Name: $\qquad$

## Math 150 Practice Final B Spring 2010

1. Carry out the following conversions.
a. Write $126.2^{\circ}$ in radians to the nearest 0.01 .
b. Write 1.23 radians in degrees, minutes, seconds, to the nearest second.
2. An arc of a circle of radius 10 cm has arclength 12 cm . What is the angle subtended in degrees to the nearest $0.1^{\circ}$ ?

3. Suppose $\sin (\theta)=0.28$ and $\theta$ lies in the $2^{\text {nd }}$ quadrant. What are the values to the nearest 0.01 of
a. $\cos (\theta)$
b. $\tan (\theta)$
c. $\sec (\theta)$
d. $\csc (\theta)$
e. $\cot (\theta)$
4. Find the length of sides $a$ and $b$ to the nearest 0.1 in the given right triangle with angle $38^{\circ}$ and given side of length 23 .

5. An antenna is located on top of a 12 foot tall garage. From a point on level ground 80 feet from the point directly below the base of the antenna, the antenna subtends an angle of $10^{\circ}$, as shown below. Approximate the length of the antenna to the nearest 0.1 feet.


Name:
6. Give exact values for the given functions at the given points.

| $\theta$ | 0 | $\pi / 3$ | $5 \pi / 6$ | $-3 \pi / 4$ |
| :---: | :--- | :--- | :--- | :--- |
| $\sin (\theta)$ |  |  |  |  |
| $\cos (\theta)$ |  |  |  |  |
| $\tan (\theta)$ |  |  |  |  |

7. Find the solutions to $\sin (2 t+2)=0.7$ for $-\pi<t<\pi$. Report your answers to the nearest 0.01 .
8. Write a formula for the graph shown.


Name:
9. The average monthly high temperature for Paris (in France) is highest in July at $24^{\circ} \mathrm{C}$ and lowest in January at $6^{\circ} \mathrm{C}$. Write a sinusoidal function that models the average monthly high temperature reflecting this data. Your answer should be a function of $t$ where $t$ is the number of the month, with $t=1$ corresponding to January and $t=12$ corresponding to December.
10. A ball kicked from ground with initial velocity $50 \mathrm{ft} / \mathrm{sec}$ at an angle $\theta$ will travel $156.25 \sin (\theta) \cos (\theta)$ feet if there is no air resistance. What angle $\theta$ will result in the ball traveling the farthest and how far will it go (to the nearest foot)?

Name:
11. Suppose you have a signal of the form $\cos (30,000 t)$. You wish to add a signal of the form $\cos (\omega t)$ so that the sum can be written as a product involving a factor of the form $\cos (10,000 t)$. What value should you choose for $\omega$ ?

In the next two problems, solve for the missing parts of the triangle. Note that there may be 0,1 , or 2 solutions. Give values to the nearest 0.1 .
12. $\mathrm{A}=36^{\circ}, \mathrm{B}=49^{\circ}, c=5.3$

13. $\mathrm{A}=42^{\circ}, b=3.7, \mathrm{C}=55^{\circ}$
14. Find the area of a triangle with sides $4.5,5.3$, and 7.2 to the nearest 0.1 .
15. Given the diagram of the plane at the right, with the indicated angle of $148^{\circ}$ and lengths of 10.7 m and 8.2 m , find the angle $B$ to the nearest $0.1^{\circ}$. Be sure to show all your work and justify your choice for B.


Name:
16. What are the third roots of unity? Give exact answers in rectangular form.
17. Let $\boldsymbol{u}=<2,-2,5>$ and $\boldsymbol{v}=<3,-3,2>$. Find $2 \boldsymbol{u}-3 \boldsymbol{v}$.
18. What is the length of the projection of $<3,5>$ onto the vector $<1,7>$ ? Give your answer to the nearest 0.1.

Name:
19. For what values of $B$ is $3 x^{2}+B x y-12 y^{2}=1$ an ellipse?
20. The vector $<3,-2>$ is rotated $30^{\circ}$ counterclockwise. What is the resulting vector? Give your answer to the nearest 0.1 .
$\qquad$
21. Convert the following. Use radians and give your answers to the nearest 0.01 .
a. Write the polar coordinates for the rectangular coordinates $(-4,3)$ (with $r>0$ ).
b. Write the same point $(-4,3)$ in polar coordinates, but this time with $r<0$.
22. A robot arm has two segments, the first 7 meters and the second 5 meters (measurements taken to the pivot in the joint connecting them). The arm starts at the origin and the two segments from a straight line at an angle of $40^{\circ}$ with the horizontal. The second segment is then rotated $20^{\circ}$ counterclockwise as indicated. What is the coordinate of the tip of arm after the rotation (ignore the width of the pieces)? Give your answer to the nearest 0.1.

$\qquad$
23. Write a formula for the ellipse in the sketch with horizontal vertices at $(3,0)$ and $(-9,0)$ and vertical vertices at $(-3,2)$ and $(-3,-2)$.

24. A parabolic reflector for a flashlight is to have a diameter of 10 cm . For what range of depths will the focus be inside the flashlight (i.e. will the distance from the vertex to the focus be smaller than the depth)?

