Math 150 Practice Final B Spring 2010

- 1. Carry out the following conversions.
 - a. Write 126.2° in radians to the nearest 0.01.
 - b. Write 1.23 radians in degrees, minutes, seconds, to the nearest second.
- 2. An arc of a circle of radius 10cm has arclength 12 cm. What is the angle subtended in degrees to the nearest 0.1°?



- 3. Suppose $sin(\theta) = 0.28$ and θ lies in the 2nd quadrant. What are the values to the nearest 0.01 of
 - a. $\cos(\theta)$
 - b. $tan(\theta)$
 - c. $sec(\theta)$
 - d. $\csc(\theta)$
 - e. $\cot(\theta)$

4. Find the length of sides a and b to the nearest 0.1 in the given right triangle with angle 38° and given side of length 23.



5. An antenna is located on top of a 12 foot tall garage. From a point on level ground 80 feet from the point directly below the base of the antenna, the antenna subtends an angle of 10°, as shown below. Approximate the length of the antenna to the nearest 0.1 feet.



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6. Give exact values for the given functions at the given points.

θ	0	π/3	5π / 6	$-3\pi / 4$
$\sin(\theta)$				
$\cos(heta)$				
$\tan(\theta)$				

7. Find the solutions to sin(2t + 2) = 0.7 for $-\pi < t < \pi$. Report your answers to the nearest 0.01.

8. Write a formula for the graph shown.



9. The average monthly high temperature for Paris (in France) is highest in July at 24° C and lowest in January at 6° C. Write a sinusoidal function that models the average monthly high temperature reflecting this data. Your answer should be a function of t where t is the number of the month, with t = 1 corresponding to January and t = 12 corresponding to December.

10. A ball kicked from ground with initial velocity 50ft/sec at an angle θ will travel 156.25 sin(θ)cos(θ) feet if there is no air resistance. What angle θ will result in the ball traveling the farthest and how far will it go (to the nearest foot)?

11. Suppose you have a signal of the form cos(30,000 t). You wish to add a signal of the form $cos(\omega t)$ so that the sum can be written as a product involving a factor of the form cos(10,000 t). What value should you choose for ω ?

In the next two problems, solve for the missing parts of the triangle. Note that there may be 0, 1, or 2 solutions. Give values to the nearest 0.1.

12. $A = 36^{\circ}, B = 49^{\circ}, c = 5.3$



13. A = 42°, b = 3.7, C = 55°

14. Find the area of a triangle with sides 4.5, 5.3, and 7.2 to the nearest 0.1.

15. Given the diagram of the plane at the right, with the indicated angle of 148° and lengths of 10.7m and 8.2m, find the angle B to the nearest 0.1°. Be sure to show all your work and justify your choice for B.



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16. What are the third roots of unity? Give exact answers in rectangular form.

17. Let $u = \langle 2, -2, 5 \rangle$ and $v = \langle 3, -3, 2 \rangle$. Find 2u - 3v.

18. What is the length of the projection of <3, 5> onto the vector <1, 7>? Give your answer to the nearest 0.1.

19. For what values of *B* is $3x^2 + Bxy - 12y^2 = 1$ an ellipse?

20. The vector <3, -2> is rotated 30° counterclockwise. What is the resulting vector? Give your answer to the nearest 0.1.

- 21. Convert the following. Use radians and give your answers to the nearest 0.01.
 - a. Write the polar coordinates for the rectangular coordinates (-4, 3) (with r > 0).

b. Write the same point (-4, 3) in polar coordinates, but this time with r < 0.

22. A robot arm has two segments, the first 7 meters and the second 5 meters (measurements taken to the pivot in the joint connecting them). The arm starts at the origin and the two segments from a straight line at an angle of 40° with the horizontal. The second segment is then rotated 20° counterclockwise as indicated. What is the coordinate of the tip of arm after the rotation (ignore the width of the pieces)? Give your answer to the nearest 0.1.



23. Write a formula for the ellipse in the sketch with horizontal vertices at (3, 0) and (-9, 0) and vertical vertices at (-3, 2) and (-3, -2).



24. A parabolic reflector for a flashlight is to have a diameter of 10cm. For what range of depths will the focus be inside the flashlight (i.e. will the distance from the vertex to the focus be smaller than the depth)?