1 / 100$ |
| $10^{-3}$ | $=0.001=1 / 1,000$ |
| $10^{-4}$ | $=0.0001=1 / 10,000$ |

and so forth. Again, the value of the exponent is equal to the number of zeros in the denominator of the associated fraction. A negative exponent implies a decimal number less than one.

A number is expressed in scientific notation by writing the first nonzero digit, then a decimal point, and then the rest of the digits. The part of a number in scientific notation that is multiplied by a power of 10 is called the coefficient. Then determine the power of 10 needed to make that number into the original number and multiply the written number by the proper power of 10 . For example, to write 79,345 in scientific notation,

$$
79,345=7.9345 \times 10,000=7.9345 \times 10^{4}
$$

Thus, the number in scientific notation is $7.9345 \times 10^{4}$. For small numbers, the same process is used, but the exponent for the power of 10 is negative:

$$
0.000411=4.11 \times 1 / 10,000=4.11 \times 10^{-4}
$$

Typically, the extra zero digits at the end or the beginning of a number are not included. (See Figure 2.1.)

## E X A M P L E 1

Express these numbers in scientific notation.

1. 306,000
2. 0.00884
3. $2,760,000$
4. 0.000000559

## Solution

1. The number 306,000 is 3.06 times 100,000 , or 3.06 times $10^{5}$. In scientific notation, the number is $3.06 \times$ $10^{5}$.
2. The number 0.00884 is 8.84 times $1 / 1,000$, which is 8.84 times $10^{-3}$. In scientific notation, the number is $8.84 \times 10^{-3}$.
3. The number $2,760,000$ is 2.76 times $1,000,000$, which is the same as 2.76 times $10^{6}$. In scientific notation, the number is written as $2.76 \times 10^{6}$. Note that we omit the zeros at the end of the original number.
4. The number 0.000000559 is 5.59 times $1 / 10,000,000$, which is 5.59 times $10^{-7}$. In scientific notation, the number is written as $5.59 \times 10^{-7}$.

## Test Yourself

Express these numbers in scientific notation.

1. 23,070
2. 0.0009706

Answers

1. $2.307 \times 10^{4}$
2. $9.706 \times 10^{-4}$

Another way to determine the power of 10 in scientific notation is to count the number of places you need to move the decimal point to get a numerical value between 1 and 10 . The number of places equals the power of 10 . This number is positive if you move the decimal point to the right and negative if you move the decimal point to the left:


Many quantities in chemistry are expressed in scientific notation. When performing calculations, you may have to enter a number in scientific notation into a calculator. Be sure you know how to correctly enter a number in scientific notation into your calculator. Different models of calculators require different actions for properly entering scientific notation. If in doubt, consult your instructor immediately. (See Figure 2.2.)

FIGURE 2.1
Using Scientific Notation
The earth is about
$93,000,000$ miles from the sun. In scientific notation, this is $9.3 \times 10^{7}$ miles.

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FIGURE 2.2 Scientific Notation on a Calculator
This calculator shows only the coefficient and the power of 10 to represent the number in scientific notation. Thus, the number being displayed is $3.84951 \times 10^{18}$, or $3,849,510,000,000,000,000$.

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## KEYTAKEAWAYS

- Standard notation expresses a number normally.
- Scientific notation expresses a number as a coefficient times a power of 10.
- The power of 10 is positive for numbers greater than 1 and negative for numbers between 0 and 1 .


## EXERCISES

1. Express these numbers in scientific notation.
a. 56.9
b. 563,100
c. 0.0804
d. 0.00000667
2. Express these numbers in scientific notation.
a. $-890,000$
b. $602,000,000,000$
c. 0.0000004099
d. 0.000000000000011
3. Express these numbers in scientific notation.
a. 0.00656
b. 65,600
c. $4,567,000$
d. 0.000005507
4. Express these numbers in scientific notation.
a. 65
b. -321.09
c. 0.000077099
d. 0.000000000218
5. Express these numbers in standard notation.
a. $1.381 \times 10^{5}$
b. $5.22 \times 10^{-7}$
c. $9.998 \times 10^{4}$
6. Express these numbers in standard notation.
a. $7.11 \times 10^{-2}$
b. $9.18 \times 10^{2}$
c. $3.09 \times 10^{-10}$
7. Express these numbers in standard notation.
a. $8.09 \times 10^{0}$
b. $3.088 \times 10^{-5}$
c. $-4.239 \times 10^{2}$
8. Express these numbers in standard notation.
a. $2.87 \times 10^{-8}$
b. $1.78 \times 10^{11}$
c. $1.381 \times 10^{-23}$
9. These numbers are not written in proper scientific notation. Rewrite them so that they are in proper scientific notation.
a. $72.44 \times 10^{3}$
b. $9,943 \times 10^{-5}$
c. $588,399 \times 10^{2}$
10. These numbers are not written in proper scientific notation. Rewrite them so that they are in proper scientific notation.
a. $0.000077 \times 10^{-7}$
b. $0.000111 \times 10^{8}$
c. $602,000 \times 10^{18}$
11. These numbers are not written in proper scientific notation. Rewrite them so that they are in proper scientific notation.
a. $345.1 \times 10^{2}$
b. $0.234 \times 10^{-3}$
c. $1,800 \times 10^{-2}$
12. These numbers are not written in proper scientific notation. Rewrite them so that they are in proper scientific notation.
a. $8,099 \times 10^{-8}$
b. $34.5 \times 10^{0}$
c. $0.000332 \times 10^{4}$
13. Write these numbers in scientific notation by counting the number of places the decimal point is moved.
a. $123,456.78$
b. 98,490
c. 0.000000445
14. Write these numbers in scientific notation by counting the number of places the decimal point is moved.
a. 0.000552
b. 1,987
c. 0.00000000887
15. Use your calculator to evaluate these expressions. Express the final answer in proper scientific notation.
a. $456 \times\left(7.4 \times 10^{8}\right)=$ ?
b. $\left(3.02 \times 10^{5}\right) \div\left(9.04 \times 10^{15}\right)=$ ?
c. $0.0044 \times 0.000833=$ ?
16. Use your calculator to evaluate these expressions. Express the final answer in proper scientific notation.
a. $98,000 \times 23,000=$ ?
b. $98,000 \div 23,000=$ ?
c. $\left(4.6 \times 10^{-5}\right) \times\left(2.09 \times 10^{3}\right)=$ ?
17. Use your calculator to evaluate these expressions. Express the final answer in proper scientific notation.
a. $45 \times 132 \div 882=$ ?
b. $\left[\left(6.37 \times 10^{4}\right) \times\left(8.44 \times 10^{-4}\right)\right] \div(3.2209$ $\left.\times 10^{15}\right)=$ ?
18. Use your calculator to evaluate these expressions. Express the final answer in proper scientific notation.
a. $\left(9.09 \times 10^{8}\right) \div\left[\left(6.33 \times 10^{9}\right) \times(4.066 \times\right.$ $\left.\left.10^{-7}\right)\right]=$ ?
b. $9,345 \times 34.866 \div 0.00665=$ ?

## A N S W ERS

1. a. $5.69 \times 10^{1}$
b. $5.631 \times 10^{5}$
c. $8.04 \times 10^{-2}$
d. $6.67 \times 10^{-6}$
2. a. $6.56 \times 10^{-3}$
b. $6.56 \times 10^{4}$
c. $4.567 \times 10^{6}$
d. $5.507 \times 10^{-6}$
3. a. 138,100
b. 0.000000522
c. 99,980
4. a. 8.09
b. 0.00003088
c. -423.9
5. a. $7.244 \times 10^{4}$
b. $9.943 \times 10^{-2}$
c. $5.88399 \times 10^{7}$
6. a. $3.451 \times 10^{4}$
b. $2.34 \times 10^{-4}$
c. $1.8 \times 10^{1}$
7. a. $1.2345678 \times 10^{5}$
b. $9.849 \times 10^{4}$
c. $4.45 \times 10^{-7}$
8. a. $3.3744 \times 10^{11}$
b. $3.3407 \times 10^{-11}$
c. $3.665 \times 10^{-6}$
9. a. $6.7346 \times 10^{0}$
b. $1.6691 \times 10^{-14}$
fundamental unit
One of the seven basic units of SI used in science.

## numerical prefix

A prefix used with a unit that refers to a multiple or fraction of a fundamental unit to make a more conveniently sized unit for a specific quantity.

## 2. EXPRESSING UNITS

## LEARNINGOBJECTIVES

1. Learn the units that go with various quantities.
2. Express units using their abbreviations.
3. Make new units by combining numerical prefixes with units.

A number indicates "how much," but the unit indicates "of what." The "of what" is important when communicating a quantity. For example, if you were to ask a friend how close you are to Lake Erie and your friend says "six," then your friend isn't giving you complete information. Six what? Six miles? Six inches? Six city blocks? The actual distance to the lake depends on what units you use.

Chemistry, like most sciences, uses the International System of Units, or SI for short. (The letters SI stand for the French "le Système International d'unités.") SI specifies certain units for various types of quantities, based on seven fundamental units for various quantities. We will use most of the fundamental units in chemistry. Initially, we will deal with three fundamental units. The meter ( m ) is the SI unit of length. It is a little longer than a yard (see Figure 2.3). The SI unit of mass is the kilogram (kg), which is about 2.2 pounds (lb). The SI unit of time is the second (s).

FIGURE 2.3 The Meter
The SI standard unit of length, the meter, is a little longer than a yard.


To express a quantity, you need to combine a number with a unit. If you have a length that is 2.4 m , then you express that length as simply 2.4 m . A time of $15,000 \mathrm{~s}$ can be expressed as $1.5 \times 10^{4} \mathrm{~s}$ in scientific notation.

Sometimes, a given unit is not an appropriate size to easily express a quantity. For example, the width of a human hair is very small, and it doesn't make much sense to express it in meters. SI also defines a series of numerical prefixes that refer to multiples or fractions of a fundamental unit to make a unit more conveniently sized for a specific quantity. Table 2.1 lists the prefixes, their abbreviations, and their multiplicative factors. Some of the prefixes, such as kilo-, mega-, and giga-, represent more than one of the fundamental unit, while other prefixes, such as centi-, milli-, and micro-, represent fractions of the original unit. Note, too, that once again we are using powers of 10 . Each prefix is a multiple of or fraction of a power of 10 .

TABLE 2.1 Multiplicative Prefixes for SI Units

| Prefix | Abbreviation | Multiplicative Amount |
| :--- | :---: | :---: |
| giga- | G | $1,000,000,000 \times$ |
| mega- | M | $1,000,000 \times$ |
| kilo- | k | $1,000 \times$ |
| deci- | d | $1 / 10 \times$ |
| centi- | c | $1 / 100 \times$ |
| milli- | m | $1 / 1,000 \times$ |
| micro- | $\mu^{*}$ | $1 / 1,000,000 \times$ |
| nano- | n | $1 / 1,000,000,000 \times$ |
| pico- | p | $1 / 1,000,000,000,000 \times$ |
| * The letter $\mu$ is the Greek letter lowercase equivalent to an m and is called "mu" (pronounced "myoo"). |  |  |

To use the fractions to generate new units, simply combine the prefix with the unit itself; the abbreviation for the new unit is the combination of the abbreviation for the prefix and the abbreviation of the unit. For example, the kilometer ( km ) is $1,000 \times$ meter, or $1,000 \mathrm{~m}$. Thus, 5 kilometers ( 5 km ) is equal to $5,000 \mathrm{~m}$. Similarly, a millisecond (ms) is $1 / 1,000 \times$ second, or one-thousandth of a second. Thus, 25 ms is 25 thousandths of a second. You will need to become proficient in combining prefixes and units. (You may recognize that one of our fundamental units, the kilogram, automatically has a prefix-unit combination, the kilogram. The word kilogram means $1,000 \mathrm{~g}$.)

In addition to the fundamental units, SI also allows for derived units based on a fundamental unit or units. There are many derived units used in science. For example, the derived unit for area comes from the idea that area is defined as width times height. Because both width and height are lengths, they both have the fundamental unit of meter, so the unit of area is meter $\times$ meter, or meter ${ }^{2}$ $\left(\mathrm{m}^{2}\right)$. This is sometimes spoken as "square meters." A unit with a prefix can also be used to derive a unit for area, so we can also have $\mathrm{cm}^{2}, \mathrm{~mm}^{2}$, or $\mathrm{km}^{2}$ as acceptable units for area.

Volume is defined as length times width times height, so it has units of meter $\times$ meter $\times$ meter or meter ${ }^{3}\left(\mathrm{~m}^{3}\right)$, sometimes spoken as "cubic meters." The cubic meter is a rather large unit, however, so another unit is defined that is somewhat more manageable: the liter ( L ). A liter is $1 / 1,000$ th of a cubic meter and is a little more than 1 quart in volume (see Figure 2.4). Prefixes can also be used with the liter unit, so we can speak of milliliters ( $1 / 1,000$ th of a liter; mL ) and kiloliters ( $1,000 \mathrm{~L} ; \mathrm{kL}$ ).

Another definition of a liter is one-tenth of a meter cubed. Because one-tenth of a meter is 10 cm , then a liter is equal to $1,000 \mathrm{~cm}^{3}$ (Figure 2.5). Because 1 L equals $1,000 \mathrm{~mL}$, we conclude that 1 mL equals $1 \mathrm{~cm}^{3}$; thus, these units are interchangeable.

FIGURE 2.5 The Size of 1 Liter
One liter equals $1,000 \mathrm{~cm}^{3}$, so $1 \mathrm{~cm}^{3}$ is the same as 1 mL .


Units not only are multiplied together but also can be divided. For example, if you are traveling at one meter for every second of time elapsed, your velocity is 1 meter per second, or $1 \mathrm{~m} / \mathrm{s}$. The word per implies division, so velocity is determined by dividing a distance quantity by a time quantity. Other units for velocity include kilometers per hour ( $\mathrm{km} / \mathrm{h}$ ) or even micrometers per nanosecond ( $\mu \mathrm{m} / \mathrm{ns}$ ). Later, we will see other derived units that can be expressed as fractions.
derived unit
A unit that is a product or a quotient of a fundamental unit.

FIGURE 2.4
The Liter
The SI unit of volume, the liter, is slightly larger than 1 quart.
$1 \mathrm{qt}=0.94 \mathrm{~L}$
$1 \mathrm{~L} \quad 0.94 \mathrm{~L}$

## E X A M P L E 2

1. A human hair has a diameter of about $6.0 \times 10^{-5} \mathrm{~m}$. Suggest an appropriate unit for this measurement and write the diameter of a human hair in terms of that unit.
2. What is the velocity of a car if it goes 25 m in 5.0 s ?

## Solution

1. The scientific notation $10^{-5}$ is close to $10^{-6}$, which defines the micro- prefix. Let us use micrometers as the unit for hair diameter. The number $6.0 \times 10^{-5}$ can be written as $60 \times 10^{-6}$, and a micrometer is $10^{-6} \mathrm{~m}$, so the diameter of a human hair is about $60 \mu \mathrm{~m}$.
2. If velocity is defined as a distance quantity divided by a time quantity, then velocity is 25 meters/5.0 seconds. Dividing the numbers gives us $25 / 5.0=5.0$, and dividing the units gives us meters/second, or $\mathrm{m} / \mathrm{s}$. The velocity is $5.0 \mathrm{~m} / \mathrm{s}$.

## Test Yourself

1. Express the volume of an Olympic-sized swimming pool, 2,500,000 L, in more appropriate units.
2. A common garden snail moves about 6.1 m in 30 min . What is its velocity in meters per minute $(\mathrm{m} / \mathrm{min})$ ?

## Answers

1. 2.5 ML
2. $0.203 \mathrm{~m} / \mathrm{min}$

## KEYTAKEAWAYS

- Numbers tell "how much," and units tell "of what."
- Chemistry uses a set of fundamental units and derived units from SI units.
- Chemistry uses a set of prefixes that represent multiples or fractions of units.
- Units can be multiplied and divided to generate new units for quantities.


## EXERCISES

1. Identify the unit in each quantity.
a. 2 boxes of crayons
b. 3.5 grams of gold
2. Identify the unit in each quantity.
a. 32 oz of cheddar cheese
b. $0.045 \mathrm{~cm}^{3}$ of water
3. Identify the unit in each quantity.
a. 9.58 s (the current world record in the 100 m dash)
b. 6.14 m (the current world record in the pole vault)
4. Identify the unit in each quantity.
a. 2 dozen eggs
b. $2.4 \mathrm{~km} / \mathrm{s}$ (the escape velocity of the moon, which is the velocity you need at the surface to escape the moon's gravity)
5. Indicate what multiplier each prefix represents.
a. $k$
b. m
c. M
6. Indicate what multiplier each prefix represents.
a. C
b. G
c. $\mu$
7. Give the prefix that represents each multiplier.
a. $1 / 1,000$ th $\times$
b. $1,000 \times$
c. $1,000,000,000 \times$
8. Give the prefix that represents each multiplier.
a. 1/1,000,000,000th $\times$
b. $1 / 100$ th $\times$
c. $1,000,000 \times$
9. Complete the following table with the missing information.

| Unit | Abbreviation |
| :--- | :---: |
| kilosecond |  |
|  | mL |
|  | Mg |
| centimeter |  |

10. Complete the following table with the missing information.

| Unit | Abbreviation |
| :--- | :---: |
| kilometer per second |  |
| second |  |
|  | $\mathrm{cm}^{3}$ |
|  | $\mu \mathrm{~L}$ |
| nanosecond |  |

11. Express each quantity in a more appropriate unit. There may be more than one acceptable answer.
a. $3.44 \times 10^{-6} \mathrm{~S}$
b. $3,500 \mathrm{~L}$
c. 0.045 m
12. Express each quantity in a more appropriate unit. There may be more than one acceptable answer.
a. $0.000066 \mathrm{~m} / \mathrm{s}$ (Hint: you need consider only the unit in the numerator.)
b. $4.66 \times 10^{6} \mathrm{~s}$
c. $7,654 \mathrm{~L}$
13. Express each quantity in a more appropriate unit. There may be more than one acceptable answer.
a. $43,600 \mathrm{~mL}$
b. 0.0000044 m
c. $1,438 \mathrm{~ms}$
14. Express each quantity in a more appropriate unit. There may be more than one acceptable answer.
a. $0.000000345 \mathrm{~m}^{3}$
b. $47,000,000 \mathrm{~mm}^{3}$
c. 0.00665 L
15. Multiplicative prefixes are used for other units as well, such as computer memory. The basic unit of computer memory is the byte (b). What is the unit for one million bytes?
16. You may have heard the terms microscale or nanoscale to represent the sizes of small objects. What units of length do you think are useful at these scales? What fractions of the fundamental unit of length are these units?
17. Acceleration is defined as a change in velocity per time. Propose a unit for acceleration in terms of the fundamental SI units.
18. Density is defined as the mass of an object divided by its volume. Propose a unit of density in terms of the fundamental SI units.

## A N S W ERS

1. a. boxes of crayons
b. grams of gold
2. a. seconds
b. meters
3. a. $1,000 \times$
b. $1 / 1,000 \times$
c. $1,000,000 \times$
4. a. milli-
b. kilo-
c. giga-
5. | Unit | Abbreviation |
| :--- | :---: |
| kilosecond | ks |
| milliliter | mL |
| megagram | Mg |
| centimeter | cm |
6. a. $3.44 \mu \mathrm{~s}$
b. 3.5 kL
c. 4.5 cm
7. a. 43.6 L
b. $4.4 \mu \mathrm{~m}$
c. 1.438 s
8. megabytes (Mb)
9. meters/second ${ }^{2}$

## 3. SIGNIFICANT FIGURES

## LEARNINGOBJECTIVES

1. Apply the concept of significant figures to limit a measurement to the proper number of digits.
2. Recognize the number of significant figures in a given quantity.
3. Limit mathematical results to the proper number of significant figures.

If you use a calculator to evaluate the expression 337/217, you will get the following:

$$
\frac{337}{217}=1.55299539171 \ldots
$$

and so on for many more digits. Although this answer is correct, it is somewhat presumptuous. You start with two values that each have three digits, and the answer has twelve digits? That does not make much sense from a strict numerical point of view.

Consider using a ruler to measure the width of an object, as shown in Figure 2.6. The object is definitely more than 1 cm long, so we know that the first digit in our measurement is 1 . We see by counting the tick marks on the ruler that the object is at least three ticks after the 1 . If each tick represents 0.1 cm , then we know the object is at least 1.3 cm wide. But our ruler does not have any more ticks between the 0.3 and the 0.4 marks, so we can't know exactly how much the next decimal place is. But with a practiced eye we can estimate it. Let us estimate it as about six-tenths of the way between the third and fourth tick marks, which estimates our hundredths place as 6 , so we identify a measurement of 1.36 cm for the width of the object.

FIGURE 2.6 Expressing Width
What is the proper way to express the width of this object?


Does it make any sense to try to report a thousandths place for the measurement? No, it doesn't; we are not exactly sure of the hundredths place (after all, it was an estimate only), so it would be fruitless to estimate a thousandths place. Our best measurement, then, stops at the hundredths place, and we report 1.36 cm as proper measurement.

This concept of reporting the proper number of digits in a measurement or a calculation is called significant figures. Significant figures (sometimes called significant digits) represent the limits of what values of a measurement or a calculation we are sure of. The convention for a measurement is that the quantity reported should be all known values and the first estimated value. The conventions for calculations are discussed as follows.

## EXAMPLE 3

Use each diagram to report a measurement to the proper number of significant figures.
1.


## Solution

1. The arrow is between 4.0 and 5.0 , so the measurement is at least 4.0 . The arrow is between the third and fourth small tick marks, so it's at least 0.3. We will have to estimate the last place. It looks like about onethird of the way across the space, so let us estimate the hundredths place as 3. Combining the digits, we have a measurement of 4.33 psi (psi stands for "pounds per square inch" and is a unit of pressure, like air in a tire). We say that the measurement is reported to three significant figures.
2. The rectangle is at least 1.0 cm wide but certainly not 2.0 cm wide, so the first significant digit is 1 . The rectangle's width is past the second tick mark but not the third; if each tick mark represents 0.1 , then the rectangle is at least 0.2 in the next significant digit. We have to estimate the next place because there are no markings to guide us. It appears to be about halfway between 0.2 and 0.3 , so we will estimate the next place to be a 5 . Thus, the measured width of the rectangle is 1.25 cm . Again, the measurement is reported to three significant figures.

## Test Yourself

What would be the reported width of this rectangle?


Answer
0.63 cm

In many cases, you will be given a measurement. How can you tell by looking what digits are significant? For example, the reported population of the United States is $306,000,000$. Does that mean that it is exactly three hundred six million or is some estimation occurring?

The following conventions dictate which numbers in a reported measurement are significant and which are not significant:

1. Any nonzero digit is significant.
2. Any zeros between nonzero digits (i.e., embedded zeros) are significant.
3. Zeros at the end of a number without a decimal point (i.e., trailing zeros) are not significant; they serve only to put the significant digits in the correct positions. However, zeros at the end of any number with a decimal point are significant.
4. Zeros at the beginning of a decimal number (i.e., leading zeros) are not significant; again, they serve only to put the significant digits in the correct positions.

So, by these rules, the population figure of the United States has only three significant figures: the 3 , the 6 , and the zero between them. The remaining six zeros simply put the 306 in the millions position. (See Figure 2.7 for another example.)

FIGURE 2.7 Significant Figures
How many of the numbers in this display are actually significant?

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## EXAMPLE 4

Give the number of significant figures in each measurement.

1. 36.7 m
2. 0.006606 s
3. $2,002 \mathrm{~kg}$
4. $306,490,000$ people

## Solution

1. By rule 1 , all nonzero digits are significant, so this measurement has three significant figures.
2. By rule 4, the first three zeros are not significant, but by rule 2 the zero between the sixes is; therefore, this number has four significant figures.
3. By rule 2 , the two zeros between the twos are significant, so this measurement has four significant figures.
4. The four trailing zeros in the number are not significant, but the other five numbers are, so this number has five significant figures.

## Test Yourself

Give the number of significant figures in each measurement.

1. 0.000601 m
2. 65.080 kg

Answers

1. three significant figures
2. five significant figures

How are significant figures handled in calculations? It depends on what type of calculation is being performed. If the calculation is an addition or a subtraction, the rule is as follows: limit the reported answer to the rightmost column that all numbers have significant figures in common. For example, if you were to add 1.2 and 4.71, we note that the first number stops its significant figures in the tenths column, while the second number stops its significant figures in the hundredths column. We therefore limit our answer to the tenths column.
$\uparrow$ limit final answer to the tenths column: 5.6
We drop the last digit—the 1 -because it is not significant to the final answer.
The dropping of positions in sums and differences brings up the topic of rounding. Although there are several conventions, in this text we will adopt the following rule: the final answer should be rounded up if the first dropped digit is 5 or greater and rounded down if the first dropped digit is less than 5.
77.2
$\underline{10.46}$
87.66
$\uparrow$ limit final answer to the tenths column and round up: 87.7

## EXAMPLE 5

Express the final answer to the proper number of significant figures.

1. $101.2+18.702=$ ?
2. $202.88-1.013=$ ?

## Solution

1. If we use a calculator to add these two numbers, we would get 119.902 . However, most calculators do not understand significant figures, and we need to limit the final answer to the tenths place. Thus, we drop the 02 and report a final answer of 119.9 (rounding down).
2. A calculator would answer 201.867. However, we have to limit our final answer to the hundredths place. Because the first number being dropped is 7 , which is greater than 7 , we round up and report a final answer of 201.87.

## Test Yourself

Express the answer for $3.445+90.83-72.4$ to the proper number of significant figures.
Answer
21.9

If the operations being performed are multiplication or division, the rule is as follows: limit the answer to the number of significant figures that the data value with the least number of significant figures has. So if we are dividing 23 by 448, which have two and three significant figures each, we should limit the final reported answer to two significant figures (the lesser of two and three significant figures):

$$
\frac{23}{448}=0.051339286 \ldots=0.051
$$

The same rounding rules apply in multiplication and division as they do in addition and subtraction.

## EXAMPLE 6

Express the final answer to the proper number of significant figures.

1. $76.4 \times 180.4=$ ?
2. $934.9 \div 0.00455=$ ?

Solution

1. The first number has three significant figures, while the second number has four significant figures. Therefore, we limit our final answer to three significant figures: $76.4 \times 180.4=13,782.56=13,800$.
2. The first number has four significant figures, while the second number has three significant figures. Therefore we limit our final answer to three significant figures: $934.9 \div 0.00455=205,472.5275 \ldots=$ 205,000.

## Test Yourself

Express the final answer to the proper number of significant figures.

1. $22.4 \times 8.314=$ ?
2. $1.381 \div 6.02=$ ?

Answers

1. 186
2. 0.229

As you have probably realized by now, the biggest issue in determining the number of significant figures in a value is the zero. Is the zero significant or not? One way to unambiguously determine whether a zero is significant or not is to write a number in scientific notation. Scientific notation will include zeros in the coefficient of the number only if they are significant. Thus, the number $8.666 \times 10^{6}$ has four significant figures. However, the number $8.6660 \times 10^{6}$ has five significant figures. That last zero is significant; if it were not, it would not be written in the coefficient. So when in doubt about expressing the number of significant figures in a quantity, use scientific notation and include the number of zeros that are truly significant.

## K EY TAKEAW AY S

- Significant figures in a quantity indicate the number of known values plus one place that is estimated.
- There are rules for which numbers in a quantity are significant and which are not significant.
- In calculations involving addition and subtraction, limit significant figures based on the rightmost place that all values have in common.
- In calculations involving multiplication and division, limit significant figures to the least number of significant figures in all the data values.


## EXERCISES

1. Express each measurement to the correct noumber of significant figures.
2. Express each measurement to the correct number of significant f(o)ures.
3. How many significant figures do these numbers have?
a. 23
b. 23.0
c. 0.00023
d. 0.0002302


How many significant figures do these numbers have?
a. $5.44 \times 10^{8}$
b. $1.008 \times$

c. 43.09

d. 0.0000001381
5. How many significant figures do these numbers have?
a. 765,890
b. $765,890.0$
c. $1.2000 \times 10^{5}$
d. 0.0005060
6. How many significant figures do these numbers have?
a. 0.009
b. 0.0000009
c. 65,444
d. 65,040
7. Compute and express each answer with the proper number of significant figures, rounding as necessary.
a. $56.0+3.44=$ ?
b. $0.00665+1.004=$ ?
c. $45.99-32.8=$ ?
d. $45.99-32.8+75.02=$ ?
8. Compute and express each answer with the proper number of significant figures, rounding as necessary.
a. $1.005+17.88=$ ?
b. $56,700-324=$ ?
c. $405,007-123.3=$ ?
d. $55.5+66.66-77.777=$ ?
9. Compute and express each answer with the proper number of significant figures, rounding as necessary.
a. $56.7 \times 66.99=$ ?
b. $1.000 \div 77=$ ?
c. $1.000 \div 77.0=$ ?
d. $6.022 \times 1.89=$ ?
10. Compute and express each answer with the proper number of significant figures, rounding as necessary.
a. $0.000440 \times 17.22=$ ?
b. $203,000 \div 0.044=$ ?
c. $67 \times 85.0 \times 0.0028=$ ?
d. $999,999 \div 3,310=$ ?
11. a. Write the number 87,449 in scientific notation with four significant figures.
b. Write the number 0.000066600 in scientific notation with five significant figures.
12. a. Write the number $306,000,000$ in scientific notation to the proper number of significant figures.
b. Write the number 0.0000558 in scientific notation with two significant figures.
13. Perform each calculation and limit each answer to three significant figures.
a. $67,883 \times 0.004321=$ ?
b. $\left(9.67 \times 10^{3}\right) \times 0.0055087=$ ?
14. Perform each calculation and limit each answer to four significant figures.
a. $18,900 \times 76.33 \div 0.00336=$ ?
b. $0.77604 \div 76,003 \times 8.888=$ ?

A N S W ERS
3. a. two
b. three
c. two
d. four
5. a. five
b. seven
c. five
d. four
7. a. 59.4
b. 1.011
c. 13.2
d. 88.2
9. a. $3.80 \times 10^{3}$
b. 0.013
c. 0.0130
d. 11.4
11. a. $8.745 \times 10^{4}$
b. $6.6600 \times 10^{-5}$
13. a. 293
b. 53.3

## 4. CONVERTING UNITS

## LEARNING O B JECTIVE

1. Convert from one unit to another unit of the same type.

In Section 2, we showed some examples of how to replace initial units with other units of the same type to get a numerical value that is easier to comprehend. In this section, we will formalize the process.

Consider a simple example: how many feet are there in 4 yards? Most people will almost automatically answer that there are 12 feet in 4 yards. How did you make this determination? Well, if there are 3 feet in 1 yard and there are 4 yards, then there are $4 \times 3=12$ feet in 4 yards.

This is correct, of course, but it is informal. Let us formalize it in a way that can be applied more generally. We know that 1 yard ( yd ) equals 3 feet ( ft ):

$$
1 \mathrm{yd}=3 \mathrm{ft}
$$

In math, this expression is called an equality. The rules of algebra say that you can change (i.e., multiply or divide or add or subtract) the equality (as long as you don't divide by zero) and the new expression will still be an equality. For example, if we divide both sides by 2 , we get

$$
\frac{1}{2} \mathrm{yd}=\frac{3}{2} \mathrm{ft}
$$

We see that one-half of a yard equals $3 / 2$, or one and a half, feet-something we also know to be true, so the above equation is still an equality. Going back to the original equality, suppose we divide both sides of the equation by 1 yard (number and unit):

$$
\frac{1 \mathrm{yd}}{1 \mathrm{yd}}=\frac{3 \mathrm{ft}}{1 \mathrm{yd}}
$$

The expression is still an equality, by the rules of algebra. The left fraction equals 1 . It has the same quantity in the numerator and the denominator, so it must equal 1 . The quantities in the numerator and denominator cancel, both the number and the unit:

$$
\frac{z y_{d}^{d}}{\frac{y}{x d}}=\frac{3 \mathrm{ft}}{1 \mathrm{yd}}
$$

When everything cancels in a fraction, the fraction reduces to 1 :

$$
1=\frac{3 \mathrm{ft}}{1 \mathrm{yd}}
$$

We have an expression, $\frac{3 \mathrm{ft}}{1 \mathrm{yd}}$, that equals 1 . This is a strange way to write 1 , but it makes sense: 3 ft equal 1 yd , so the quantities in the numerator and denominator are the same quantity, just expressed with different units. The expression $\frac{3 \mathrm{ft}}{1 \mathrm{yd}}$ is called a conversion factor, and it is used to formally change the unit of a quantity into another unit. (The process of converting units in such a formal fashion is sometimes called dimensional analysis or the factor label method.)

To see how this happens, let us start with the original quantity:

Now let us multiply this quantity by 1 . When you multiply anything by 1 , you don't change the value of the quantity. Rather than multiplying by just 1 , let us write 1 as $\frac{3 \mathrm{ft}}{1 \mathrm{yd}}$ :

$$
4 \mathrm{yd} \times \frac{3 \mathrm{ft}}{1 \mathrm{yd}}
$$

The 4 yd term can be thought of as $\frac{4 \mathrm{yd}}{1}$; that is, it can be thought of as a fraction with 1 in the denominator. We are essentially multiplying fractions. If the same thing appears in the numerator and denominator of a fraction, they cancel. In this case, what cancels is the unit yard:

$$
4 y d \times \frac{3 \mathrm{ft}}{1 \not \partial \mathrm{~d}}
$$

That is all that we can cancel. Now, multiply and divide all the numbers to get the final answer:

$$
\frac{4 \times 3 \mathrm{ft}}{1}=\frac{12 \mathrm{ft}}{1}=12 \mathrm{ft}
$$

Again, we get an answer of 12 ft , just as we did originally. But in this case, we used a more formal procedure that is applicable to a variety of problems.

How many millimeters are in 14.66 m ? To answer this, we need to construct a conversion factor between millimeters and meters and apply it correctly to the original quantity. We start with the definition of a millimeter, which is

$$
1 \mathrm{~mm}=1 / 1,000 \mathrm{~m}
$$

The $1 / 1,000$ is what the prefix milli- means. Most people are more comfortable working without fractions, so we will rewrite this equation by bringing the 1,000 into the numerator of the other side of the equation:

$$
1,000 \mathrm{~mm}=1 \mathrm{~m}
$$

Now we construct a conversion factor by dividing one quantity into both sides. But now a question arises: which quantity do we divide by? It turns out that we have two choices, and the two choices will give us different conversion factors, both of which equal 1:

$$
\begin{gathered}
\frac{1,000 \mathrm{~mm}}{1,000 \mathrm{~mm}}=\frac{1 \mathrm{~m}}{1,000 \mathrm{~mm}} \quad \text { or } \quad \frac{1,000 \mathrm{~mm}}{1 \mathrm{~m}}=\frac{1 \mathrm{~m}}{1 \mathrm{~m}} \\
1=\frac{1 \mathrm{~m}}{1,000 \mathrm{~mm}} \quad \text { or } \quad \frac{1,000 \mathrm{~mm}}{1 \mathrm{~m}}=1
\end{gathered}
$$

Which conversion factor do we use? The answer is based on what unit you want to get rid of in your initial quantity. The original unit of our quantity is meters, which we want to convert to millimeters. Because the original unit is assumed to be in the numerator, to get rid of it, we want the meter unit in the denominator; then they will cancel. Therefore, we will use the second conversion factor. Canceling units and performing the mathematics, we get

$$
14.66 \not \mu \times \frac{1,000 \mathrm{~mm}}{1 \not \mathrm{M}}=14,660 \mathrm{~mm}
$$

Note how m cancels, leaving mm , which is the unit of interest.
The ability to construct and apply proper conversion factors is a very powerful mathematical technique in chemistry. You need to master this technique if you are going to be successful in this and future courses.

## EXAMPLE 7

1. Convert 35.9 kL to liters.
2. Convert 555 nm to meters.

## Solution

1. We will use the fact that $1 \mathrm{~kL}=1,000 \mathrm{~L}$. Of the two conversion factors that can be defined, the one that will $1,000 \mathrm{~L}$
work is 1 kL . Applying this conversion factor, we get

$$
35.9 \mathrm{KL} \times \frac{1,000 \mathrm{~L}}{1 \mathrm{LL}}=35,900 \mathrm{~L}
$$

2. We will use the fact that $1 \mathrm{~nm}=1 / 1,000,000,000 \mathrm{~m}$, which we will rewrite as $1,000,000,000 \mathrm{~nm}=1 \mathrm{~m}$, or $10^{9} \mathrm{~nm}=1 \mathrm{~m}$. Of the two possible conversion factors, the appropriate one has the nm unit in the denominator: $\frac{1 \mathrm{~m}}{10^{9} \mathrm{~nm}}$. Applying this conversion factor, we get

$$
555 \mathrm{n} \text { n } \times \frac{1 \mathrm{~m}}{10^{9} \mathrm{n} \pi}=0.000000555 \mathrm{~m}=5.55 \times 10^{-7} \mathrm{~m}
$$

In the final step, we expressed the answer in scientific notation.

## Test Yourself

1. Convert $67.08 \mu \mathrm{~L}$ to liters.
2. Convert 56.8 m to kilometers.

Answers

1. $6.708 \times 10^{-5} \mathrm{~L}$
2. $5.68 \times 10^{-2} \mathrm{~km}$

What if we have a derived unit that is the product of more than one unit, such as $\mathrm{m}^{2}$ ? Suppose we want to convert square meters to square centimeters? The key is to remember that $\mathrm{m}^{2}$ means $\mathrm{m} \times \mathrm{m}$, which means we have two meter units in our derived unit. That means we have to include two conversion factors, one for each unit. For example, to convert $17.6 \mathrm{~m}^{2}$ to square centimeters, we perform the conversion as follows:

$$
17.6 \mathrm{~m}^{2}=17.6(\not \boxed{ } \times \not 1 \times 1) \times \frac{100 \mathrm{~cm}}{1 \not \mathrm{~m}_{1}} \times \frac{100 \mathrm{~cm}}{1 \not \mathrm{~m}_{1}}=176,000 \mathrm{~cm} \times \mathrm{cm}=1.76 \times 10^{5} \mathrm{~cm}^{2}
$$

## EXAMPLE 8

How many cubic centimeters are in $0.883 \mathrm{~m}^{3}$ ?

## Solution

With an exponent of 3, we have three length units, so by extension we need to use three conversion factors between meters and centimeters. Thus, we have

You should demonstrate to yourself that the three meter units do indeed cancel.

## Test Yourself

How many cubic millimeters are present in $0.0923 \mathrm{~m}^{3}$ ?
Answer
$9.23 \times 10^{7} \mathrm{~mm}^{3}$

Suppose the unit you want to convert is in the denominator of a derived unit; what then? Then, in the conversion factor, the unit you want to remove must be in the numerator. This will cancel with the original unit in the denominator and introduce a new unit in the denominator. The following example illustrates this situation.

## EXAMPLE 9

Convert $88.4 \mathrm{~m} / \mathrm{min}$ to meters/second.

## Solution

We want to change the unit in the denominator from minutes to seconds. Because there are 60 seconds in 1 minute ( $60 \mathrm{~s}=1 \mathrm{~min}$ ), we construct a conversion factor so that the unit we want to remove, minutes, is in the numerator: $\frac{1 \mathrm{~min}}{60 \mathrm{~s}}$. Apply and perform the math:

$$
\frac{88.4 \mathrm{~m}}{\text { min }} \times \frac{1 \text { min }}{60 \mathrm{~s}}=1.47 \mathrm{~m} / \mathrm{s}
$$

Notice how the 88.4 automatically goes in the numerator. That's because any number can be thought of as being in the numerator of a fraction divided by 1 .

## Test Yourself

Convert $0.203 \mathrm{~m} / \mathrm{min}$ to meters $/$ second
Answer
$0.00338 \mathrm{~m} / \mathrm{s}$ or $3.38 \times 10^{-3} \mathrm{~m} / \mathrm{s}$
How Fast Is Fast?
A common garden snail moves at a rate of about $0.2 \mathrm{~m} / \mathrm{min}$, which is about $0.003 \mathrm{~m} / \mathrm{s}$, which is $3 \mathrm{~mm} / \mathrm{s}$ !

© Thinkstock

Sometimes there will be a need to convert from one unit with one numerical prefix to another unit with a different numerical prefix. How do we handle those conversions? Well, you could memorize the conversion factors that interrelate all numerical prefixes. Or you can go the easier route: first convert the quantity to the base unit, the unit with no numerical prefix, using the definition of the original prefix. Then convert the quantity in the base unit to the desired unit using the definition of the second prefix. You can do the conversion in two separate steps or as one long algebraic step. For example, to convert 2.77 kg to milligrams:

$$
\begin{gathered}
2.77 \mathrm{~kg} \times \frac{1,000 \mathrm{~g}}{1 \mathrm{~kg}}=2,770 \mathrm{~g} \quad(\text { convert to the base unit of grams) } \\
2,770 \not g \times \frac{1,000 \mathrm{mg}}{1 \not g}=2,770,000 \mathrm{mg}=2.77 \times 10^{6} \mathrm{mg} \quad \text { (convert to desired unit) }
\end{gathered}
$$

Alternatively, it can be done in a single multistep process:

$$
2.77 \mathrm{~kg} \times \frac{1,000 \mathrm{~g}}{1 \mathrm{~kg}} \times \frac{1,000 \mathrm{mg}}{1 / \mathrm{g}}=2,770,000 \mathrm{mg}=2.77 \times 10^{6} \mathrm{mg}
$$

You get the same answer either way.

## exact number

A number from a defined relationship that technically has an infinite number of significant figures.

## E X A M P L E 10

How many nanoseconds are in $368.09 \mu s$ ?

## Solution

You can either do this as a one-step conversion from microseconds to nanoseconds or convert to the base unit first and then to the final desired unit. We will use the second method here, showing the two steps in a single line. Using the definitions of the prefixes micro- and nano-,

$$
368.09 \nprec \mathrm{~s} \times \frac{1 \not \hbar}{1,000,000 \nprec \mathrm{~s}} \times \frac{1,000,000,000 \mathrm{~ns}}{1 \not \hbar}=368,090 \mathrm{~ns}=3.6809 \times 10^{5} \mathrm{~ns}
$$

## Test Yourself

How many milliliters are in 607.8 kL?
Answer
$6.078 \times 10^{8} \mathrm{~mL}$

When considering the significant figures of a final numerical answer in a conversion, there is one important case where a number does not impact the number of significant figures in a final answer-the so-called exact number. An exact number is a number from a defined relationship, not a measured one. For example, the prefix kilo- means 1,000 -exactly 1,000 , no more or no less. Thus, in constructing the conversion factor

$$
\frac{1,000 \mathrm{~g}}{1 \mathrm{~kg}}
$$

neither the 1,000 nor the 1 enter into our consideration of significant figures. The numbers in the numerator and denominator are defined exactly by what the prefix kilo-means. Another way of thinking about it is that these numbers can be thought of as having an infinite number of significant figures, such as

$$
\frac{1,000.0000000000 \ldots \mathrm{~g}}{1.0000000000 \ldots \mathrm{~kg}}
$$

The other numbers in the calculation will determine the number of significant figures in the final answer.

## E X A M P LE 11

A rectangular plot in a garden has the dimensions 36.7 cm by 128.8 cm . What is the area of the garden plot in square meters? Express your answer in the proper number of significant figures.

## Solution

Area is defined as the product of the two dimensions, which we then have to convert to square meters and express our final answer to the correct number of significant figures, which in this case will be three.

$$
36.7 \mathrm{cn} \times 128.8 \mathrm{cn} \times \frac{1 \mathrm{~m}}{100 \mathrm{~cm}} \times \frac{1 \mathrm{~m}}{100 \mathrm{~cm}}=0.472696 \mathrm{~m}^{2}=0.473 \mathrm{~m}^{2}
$$

The 1 and 100 in the conversion factors do not affect the determination of significant figures because they are exact numbers, defined by the centi- prefix.

## Test Yourself

What is the volume of a block in cubic meters whose dimensions are $2.1 \mathrm{~cm} \times 34.0 \mathrm{~cm} \times 118 \mathrm{~cm}$ ?
Answer
$0.0084 \mathrm{~m}^{3}$

## Chemistry Is Everywhere: The Gimli Glider

On July 23, 1983, an Air Canada Boeing 767 jet had to glide to an emergency landing at Gimli Industrial Park Airport in Gimli, Manitoba, because it unexpectedly ran out of fuel during flight. There was no loss of life in the course of the emergency landing, only some minor injuries associated in part with the evacuation of the craft after landing. For the remainder of its operational life (the plane was retired in 2008), the aircraft was nicknamed "the Gimli Glider."

The Gimli Glider is the Boeing 767 that ran out of fuel and glided to safety at Gimli Airport. The aircraft ran out of fuel because of confusion over the units used to express the amount of fuel.


Source: Photo courtesy of Will F., http://commons.wikimedia.org/wiki/File:Gimli_Glider_today.jpg.
The 767 took off from Montreal on its way to Ottawa, ultimately heading for Edmonton, Canada. About halfway through the flight, all the engines on the plane began to shut down because of a lack of fuel. When the final engine cut off, all electricity (which was generated by the engines) was lost; the plane became, essentially, a powerless glider. Captain Robert Pearson was an experienced glider pilot, although he had never flown a glider the size of a 767. First Officer Maurice Quintal quickly determined that the aircraft would not be able make it to Winnipeg, the next large airport. He suggested his old Royal Air Force base at Gimli Station, one of whose runways was still being used as a community airport. Between the efforts of the pilots and the flight crew, they managed to get the airplane safely on the ground (although with buckled landing gear) and all passengers off safely.

What happened? At the time, Canada was transitioning from the older English system to the metric system. The Boeing 767s were the first aircraft whose gauges were calibrated in the metric system of units (liters and kilograms) rather than the English system of units (gallons and pounds). Thus, when the fuel gauge read 22,300 , the gauge meant kilograms, but the ground crew mistakenly fueled the plane with 22,300 pounds of fuel. This ended up being just less than half of the fuel needed to make the trip, causing the engines to quit about halfway to Ottawa. Quick thinking and extraordinary skill saved the lives of 61 passengers and 8 crew members-an incident that would not have occurred if people were watching their units.

## K E Y TAKEAW AYS

- Units can be converted to other units using the proper conversion factors.
- Conversion factors are constructed from equalities that relate two different units.
- Conversions can be a single step or multistep.
- Unit conversion is a powerful mathematical technique in chemistry that must be mastered.
- Exact numbers do not affect the determination of significant figures.


## EXERCISES

1. Write the two conversion factors that exist between the two given units.
a. milliliters and liters
b. microseconds and seconds
c. kilometers and meters
2. Write the two conversion factors that exist between the two given units.
a. kilograms and grams
b. milliseconds and seconds
c. centimeters and meters
3. Perform the following conversions.
a. 5.4 km to meters
b. 0.665 m to millimeters
c. 0.665 m to kilometers
4. Perform the following conversions.
a. 90.6 mL to liters
b. 0.00066 ML to liters
c. 750 L to kiloliters
5. Perform the following conversions.
a. $17.8 \mu \mathrm{~g}$ to grams
b. $7.22 \times 10^{2} \mathrm{~kg}$ to grams
c. 0.00118 g to nanograms
6. Perform the following conversions.
a. 833 ns to seconds
b. 5.809 s to milliseconds
c. $2.77 \times 10^{6}$ s to megaseconds
7. Perform the following conversions.
a. $9.44 \mathrm{~m}^{2}$ to square centimeters
b. $3.44 \times 10^{8} \mathrm{~mm}^{3}$ to cubic meters
8. Perform the following conversions.
a. $0.00444 \mathrm{~cm}^{3}$ to cubic meters
b. $8.11 \times 10^{2} \mathrm{~m}^{2}$ to square nanometers
9. Why would it be inappropriate to convert square centimeters to cubic meters?
10. Why would it be inappropriate to convert from cubic meters to cubic seconds?
11. Perform the following conversions.
a. $45.0 \mathrm{~m} / \mathrm{min}$ to meters $/$ second
b. $0.000444 \mathrm{~m} / \mathrm{s}$ to micrometers $/$ second
c. $60.0 \mathrm{~km} / \mathrm{h}$ to kilometers $/ \mathrm{second}$
12. Perform the following conversions.
a. $3.4 \times 10^{2} \mathrm{~cm} / \mathrm{s}$ to centimeters/minute
b. $26.6 \mathrm{~mm} / \mathrm{s}$ to millimeters/hour
c. $13.7 \mathrm{~kg} / \mathrm{L}$ to kilograms/milliliters
13. Perform the following conversions.
a. 0.674 kL to milliliters
b. $2.81 \times 10^{12} \mathrm{~mm}$ to kilometers
c. 94.5 kg to milligrams
14. Perform the following conversions.
a. $6.79 \times 10^{-6} \mathrm{~kg}$ to micrograms
b. 1.22 mL to kiloliters
c. $9.508 \times 10^{-9} \mathrm{ks}$ to milliseconds
15. Perform the following conversions.
a. $6.77 \times 10^{14} \mathrm{~ms}$ to kiloseconds
b. $34,550,000 \mathrm{~cm}$ to kilometers
16. Perform the following conversions.
a. $4.701 \times 10^{15} \mathrm{~mL}$ to kiloliters
b. $8.022 \times 10^{-11} \mathrm{ks}$ to microseconds
17. Perform the following conversions. Note that you will have to convert units in both the numerator and the denominator.
a. $88 \mathrm{ft} / \mathrm{s}$ to miles/hour (Hint: use $5,280 \mathrm{ft}$ $=1 \mathrm{mi}$.)
b. $0.00667 \mathrm{~km} / \mathrm{h}$ to meters $/$ second
18. Perform the following conversions. Note that you will have to convert units in both the numerator and the denominator.
a. $3.88 \times 10^{2} \mathrm{~mm} / \mathrm{s}$ to kilometers/hour
b. $1.004 \mathrm{~kg} / \mathrm{L}$ to grams $/$ milliliter
19. What is the area in square millimeters of a rectangle whose sides are $2.44 \mathrm{~cm} \times 6.077$ cm ? Express the answer to the proper number of significant figures.
20. What is the volume in cubic centimeters of a cube with sides of 0.774 m ? Express the answer to the proper number of significant figures.
21. The formula for the area of a triangle is $1 / 2$ $\times$ base $\times$ height. What is the area of a triangle in square centimeters if its base is 1.007 m and its height is 0.665 m ? Express the answer to the proper number of significant figures.
22. The formula for the area of a triangle is $1 / 2$ $\times$ base $\times$ height. What is the area of a triangle in square meters if its base is 166 mm and its height is 930.0 mm ? Express the answer to the proper number of significant figures.

## A N S W ERS

1. a. $\frac{1,000 \mathrm{~mL}}{1 \mathrm{~L}}$ and $\frac{1 \mathrm{~L}}{1,000 \mathrm{~mL}}$
b. $\frac{1,000,000 \mu \mathrm{~s}}{1 \mathrm{~s}}$ and $\frac{1 \mathrm{~s}}{1,000,000 \mu \mathrm{~s}}$
c. $\frac{1,000 \mathrm{~m}}{1 \mathrm{~km}}$ and $\frac{1 \mathrm{~km}}{1,000 \mathrm{~m}}$
2. a. $5,400 \mathrm{~m}$
b. 665 mm
c. $6.65 \times 10^{-4} \mathrm{~km}$
3. a. $1.78 \times 10^{-5} \mathrm{~g}$
b. $7.22 \times 10^{5} \mathrm{~g}$
c. $1.18 \times 10^{6} \mathrm{ng}$
4. a. $94,400 \mathrm{~cm}^{2}$
b. $0.344 \mathrm{~m}^{3}$
5. One is a unit of area, and the other is a unit of volume.
6. a. $0.75 \mathrm{~m} / \mathrm{s}$
b. $444 \mu \mathrm{~m} / \mathrm{s}$
c. $1.666 \times 10^{-2} \mathrm{~km} / \mathrm{s}$
7. a. $674,000 \mathrm{~mL}$
b. $2.81 \times 10^{6} \mathrm{~km}$
c. $9.45 \times 10^{7} \mathrm{mg}$
8. a. $6.77 \times 10^{8} \mathrm{ks}$
b. 345.5 km
9. a. $6.0 \times 10^{1} \mathrm{mi} / \mathrm{h}$
b. $0.00185 \mathrm{~m} / \mathrm{s}$
10. $1.48 \times 10^{3} \mathrm{~mm}^{2}$
11. $3.35 \times 10^{3} \mathrm{~cm}^{2}$

## 5. OTHER UNITS: TEMPERATURE AND DENSITY

## LEARNING OBJECTIVES

1. Learn about the various temperature scales that are commonly used in chemistry.
2. Define density and use it as a conversion factor.

There are other units in chemistry that are important, and we will cover others in the course of the entire book. One of the fundamental quantities in science is temperature. Temperature is a measure of the average amount of energy of motion, or kinetic energy, a system contains. Temperatures are expressed using scales that use units called degrees, and there are several temperature scales in use. In the United States, the commonly used temperature scale is the Fahrenheit scale (symbolized by ${ }^{\circ} \mathrm{F}$ and spoken as "degrees Fahrenheit"). On this scale, the freezing point of liquid water (the temperature at which liquid water turns to solid ice) is $32^{\circ} \mathrm{F}$, and the boiling point of water (the temperature at which liquid water turns to steam) is $212^{\circ} \mathrm{F}$.

Science also uses other scales to express temperature. The Celsius scale (symbolized by ${ }^{\circ} \mathrm{C}$ and spoken as "degrees Celsius") is a temperature scale where $0^{\circ} \mathrm{C}$ is the freezing point of water and $100^{\circ} \mathrm{C}$ is the boiling point of water; the scale is divided into 100 divisions between these two landmarks and extended higher and lower. By comparing the Fahrenheit and Celsius scales, a conversion between the two scales can be determined:

$$
\begin{aligned}
& { }^{\circ} \mathrm{C}=\left({ }^{\circ} \mathrm{F}-32\right) \times \frac{5}{9} \\
& { }^{\circ} \mathrm{F}=\left({ }^{\circ} \mathrm{C} \times \frac{9}{5}\right)+32
\end{aligned}
$$

Using these formulas, we can convert from one temperature scale to another. The number 32 in the formulas is exact and does not count in significant figure determination.

## temperature

A measure of the average amount of kinetic energy a system contains.

## degree

The unit of temperature scales.

## kelvin

The fundamental unit of temperature in SI.

## absolute zero

The minimum possible temperature, labeled 0 K (zero kelvins)

## E X A M P L E 12

1. What is $98.6^{\circ} \mathrm{F}$ in degrees Celsius?
2. What is $25.0^{\circ} \mathrm{C}$ in degrees Fahrenheit?

## Solution

1. Using the first formula from above, we have

$$
{ }^{\circ} \mathrm{C}=(98.6-32) \times \frac{5}{9}=66.6 \times \frac{5}{9}=37.0^{\circ} \mathrm{C}
$$

2. Using the second formula from above, we have

$$
{ }^{\circ} \mathrm{F}=\left(25.0 \times \frac{9}{5}\right)+32=45.0+32=77.0^{\circ} \mathrm{F}
$$

## Test Yourself

1. Convert $0^{\circ} \mathrm{F}$ to degrees Celsius.
2. Convert $212^{\circ} \mathrm{C}$ to degrees Fahrenheit.

Answers

1. $-17.8^{\circ} \mathrm{C}$
2. $414^{\circ} \mathrm{F}$

The fundamental unit of temperature (another fundamental unit of science, bringing us to four) in SI is the kelvin (K). The Kelvin temperature scale (note that the name of the scale capitalizes the word Kelvin, but the unit itself is lowercase) uses degrees that are the same size as the Celsius degree, but the numerical scale is shifted up by 273.15 units. That is, the conversion between the Kelvin and Celsius scales is as follows:

$$
\begin{aligned}
& \mathrm{K}={ }^{\circ} \mathrm{C}+273.15 \\
& { }^{\circ} \mathrm{C}=\mathrm{K}-273.15
\end{aligned}
$$

For most purposes, it is acceptable to use 273 instead of 273.15 . Note that the Kelvin scale does not use the word degrees; a temperature of 295 K is spoken of as "two hundred ninety-five kelvins" and not "two hundred ninety-five degrees Kelvin."

The reason that the Kelvin scale is defined this way is because there exists a minimum possible temperature called absolute zero. The Kelvin temperature scale is set so that 0 K is absolute zero, and temperature is counted upward from there. Normal room temperature is about 295 K , as seen in the following example.

## E X A M P L E 13

If normal room temperature is $72.0^{\circ} \mathrm{F}$, what is room temperature in degrees Celsius and kelvins?

## Solution

First, we use the formula to determine the temperature in degrees Celsius:

$$
{ }^{\circ} \mathrm{C}=(72.0-32) \times \frac{5}{9}=40.0 \times \frac{5}{9}=22.2^{\circ} \mathrm{C}
$$

Then we use the appropriate formula above to determine the temperature in the Kelvin scale:

$$
\mathrm{K}=22.2^{\circ} \mathrm{C}+273.15=295.4 \mathrm{~K}
$$

So, room temperature is about 295 K .

## Test Yourself

What is $98.6^{\circ} \mathrm{F}$ on the Kelvin scale?
Answer
310.2 K

Figure 2.9 compares the three temperature scales. Note that science uses the Celsius and Kelvin scales almost exclusively; virtually no practicing chemist expresses laboratory-measured temperatures with the Fahrenheit scale. (In fact, the United States is one of the few countries in the world that still uses the Fahrenheit scale on a daily basis. The other two countries are Liberia and Myanmar [formerly Burma]. People driving near the borders of Canada or Mexico may pick up local radio stations on the other side of the border that express the daily weather in degrees Celsius, so don't get confused by their weather reports.)

FIGURE 2.9 Fahrenheit, Celsius, and Kelvin Temperatures
A comparison of the three temperature scales.


Density is a physical property that is defined as a substance's mass divided by its volume:

$$
\text { density }=\frac{\text { mass }}{\text { volume }} \quad \text { or } d=\frac{m}{V}
$$

Density is usually a measured property of a substance, so its numerical value affects the significant figures in a calculation. Notice that density is defined in terms of two dissimilar units, mass and volume. That means that density overall has derived units, just like velocity. Common units for density include $\mathrm{g} / \mathrm{mL}, \mathrm{g} / \mathrm{cm}^{3}, \mathrm{~g} / \mathrm{L}, \mathrm{kg} / \mathrm{L}$, and even $\mathrm{kg} / \mathrm{m}^{3}$. Densities for some common substances are listed in Table 2.2.

## density

A physical property defined as a substance's mass divided by its volume.

TABLE 2.2 Densities of Some Common Substances

| Substance | Density $\left(\mathrm{g} / \mathrm{mL}\right.$ or $\left.\mathrm{g} / \mathrm{cm}^{3}\right)$ |
| :--- | :--- |
| water | 1.0 |
| gold | 19.3 |
| mercury | 13.6 |
| air | 0.0012 |
| cork | $0.22-0.26$ |
| aluminum | 2.7 |
| iron | 7.87 |

Because of how it is defined, density can act as a conversion factor for switching between units of mass and volume. For example, suppose you have a sample of aluminum that has a volume of $7.88 \mathrm{~cm}^{3}$. How can you determine what mass of aluminum you have without measuring it? You can use the volume to calculate it. If you multiply the given volume by the known density (from Table 2.2), the volume units will cancel and leave you with mass units, telling you the mass of the sample:

$$
7.88 \mathrm{~cm}^{3} \times \frac{2.7 \mathrm{~g}}{\mathrm{ch}^{3}}=21 \mathrm{~g} \text { of aluminum }
$$

where we have limited our answer to two significant figures.

## EXAMPLE 14

What is the mass of 44.6 mL of mercury?

## Solution

Use the density from Table 2.2 as a conversion factor to go from volume to mass:

$$
44.6 \mathrm{~mL} \times \frac{13.6 \mathrm{~g}}{\underline{\mathrm{DL}}}=607 \mathrm{~g}
$$

The mass of the mercury is 607 g .
Test Yourself
What is the mass of $25.0 \mathrm{~cm}^{3}$ of iron?
Answer
197 g

Density can also be used as a conversion factor to convert mass to volume-but care must be taken. We have already demonstrated that the number that goes with density normally goes in the numerator when density is written as a fraction. Take the density of gold, for example:

$$
d=19.3 \mathrm{~g} / \mathrm{mL}=\frac{19.3 \mathrm{~g}}{\mathrm{~mL}}
$$

Although this was not previously pointed out, it can be assumed that there is a 1 in the denominator:

$$
d=19.3 \mathrm{~g} / \mathrm{mL}=\frac{19.3 \mathrm{~g}}{1 \mathrm{~mL}}
$$

That is, the density value tells us that we have 19.3 grams for every 1 milliliter of volume, and the 1 is an exact number. When we want to use density to convert from mass to volume, the numerator and denominator of density need to be switched-that is, we must take the reciprocal of the density. In so doing, we move not only the units but also the numbers:

$$
\frac{1}{d}=\frac{1 \mathrm{~mL}}{19.3 \mathrm{~g}}
$$

This reciprocal density is still a useful conversion factor, but now the mass unit will cancel and the volume unit will be introduced. Thus, if we want to know the volume of 45.9 g of gold, we would set up the conversion as follows:

$$
45.9 \not \mathrm{~g} \times \frac{1 \mathrm{~mL}}{19.3 / \mathrm{g}}=2.38 \mathrm{~mL}
$$

Note how the mass units cancel, leaving the volume unit, which is what we're looking for.

## EXAMPLE 15

A cork stopper from a bottle of wine has a mass of 3.78 g . If the density of cork is $0.22 \mathrm{~g} / \mathrm{cm}^{3}$, what is the volume of the cork?

## Solution

To use density as a conversion factor, we need to take the reciprocal so that the mass unit of density is in the denominator. Taking the reciprocal, we find

$$
\frac{1}{d}=\frac{1 \mathrm{~cm}^{3}}{0.22 \mathrm{~g}}
$$

We can use this expression as the conversion factor. So

$$
3.78 \not g \times \frac{1 \mathrm{~cm}^{3}}{0.22 \not \not \mathrm{~g}}=17.2 \mathrm{~cm}^{3}
$$

## Test Yourself

What is the volume of 3.78 g of gold?
Answer
$0.196 \mathrm{~cm}^{3}$

Care must be used with density as a conversion factor. Make sure the mass units are the same, or the volume units are the same, before using density to convert to a different unit. Often, the unit of the given quantity must be first converted to the appropriate unit before applying density as a conversion factor.

## Food and Drink App: Cooking Temperatures

Because degrees Fahrenheit is the common temperature scale in the United States, kitchen appliances, such as ovens, are calibrated in that scale. A cool oven may be only $150^{\circ} \mathrm{F}$, while a cake may be baked at $350^{\circ} \mathrm{F}$ and a chicken roasted at $400^{\circ} \mathrm{F}$. The broil setting on many ovens is $500^{\circ} \mathrm{F}$, which is typically the highest temperature setting on a household oven.
People who live at high altitudes, typically $2,000 \mathrm{ft}$ above sea level or higher, are sometimes urged to use slightly different cooking instructions on some products, such as cakes and bread, because water boils at a lower temperature the higher in altitude you go, meaning that foods cook slower. For example, in Cleveland water typically boils at $212^{\circ} \mathrm{F}\left(100^{\circ} \mathrm{C}\right)$, but in Denver, the Mile-High City, water boils at about $200^{\circ} \mathrm{F}\left(93.3^{\circ} \mathrm{C}\right)$, which can significantly lengthen cooking times. Good cooks need to be aware of this.
At the other end is pressure cooking. A pressure cooker is a closed vessel that allows steam to build up additional pressure, which increases the temperature at which water boils. A good pressure cooker can get to temperatures as high as $252^{\circ} \mathrm{F}\left(122^{\circ} \mathrm{C}\right)$; at these temperatures, food cooks much faster than it normally would. Great care must be used with pressure cookers because of the high pressure and high temperature. (When a pressure cooker is used to sterilize medical instruments, it is called an autoclave.)

Other countries use the Celsius scale for everyday purposes. Therefore, oven dials in their kitchens are marked in degrees Celsius. It can be confusing for US cooks to use ovens abroad-a $425^{\circ}$ F oven in the United States is equivalent to a $220^{\circ} \mathrm{C}$ oven in other countries. These days, many oven thermometers are marked with both temperature scales.

This oven thermometer shows both Fahrenheit (outer scale) and Celsius (inner scale) temperatures. Recipes for cooking food in an oven can use very different numbers, depending on the country you're in.

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## K EY TAKEAWAYS

- Chemistry uses the Celsius and Kelvin scales to express temperatures.
- A temperature on the Kelvin scale is the Celsius temperature plus 273.15.
- The minimum possible temperature is absolute zero and is assigned 0 K on the Kelvin scale.
- Density relates a substance's mass and volume.
- Density can be used to calculate volume from a given mass or mass from a given volume.


## EXERCISES

1. Perform the following conversions.
a. $255^{\circ} \mathrm{F}$ to degrees Celsius
b. $-255^{\circ} \mathrm{F}$ to degrees Celsius
c. $50.0^{\circ} \mathrm{C}$ to degrees Fahrenheit
d. $-50.0^{\circ} \mathrm{C}$ to degrees Fahrenheit
2. Perform the following conversions.
a. $1,065^{\circ} \mathrm{C}$ to degrees Fahrenheit
b. $-222^{\circ} \mathrm{C}$ to degrees Fahrenheit
c. $400.0^{\circ} \mathrm{F}$ to degrees Celsius
d. $200.0^{\circ} \mathrm{F}$ to degrees Celsius
3. Perform the following conversions.
a. $100.0^{\circ} \mathrm{C}$ to kelvins
b. $-100.0^{\circ} \mathrm{C}$ to kelvins
c. 100 K to degrees Celsius
d. 300 K to degrees Celsius
4. Perform the following conversions.
a. $1,000.0 \mathrm{~K}$ to degrees Celsius
b. 50.0 K to degrees Celsius
c. $37.0^{\circ} \mathrm{C}$ to kelvins
d. $-37.0^{\circ} \mathrm{C}$ to kelvins
5. Convert 0 K to degrees Celsius. What is the significance of the temperature in degrees Celsius?
6. Convert 0 K to degrees Fahrenheit. What is the significance of the temperature in degrees Fahrenheit?
7. The hottest temperature ever recorded on the surface of the earth was $136^{\circ} \mathrm{F}$ in Libya in 1922. What is the temperature in degrees Celsius and in kelvins?
8. The coldest temperature ever recorded on the surface of the earth was $-128.6^{\circ} \mathrm{F}$ in Vostok, Antarctica, in 1983. What is the temperature in degrees Celsius and in kelvins?
9. Give at least three possible units for density.
10. What are the units when density is inverted? Give three examples.
11. A sample of iron has a volume of $48.2 \mathrm{~cm}^{3}$. What is its mass?
12. A sample of air has a volume of $1,015 \mathrm{~mL}$. What is its mass?
13. The volume of hydrogen used by the Hindenburg, the German airship that exploded in New Jersey in 1937, was 2.000 $\times 10^{8} \mathrm{~L}$. If hydrogen gas has a density of $0.0899 \mathrm{~g} / \mathrm{L}$, what mass of hydrogen was used by the airship?
14. The volume of an Olympic-sized swimming pool is $2.50 \times 10^{9} \mathrm{~cm}^{3}$. If the pool is filled with alcohol ( $d=0.789$ $\mathrm{g} / \mathrm{cm}^{3}$ ), what mass of alcohol is in the pool?
15. A typical engagement ring has $0.77 \mathrm{~cm}^{3}$ of gold. What mass of gold is present?
16. A typical mercury thermometer has 0.039 mL of mercury in it. What mass of mercury is in the thermometer?
17. What is the volume of 100.0 g of lead if lead has a density of $11.34 \mathrm{~g} / \mathrm{cm}^{3}$ ?
18. What is the volume of 255.0 g of uranium if uranium has a density of $19.05 \mathrm{~g} / \mathrm{cm}^{3}$ ?
19. What is the volume in liters of 222 g of neon if neon has a density of $0.900 \mathrm{~g} / \mathrm{L}$ ?
20. What is the volume in liters of 20.5 g of sulfur hexafluoride if sulfur hexafluoride has a density of $6.164 \mathrm{~g} / \mathrm{L}$ ?
21. Which has the greater volume, 100.0 g of iron $\left(d=7.87 \mathrm{~g} / \mathrm{cm}^{3}\right)$ or 75.0 g of gold $(d=$ $19.3 \mathrm{~g} / \mathrm{cm}^{3}$ )?
22. Which has the greater volume, 100.0 g of hydrogen gas ( $d=0.0000899 \mathrm{~g} / \mathrm{cm}^{3}$ ) or 25.0 g of argon gas $\left(d=0.00178 \mathrm{~g} / \mathrm{cm}^{3}\right)$ ?

## A N S W ERS

1. a. $124^{\circ} \mathrm{C}$
b. $-159^{\circ} \mathrm{C}$
C. $122^{\circ} \mathrm{F}$
d. $-58^{\circ} \mathrm{F}$
2. a. 373 K
b. 173 K
c. $-173^{\circ} \mathrm{C}$
d. $27^{\circ} \mathrm{C}$
3. $-273^{\circ} \mathrm{C}$. This is the lowest possible temperature in degrees Celsius.
4. $57.8^{\circ} \mathrm{C} ; 331 \mathrm{~K}$
5. $\mathrm{g} / \mathrm{mL}, \mathrm{g} / \mathrm{L}$, and $\mathrm{kg} / \mathrm{L}$ (answers will vary)
6. 379 g
7. $1.80 \times 10^{7} \mathrm{~g}$
8. 15 g
9. $8.818 \mathrm{~cm}^{3}$
10. 247 L
11. The 100.0 g of iron has the greater volume.

## 6. END-OF-CHAPTER MATERIAL

## ADDITIONALEXERCISES

1. Evaluate $0.00000000552 \times$
0.0000000006188 and express the answer in scientific notation. You may have to rewrite the original numbers in scientific notation first.
2. Evaluate $333,999,500,000 \div$ 0.00000000003396 and express the answer in scientific notation. You may need to rewrite the original numbers in scientific notation first.
3. Express the number $6.022 \times 10^{23}$ in standard notation.
4. Express the number $6.626 \times 10^{-34}$ in standard notation.
5. When powers of 10 are multiplied together, the powers are added together. For example, $10^{2} \times 10^{3}=10^{2+3}=10^{5}$. With this in mind, can you evaluate (4.506 $\left.\times 10^{4}\right) \times\left(1.003 \times 10^{2}\right)$ without entering scientific notation into your calculator?
6. When powers of 10 are divided into each other, the bottom exponent is subtracted from the top exponent. For example, $10^{5} / 10^{3}=10^{5-3}=10^{2}$. With this in mind, can you evaluate $\left(8.552 \times 10^{6}\right) \div(3.129 \times$ $10^{3}$ ) without entering scientific notation into your calculator?
7. Consider the quantity two dozen eggs. Is the number in this quantity "two" or "two dozen"? Justify your choice.
8. Consider the quantity two dozen eggs. Is the unit in this quantity "eggs" or "dozen eggs"? Justify your choice.
9. Fill in the blank: $1 \mathrm{~km}=$ $\qquad$ $\mu \mathrm{m}$.
10. Fill in the blank: $1 \mathrm{Ms}=$ $\qquad$ ns.
11. Fill in the blank: $1 \mathrm{CL}=$ $\qquad$ ML.
12. Fill in the blank: $1 \mathrm{mg}=$ $\qquad$ kg .
13. Express $67.3 \mathrm{~km} / \mathrm{h}$ in meters/second.
14. Express $0.00444 \mathrm{~m} / \mathrm{s}$ in kilometers/hour.
15. Using the idea that $1.602 \mathrm{~km}=1.000 \mathrm{mi}$, convert a speed of $60.0 \mathrm{mi} / \mathrm{h}$ into kilometers/hour.
16. Using the idea that $1.602 \mathrm{~km}=1.000 \mathrm{mi}$, convert a speed of $60.0 \mathrm{~km} / \mathrm{h}$ into miles/ hour.
17. Convert $52.09 \mathrm{~km} / \mathrm{h}$ into meters/second.
18. Convert $2.155 \mathrm{~m} / \mathrm{s}$ into kilometers/hour.
19. Use the formulas for converting degrees Fahrenheit into degrees Celsius to determine the relative size of the Fahrenheit degree over the Celsius degree.
20. Use the formulas for converting degrees Celsius into kelvins to determine the relative size of the Celsius degree over kelvins.
21. What is the mass of 12.67 L of mercury?
22. What is the mass of $0.663 \mathrm{~m}^{3}$ of air?
23. What is the volume of 2.884 kg of gold?
24. What is the volume of 40.99 kg of cork? Assume a density of $0.22 \mathrm{~g} / \mathrm{cm}^{3}$.

## A N S W ERS

1. $3.42 \times 10^{-18}$
2. $602,200,000,000,000,000,000,000$
3. $4.520 \times 10^{6}$
4. The quantity is two; dozen is the unit.
5. 1,000,000,000
6. 1/100,000,000
7. $18.7 \mathrm{~m} / \mathrm{s}$
8. $96.1 \mathrm{~km} / \mathrm{h}$
9. $14.47 \mathrm{~m} / \mathrm{s}$
10. One Fahrenheit degree is nine-fifths the size of a Celsius degree.
11. $1.72 \times 10^{5} \mathrm{~g}$
12. 149 mL
