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ABSTRACT

An Adaptive Fusion Model For Distributed Detection Systems With Unequiprobable Sources

by
Yuzheng Zhang

In a traditional communication system, a single sensor such as a radar or a sonar is used to detect targets. Since the reliability of a single sensor is limited, distributed detection systems in which several sensors are employed simultaneously have received increasing attention in recent years. We consider a distributed detection system which consists of a number of independent local detectors and a fusion center. *Chair* and *Varshney* have derived an optimal decision rule for fusing decisions based on the *Bayesian* criterion. To implement such a rule, the probability of detection P_D and the probability of false alarm P_F for each local detector must be known. This thesis introduces an adaptive fusion model using the fusion result as a supervisor to estimate the P_D and P_F . The fusion results are classified as “reliable” and “unreliable.” Reliable results will be used as a reference to update the weights in the fusion center. Unreliable results will be discarded. The thesis concludes with simulation results which conform to the analysis.

AN ADAPTIVE FUSION MODEL FOR DISTRIBUTED
DETECTION SYSTEMS WITH UNEQUIPROBABLE SOURCES

by
Yuzheng Zhang

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APPROVAL PAGE

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This work is dedicated to
my family

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CHAPTER 1

INTRODUCTION

1.1 Background

There has been a growing interest in developing efficient and reliable distributed detection systems (the multiple sensor systems) for target recognition and communications. There are two major options for data processing in multiple sensor systems. In the first option, complete sensor observations are transmitted to the central processor. This requires a large communication bandwidth. The second option is to have distributed systems. Some or all of the processing results can be done at each local sensor system and then transferred to a fusion center. Tenney and Sandell [1] were one of the first to study the problem of detection with distributed sensors. They applied the classical single sensor detection theory to a two-sensor two-hypothesis test. An optimum local decision rule was established to minimize a global cost. Sadjadi [2] generalized the work of [1] to n detectors and m hypotheses, and obtained similar conclusions. Chair and Varshney [3] assumed that each local detector had fixed thresholds and each local decision was independent. With these assumptions, an optimum fusion model was generated.

Optimal techniques have also been developed for other criterions. When *a priori* probabilities were unknown, Thomopoulos [4] used the Neyman-Pearson (NP) test both at the local detector level as well as the decision fusion level. An optimal decision scheme was derived. Demirbas [5] applied the maximum a posterior (MAP) concept for object recognition in multi sensor environment and showed that the maximum a posterior (MAP) estimation approach minimized mean square error estimation.

In the distributed system with a data fusion shown in Figure 1.1, some data processing is done at each sensor and partial results are transmitted to the data fusion center for further processing. The final result are then available at the data

fusion center. In considering the cost, reliability, survivability, and communication bandwidth, the option of distributed processing is more attractive for many applications.

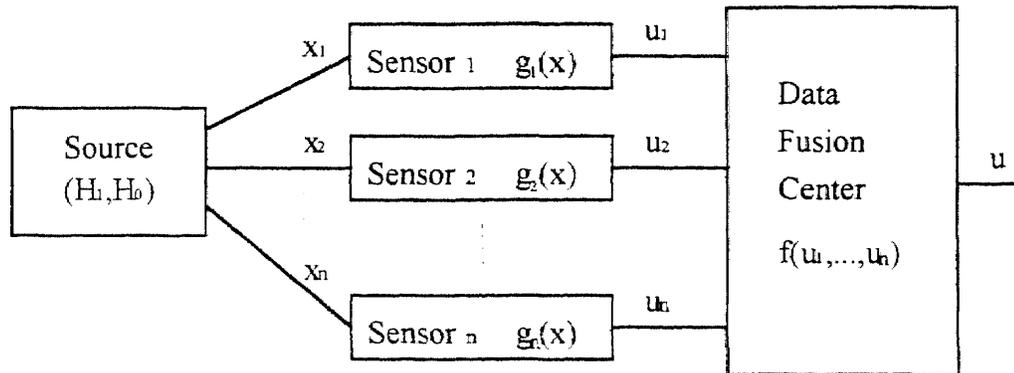


Figure 1.1 Distributed detection system with a data fusion center

We consider the optimal decision rule which was derived by Chair and Varshney [3]. To implement such rule, the probability of detection P_D and the probability of false alarm P_F for each detector must be known, but this information is not always available in practice. In this thesis, we proposed and developed an adaptive model which is extended from Chair and Varshney's work [3], and uses the fusion results as a supervisor to estimate P_D and P_F . The model for equiprobable sources has been presented [6]. This thesis consider the performance and analysis for unequiprobable sources. Various components of the model will be covered: the fusion rule, classification of fusion results, updating algorithm for the fusion center, and computer simulations.

1.2 Preliminaries

Let us consider a binary hypothesis testing problem with the following two hypotheses

H_0 : signal is absent

H_1 : signal is present

The *a priori* probabilities of the two hypotheses are denoted by $P(H_0) = P_0$ and $P(H_1) = P_1$. As shown in Figure 1.1, we assume that there are n detectors, and the observations at each detector are denoted by $x_i, i = 1, \dots, n$. We further assume that the observations at the individual detectors are statistically independent and that the conditional probability is denoted by $P(x_i|H_j), i = 1, \dots, n, j = 0, 1$. Each detector employs a decision rule $g_i(x_i)$ to make a decision $u_i, i = 1, \dots, n$, where

$$u_i = \begin{cases} -1, & \text{if } H_0 \text{ is declared} \\ +1, & \text{if } H_1 \text{ is declared} \end{cases} \quad (1.1)$$

The probabilities of false alarm and miss for each detector are denoted by P_{F_i} and P_{M_i} , respectively.

After processing the observations locally, the decisions u_i are transmitted to the data fusion center. This reduces the communication bandwidth required as compared to what is needed if the complete observations x_i were transmitted. The data fusion center determines the overall decision u for the system based on the individual decisions. i.e.,

$$u = f(u_1, \dots, u_n). \quad (1.2)$$

In the next chapter, an optimum data fusion rule for our model will be derived.

CHAPTER 2

DATA FUSION RULE

2.1 Derivation of The Data Fusion Rule

We assume that each local detector has fixed thresholds and the probabilities of false alarm and miss for each detector, P_F and P_M , are known. Each local decision is also assumed to be independent.

The data fusion problem can be viewed as a binary-hypothesis detection problem with individual detector's decisions being the observations. We consider the Bayes decision criterion which employs a systematic procedure of assigning a cost to each correct and incorrect decision, and then minimizing the total average cost, denoted by B . If we let C_{jk} be the cost of making decision D_j when H_k is true, then for binary decision problem there are four possible costs:

$$C_{10} = \text{Cost of deciding } D_1 \text{ when } H_0 \text{ is true}$$

$$C_{00} = \text{Cost of deciding } D_0 \text{ when } H_0 \text{ is true}$$

$$C_{01} = \text{Cost of deciding } D_0 \text{ when } H_1 \text{ is true}$$

$$C_{11} = \text{Cost of deciding } D_1 \text{ when } H_1 \text{ is true}$$

where $D_1 : u = +1$, $D_0 : u = -1$. The total average cost is:

$$\begin{aligned} B &= E[C_{jk}] \\ &= C_{10}P[D_1, H_0] + C_{00}P[D_0, H_0] + C_{01}P[D_0, H_1] + C_{11}P[D_1, H_1]. \end{aligned}$$

To minimize the cost B , The optimum decision rule is given by the following likelihood ratio test [7] (Bayes decision criterion):

$$\frac{P(u_1, \dots, u_n | H_1)}{P(u_1, \dots, u_n | H_0)} \underset{H_0}{\overset{H_1}{>}} \frac{P_0(C_{10} - C_{00})}{P_1(C_{01} - C_{11})}. \quad (2.1)$$

The quantity on the left-hand side is the likelihood ratio, and the Bayes optimum threshold is on the right-hand side. In our model, we use the minimum probability of error criterion, that is, $C_{00} = C_{11} = 0$, and $C_{10} = C_{01} = 1$. Therefore,

$$\frac{P(\mathbf{u} | H_1)}{P(\mathbf{u} | H_0)} \underset{H_0}{\overset{H_1}{>}} \frac{P_0}{P_1}, \quad (2.2)$$

where \mathbf{u} is a vector of observations. Using *Bayes* rule:

$$P(x, y) = P(x|y)P(y) = P(y|x)P(x),$$

to express the conditional probabilities, we have:

$$\frac{P(\mathbf{u}|H_1)P_1}{P(\mathbf{u}|H_0)P_0} = \frac{P(\mathbf{u}, H_1)}{P(\mathbf{u}, H_0)} = \frac{P(H_1|\mathbf{u})}{P(H_0|\mathbf{u})} \underset{H_0}{\overset{H_1}{>}} 1. \quad (2.3)$$

Thus the corresponding log-likelihood ratio test is

$$\log \frac{P(H_1|\mathbf{u})}{P(H_0|\mathbf{u})} \underset{H_0}{\overset{H_1}{>}} 0 \quad (2.4)$$

Let S_+ be the set of all local detectors i such that the local decision $u_i = +1$, and S_- be the set of all local detectors i such that the local decision $u_i = -1$. Assume that u_i 's are independent,

$$\begin{aligned} P(H_1|\mathbf{u}) &= \frac{P_1 P(\mathbf{u}|H_1)}{P(\mathbf{u})} \\ &= \frac{P_1}{P(\mathbf{u})} \prod_{S_+} P(u_i = +1|H_1) \cdot \prod_{S_-} P(u_i = -1|H_1). \end{aligned} \quad (2.5)$$

Similarly,

$$\begin{aligned} P(H_0|\mathbf{u}) &= \frac{P_0 P(\mathbf{u}|H_0)}{P(\mathbf{u})} \\ &= \frac{P_0}{P(\mathbf{u})} \prod_{S_+} P(u_i = +1|H_0) \cdot \prod_{S_-} P(u_i = -1|H_0). \end{aligned} \quad (2.6)$$

Thus, from Eq.(2.5) and Eq.(2.6):

$$\log \frac{P(H_1|\mathbf{u})}{P(H_0|\mathbf{u})} = \log \frac{P_1}{P_0} + \sum_{S_+} \log \frac{P(u_i = +1|H_1)}{P(u_i = +1|H_0)} + \sum_{S_-} \log \frac{P(u_i = -1|H_1)}{P(u_i = -1|H_0)} \quad (2.7)$$

Define

$$\begin{aligned} w_0 &= \log \frac{P_1}{P_0}, \\ w_i &= \begin{cases} \log \frac{P(u_i = +1|H_1)}{P(u_i = +1|H_0)}, & \text{if } u_i = +1, \\ \log \frac{P(u_i = -1|H_0)}{P(u_i = -1|H_1)}, & \text{if } u_i = -1, \end{cases} \end{aligned} \quad (2.8)$$

or

$$w_0 = \log \frac{P_1}{P_0}$$

$$w_i = \begin{cases} \log \frac{1 - P_{M_i}}{P_{F_i}}, & \text{if } u_i = +1. \\ \log \frac{1 - P_{F_i}}{P_{M_i}}, & \text{if } u_i = -1. \end{cases} \quad (2.9)$$

Eq.(2.7) can be expressed as

$$\log \frac{P(H_1|\mathbf{u})}{P(H_0|\mathbf{u})} = w_0 + \sum_{S_+} w_i - \sum_{S_-} w_i$$

$$= w_0 + \sum_{i=1}^n w_i u_i. \quad (2.10)$$

Therefore, from Eq.(2.4) and Eq.(2.10), we have the data fusion rule as

$$u = f(u_1, \dots, u_n) = \begin{cases} 1, & \text{if } w_0 + \sum_{i=1}^n w_i u_i > 0. \\ -1, & \text{otherwise.} \end{cases} \quad (2.11)$$

The optimum data fusion rule can be implemented as shown in Figure 2.1.

where

$$y = w_0 + \sum_{i=1}^n w_i u_i.$$

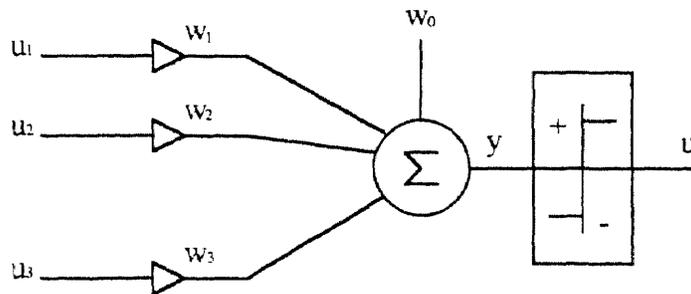


Figure 2.1 The fusion center structure

2.2 Properties of The Fusion Rule

There are two interesting properties about the fusion rule. One describes the relationship between two conditional probability mass functions: $P(y - w_0 = \zeta|H_1)$ and $P(y - w_0 = \zeta|H_0)$, described as Lemma I. It is very useful to analyze the performance, when we use y (see Figure 2.1) as a supervisor to train each weight in the fusion center. The other describes the conditions, which can make the system approach optimum, described as Lemma II.

2.2.1 Lemma I:

When each weight in the fusion center is optimum (described in section 2.1), the conditional probability mass functions $P(y - w_0 = \zeta|H_1)$ and $P(y - w_0 = \zeta|H_0)$ satisfy the following equation:

$$e^\zeta = \frac{P(y - w_0 = \zeta|H_1)}{P(y - w_0 = \zeta|H_0)},$$

where ζ is a possible value of $y - w_0$.

Proof:

Consider the structure shown in Figure 2.1. We have:

$$y = w_0 + \sum_{j=1}^n w_j u_j \quad (2.12)$$

$$\text{or } y = w_0 + \sum_{j \in S^+} w_j - \sum_{j \in S^-} w_j. \quad (2.13)$$

Here $S^+ = \{j : u_j = 1\}$, and $S^- = \{j : u_j = -1\}$. From Eq.(2.8), Eq.(2.13):

$$\begin{aligned} y &= w_0 + \sum_{j \in S^+} \log \frac{P(u_j = 1|H_1)}{P(u_j = 1|H_0)} - \sum_{j \in S^-} \log \frac{P(u_j = -1|H_0)}{P(u_j = -1|H_1)} \\ &= w_0 + \log \left[\prod_{j \in S^+} \frac{P(u_j = 1|H_1)}{P(u_j = 1|H_0)} \bigg/ \prod_{j \in S^-} \frac{P(u_j = -1|H_0)}{P(u_j = -1|H_1)} \right] \\ \text{or } e^{y-w_0} &= \frac{\prod_{j \in S^+} P(u_j = 1|H_1) \prod_{j \in S^-} P(u_j = -1|H_1)}{\prod_{j \in S^+} P(u_j = 1|H_0) \prod_{j \in S^-} P(u_j = -1|H_0)}. \end{aligned} \quad (2.14)$$

Let ζ be a possible value of $y - w_0$ and each local decision u_j is independent,

$$P(y - w_0 = \zeta | H_1) = \sum_{\mathbf{u} \in U} P(\mathbf{w}^T \mathbf{u} = \zeta | H_1),$$

where \mathbf{u} is a vector of $u_i, i = 1, 2, \dots$. \mathbf{w} is a vector of $w_i, i = 1, 2, \dots$, and

$$U = \{\mathbf{u} : \mathbf{w}^T \mathbf{u} = \zeta\}.$$

By defining S as $\{\{S^+, S^-\}$: a combination of S^+ and S^- such that

$$\sum_{j \in S^+} w_j - \sum_{j \in S^-} w_j = \zeta\},$$

$$P(y - w_0 = \zeta | H_1) = \sum_S \prod_{j \in S^+} P(u_j = 1 | H_1) \prod_{j \in S^-} P(u_j = -1 | H_1),$$

$$\text{and } P(y - w_0 = \zeta | H_0) = \sum_S \prod_{j \in S^+} P(u_j = 1 | H_0) \prod_{j \in S^-} P(u_j = -1 | H_0).$$

Thus,

$$\frac{P(y - w_0 = \zeta | H_1)}{P(y - w_0 = \zeta | H_0)} = \frac{\sum_S \prod_{j \in S^+} P(u_j = 1 | H_1) \prod_{j \in S^-} P(u_j = -1 | H_1)}{\sum_S \prod_{j \in S^+} P(u_j = 1 | H_0) \prod_{j \in S^-} P(u_j = -1 | H_0)}. \quad (2.15)$$

From Eq.(2.14) and the following equality

$$\frac{a}{b} = \frac{c}{d} = k \quad \Rightarrow \quad \frac{a+c}{b+d} = \frac{bk+dk}{b+d} = k, \quad (b \neq 0, d \neq 0, b+d \neq 0)$$

then

$$\begin{aligned} \frac{P(y - w_0 = \zeta | H_1)}{P(y - w_0 = \zeta | H_0)} &= \frac{\sum_S \prod_{j \in S^+} P(u_j = 1 | H_1) \prod_{j \in S^-} P(u_j = -1 | H_1)}{\sum_S \prod_{j \in S^+} P(u_j = 1 | H_0) \prod_{j \in S^-} P(u_j = -1 | H_0)} \\ &= \frac{\prod_{j \in S^+} P(u_j = 1 | H_1) \prod_{j \in S^-} P(u_j = -1 | H_1)}{\prod_{j \in S^+} P(u_j = 1 | H_0) \prod_{j \in S^-} P(u_j = -1 | H_0)} \end{aligned}$$

$$\frac{P(y - w_0 = \zeta | H_1)}{P(y - w_0 = \zeta | H_0)} = e^{y - w_0} = e^\zeta. \quad (2.16)$$

□

Eq.(2.16) is a very interesting result. The ratio of the conditional probabilities under H_1 and H_0 only depends on the value $y-w_0$, even the probability mass functions $P(y-w_0=\zeta|H_1)$ and $P(y-w_0=\zeta|H_0)$ may not be monotonic with ζ . This is illustrated in Figure 2.2.

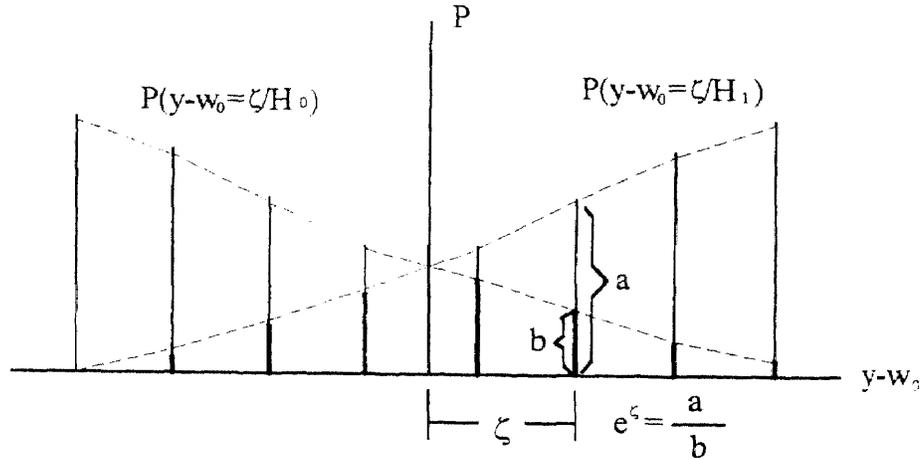


Figure 2.2 Relationship between $P(y-w_0=\zeta|H_1)$ and $P(y-w_0=\zeta|H_0)$

2.2.2 Lemma II

Let the fused results be classified as reliable and unreliable. Denoting the reliable results by \widehat{H}_1 and \widehat{H}_0 , and the unreliable results by \widehat{H}_r :

$$P(\widehat{H}_1) + P(\widehat{H}_0) + P(\widehat{H}_r) = 1. \quad (2.17)$$

Only reliable results \widehat{H}_1 and \widehat{H}_0 are used to update each weight, denoted by \widehat{w}_i . Let $\alpha = \frac{P(\widehat{H}_1|H_0)}{P(\widehat{H}_1|H_1)}$, $\beta = \frac{P(\widehat{H}_0|H_1)}{P(\widehat{H}_0|H_0)}$ and $\gamma = \frac{P(\widehat{H}_1|H_1)}{P(\widehat{H}_0|H_0)}$. If $\alpha = 0$, $\beta = 0$ and $\gamma = 1$, then $\epsilon = |w_i - \widehat{w}_i| = 0$, $i = 0, 1, \dots$, i.e., \widehat{w}_i 's are perfect estimation of w_i in this case.

Proof:

Let $r_i = \log w_i$ and $\hat{r}_i = \log \hat{w}_i$. we have,

$$\left\{ \begin{array}{l} r_0 = \frac{P_1}{P_0} \\ r_i = \begin{cases} \frac{P(u_i = 1|H_1)}{P(u_i = 1|H_0)} & \text{if } u_i = +1 \\ \frac{P(u_i = -1|H_0)}{P(u_i = -1|H_1)} & \text{if } u_i = -1, \end{cases} \end{array} \right. \quad (2.18)$$

and

$$\left\{ \begin{array}{l} \hat{r}_0 = \frac{P(\hat{H}_1)}{P(\hat{H}_0)} \\ \hat{r}_i = \begin{cases} \frac{P(u_i = 1|\hat{H}_1)}{P(u_i = 1|\hat{H}_0)} & \text{if } u_i = +1 \\ \frac{P(u_i = -1|\hat{H}_0)}{P(u_i = -1|\hat{H}_1)} & \text{if } u_i = -1. \end{cases} \end{array} \right. \quad (2.19)$$

Using the *total probability theorem* $P(BA) = P(B|A)P(A)$:

$$\begin{aligned} P(u_i = 1|\hat{H}_1) &= \frac{P(u_i = 1, \hat{H}_1)}{P(\hat{H}_1)} \\ &= \frac{P(u_i = 1, \hat{H}_1|H_0)P(H_0) + P(u_i = 1, \hat{H}_1|H_1)P(H_1)}{P(\hat{H}_1)} \\ &= \frac{P(u_i = 1|H_0)P(\hat{H}_1|u_i = 1, H_0)P(H_0) + P(u_i = 1|H_1)P(\hat{H}_1|u_i = 1, H_1)P(H_1)}{P(\hat{H}_1)}. \end{aligned}$$

Similarly,

$$P(u_i = 1|\widehat{H}_0) =$$

$$\frac{P(u_i = 1|H_0)P(\widehat{H}_0|u_i = 1, H_0)P(H_0) + P(u_i = 1|H_1)P(\widehat{H}_0|u_i = 1, H_1)P(H_1)}{P(\widehat{H}_0)},$$

$$P(u_i = -1|\widehat{H}_0) =$$

$$\frac{P(u_i = -1|H_0)P(\widehat{H}_0|u_i = -1, H_0)P(H_0) + P(u_i = -1|H_1)P(\widehat{H}_0|u_i = -1, H_1)P(H_1)}{P(\widehat{H}_0)},$$

$$P(u_i = -1|\widehat{H}_1) =$$

$$\frac{P(u_i = 1|H_0)P(\widehat{H}_1|u_i = -1, H_0)P(H_0) + P(u_i = -1|H_1)P(\widehat{H}_1|u_i = -1, H_1)P(H_1)}{P(\widehat{H}_1)}.$$

Using Eq.(2.19) and the above formulas:

if $u_i = +1$

$$\begin{aligned} \widehat{r}_i &= \frac{[P(u_i = 1|H_0)P(\widehat{H}_1|u_i = 1, H_0)P(H_0) + P(u_i = 1|H_1)P(\widehat{H}_1|u_i = 1, H_1)P(H_1)]P(\widehat{H}_0)}{[P(u_i = 1|H_0)P(\widehat{H}_0|u_i = 1, H_0)P(H_0) + P(u_i = 1|H_1)P(\widehat{H}_0|u_i = 1, H_1)P(H_1)]P(\widehat{H}_1)} \\ &= \frac{P(u_i = 1|H_1)P(\widehat{H}_1|H_1)P(H_1)P(\widehat{H}_0)}{P(u_i = 1|H_0)P(\widehat{H}_0|H_0)P(H_0)P(\widehat{H}_1)} \cdot \frac{P(u_i = 1|H_0) \frac{P(\widehat{H}_1|H_0)}{P(\widehat{H}_1|H_1)} \frac{P(H_0)}{P(H_1)} + 1}{1 + \frac{P(u_i = 1|H_1) \frac{P(\widehat{H}_0|H_1)}{P(\widehat{H}_0|H_0)} \frac{P(H_1)}{P(H_0)}}{P(u_i = 1|H_0) \frac{P(\widehat{H}_0|H_0)}{P(\widehat{H}_0|H_0)} \frac{P(H_0)}{P(H_1)}}} \\ &= r_i \cdot \frac{P(\widehat{H}_1|H_1)}{P(\widehat{H}_0|H_0)} \cdot \frac{P(H_1)}{P(H_0)} \cdot \frac{P(\widehat{H}_0)}{P(\widehat{H}_1)} \cdot \frac{\frac{1}{r_i} \frac{P(\widehat{H}_1|H_0)}{P(\widehat{H}_1|H_1)} \frac{1}{r_0} + 1}{1 + r_i \frac{P(\widehat{H}_0|H_1)}{P(\widehat{H}_0|H_0)} r_0}. \end{aligned}$$

Here,

$$\begin{aligned}
& \frac{P(\widehat{H}_1|H_1)}{P(\widehat{H}_0|H_0)} \cdot \frac{P(H_1)}{P(H_0)} \cdot \frac{P(\widehat{H}_0)}{P(\widehat{H}_1)} = \frac{P(\widehat{H}_1, H_1)}{P(\widehat{H}_0, H_0)} \cdot \frac{P(\widehat{H}_0)}{P(\widehat{H}_1)} = \frac{P(H_1|\widehat{H}_1)}{P(H_0|\widehat{H}_0)} \\
& = \frac{P(\widehat{H}_1|H_1)}{P(\widehat{H}_1|H_0) + P(\widehat{H}_1|H_1)} \cdot \frac{P(\widehat{H}_0|H_0) + P(\widehat{H}_0|H_1)}{P(\widehat{H}_0|H_0)} \quad (\text{by Bayes' Theorem}) \\
& = \frac{1}{1 + \frac{P(\widehat{H}_1|H_0)}{P(\widehat{H}_1|H_1)}} \cdot \left[1 + \frac{P(\widehat{H}_0|H_1)}{P(\widehat{H}_0|H_0)} \right].
\end{aligned}$$

Thus,

$$\widehat{r}_i = r_i \cdot \frac{1 + \frac{P(\widehat{H}_0|H_1)}{P(\widehat{H}_0|H_0)}}{1 + \frac{P(\widehat{H}_1|H_0)}{P(\widehat{H}_1|H_1)}} \cdot \frac{1 + \frac{1}{r_i r_0} \frac{P(\widehat{H}_1|H_0)}{P(\widehat{H}_1|H_1)}}{1 + r_i r_0 \frac{P(\widehat{H}_0|H_1)}{P(\widehat{H}_0|H_0)}}.$$

Let $\alpha = \frac{P(\widehat{H}_1|H_0)}{P(\widehat{H}_1|H_1)}$, and $\beta = \frac{P(\widehat{H}_0|H_1)}{P(\widehat{H}_0|H_0)}$, then

$$\widehat{r}_i = r_i \cdot \frac{1 + \beta}{1 + \alpha} \cdot \frac{1 + \frac{\alpha}{r_i r_0}}{1 + r_i r_0 \beta}. \quad (2.20)$$

Using the following equality

$$\frac{1}{1+x} = 1 - x + x^2 - x^3 + x^4 - \dots = 1 - x + O[x] \quad (|x| < 1) \quad (2.21)$$

where $O[x]$ is the higher order terms of x .

If $\alpha \ll 1$, and $\beta \ll 1$, we have

$$\begin{aligned}
\widehat{r}_i & = r_i (1 + \beta) \left(1 + \frac{\alpha}{r_i r_0} \right) (1 - \alpha + O[\alpha]) (1 - r_i r_0 \beta + O[\beta]) \\
& = r_i \cdot \left[1 + \alpha \cdot \left(1/(r_i r_0) - 1 \right) + \beta \cdot (1 - r_i r_0) + O[\alpha, \beta] \right], \quad (2.22)
\end{aligned}$$

where $O[\alpha, \beta]$ is higher order terms of α and β that is close to 0.

Similarly, if $u_i = -1$,

$$\begin{aligned}
\hat{r}_i &= r_i \cdot \frac{1 + \frac{r_0 P(\widehat{H}_0|H_1)}{r_i P(\widehat{H}_0|H_0)}}{1 + \frac{r_i P(\widehat{H}_1|H_0)}{r_0 P(\widehat{H}_1|H_1)}} \cdot \frac{1 + \frac{P(\widehat{H}_1|H_0)}{P(\widehat{H}_1|H_1)}}{1 + \frac{P(\widehat{H}_0|H_1)}{P(\widehat{H}_0|H_0)}} \\
&= r_i \cdot \frac{1 + \frac{r_0}{r_i} \beta}{1 + \frac{r_i}{r_0} \alpha} \cdot \frac{1 + \alpha}{1 + \beta} \\
&= r_i \left(1 + \frac{r_0}{r_i} \beta\right) \left(1 - \frac{r_i}{r_0} \alpha + O[\alpha]\right) (1 + \alpha) (1 - \beta + O[\beta]) \\
&= r_i \cdot [1 + \beta \cdot (r_0/r_i - 1) + \alpha \cdot (1 - r_i/r_0) + O[\alpha, \beta]]. \tag{2.23}
\end{aligned}$$

From Eq.(2.19):

$$\begin{aligned}
\hat{r}_0 &= \frac{P(\widehat{H}_1)}{P(\widehat{H}_0)} \\
&= \frac{P_1}{P_0} \cdot \frac{P(\widehat{H}_1|H_1)}{P(\widehat{H}_0|H_0)} \\
\hat{r}_0 &= r_0 \cdot \gamma \tag{2.24}
\end{aligned}$$

$$\text{where } \gamma = \frac{P(\widehat{H}_1|H_1)}{P(\widehat{H}_0|H_0)}.$$

From Eq.(2.22), Eq.(2.23), Eq.(2.24), if $\alpha = \frac{P(\widehat{H}_1|H_0)}{P(\widehat{H}_1|H_1)} \rightarrow 0$, $\beta = \frac{P(\widehat{H}_0|H_1)}{P(\widehat{H}_0|H_0)} \rightarrow 0$ and $\gamma = \frac{P(\widehat{H}_1|H_1)}{P(\widehat{H}_0|H_0)} \rightarrow 1$, then $\hat{r}_i \rightarrow r_i$, $\hat{w}_i \rightarrow w_i$, for $i = 0, 1, \dots$. □

CHAPTER 3
MODEL ANALYSIS

3.1 Classification of Fusion Results

Recall the data fusion center structure shown in Figure 2.1. If the reference signals are given, they can be used as a "reference" to train the system such that weights will converge to the optimal values defined by Eq.(2.8). However, in practice such a reference is not readily available and at the same time, the P_D and P_F of a detector may vary with time. Since the fused decisions are usually better than local decisions, they can be considered as the reference. When the i th local decision u_i is equal to

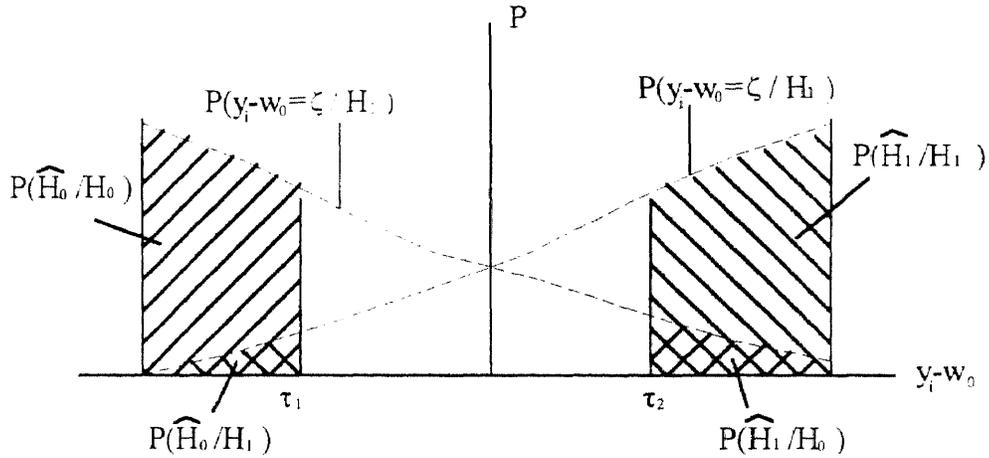


Figure 3.1 Classification of fusion results

the fused decision u , then u_i is considered to be correct, otherwise, u_i is considered to be incorrect. Since $y = w_0 + \sum_{i=1}^n w_i u_i$, the fused decision u has already taken into account the decision of the i th detector, u_i . If u is used as a reference for u_i , a bias is established for u_i . Thus, in the proposed system, the decision of the i th local detector u_i is arbitrated by the fused decision of all the other $(n - 1)$ local detectors. Denote this fused decision as \bar{u}_i , and define

$$y_i = y - w_0 - w_i = \sum_{j \neq i} w_j u_j \quad (3.1)$$

The decision \bar{u}_i in the fusion center for updating \hat{w}_i depends on the value y_i . The value y_i is divided into reliable and unreliable range. We denote the lower and upper

limit of the unreliable range as τ_1 and τ_2 shown in Figure 3.1. We call τ_1 and τ_2 the *reliability thresholds*. Only the fused decision \bar{u}_i which satisfy $y_i < \tau_1$ or $y_i > \tau_2$ are chosen to adapt the weight w_i . These decisions are considered as *reliable decisions*, defined by \widehat{H}_1 when $y_i > \tau_2$, and \widehat{H}_0 when $y_i < \tau_1$. This type of learning belongs to the class of reinforcement learning [8][9][10][11].

3.1.1 Lemma III

$\alpha = \frac{P(\widehat{H}_1|H_0)}{P(\widehat{H}_1|H_1)}$ is monotonically decreasing with τ_2 .

proof :

$$\begin{aligned} \alpha &= \frac{P(\widehat{H}_1|H_0)}{P(\widehat{H}_1|H_1)} \\ &= \frac{P(y_i > \tau_2|H_0)}{P(y_i > \tau_2|H_1)} \\ &= \frac{\sum_{j=1}^n P(y_i = \zeta_j|H_0)}{\sum_{j=1}^n P(y_i = \zeta_j|H_1)}. \end{aligned}$$

Without lose of generality, assume that $\zeta_1 > \zeta_2 > \dots > \zeta_n > \tau_2$ are all possible y_j . Note that as τ_2 becomes larger, n becomes smaller.

From Eq.(2.16)

$$e^{-\zeta} = \frac{P(y_i = \zeta|H_0)}{P(y_i = \zeta|H_1)},$$

we have,

$$\frac{P(y_i = \zeta_1|H_0)}{P(y_i = \zeta_1|H_1)} < \frac{P(y_i = \zeta_2|H_0)}{P(y_i = \zeta_2|H_1)} < \dots < \frac{P(y_i = \zeta_n|H_0)}{P(y_i = \zeta_n|H_1)} \quad (3.2)$$

Denote $A_k = \sum_{j=1}^k P(y_i = \zeta_j|H_1)$, $B_k = \sum_{j=1}^k P(y_i = \zeta_j|H_0)$, and $\alpha_k = \frac{A_k}{B_k}$. The objective is to show that $\alpha_k > \alpha_{k-1}$ for $k = 1, 2, \dots, n$. First we need to show $\alpha_2 > \alpha_1$.

$$\begin{aligned}\alpha_1 &= \frac{P(y_i = \zeta_1|H_0)}{P(y_i = \zeta_1|H_1)} \\ \alpha_2 &= \frac{P(y_i = \zeta_1|H_0) + P(y_i = \zeta_2|H_0)}{P(y_i = \zeta_1|H_1) + P(y_i = \zeta_2|H_1)}\end{aligned}$$

Using the following inequality and Eq.(3.2),

$$\frac{X}{Y} < \frac{a}{b} \quad \Rightarrow \quad \frac{X}{Y} < \frac{X+a}{Y+b} < \frac{a}{b} \quad (Y, b > 0), \quad (3.3)$$

we have:

$$\alpha_2 > \alpha_1. \quad (3.4)$$

Next, we shall show that, if $\alpha_k > \alpha_{k-1}$, then $\alpha_{k+1} > \alpha_k$.

Since

$$\alpha_{k-1} < \alpha_k \quad (3.5)$$

$$\begin{aligned}\frac{A_{k-1}}{B_{k-1}} &< \frac{A_k}{B_k} \\ \Rightarrow \frac{A_{k-1}}{B_{k-1}} &< \frac{A_{k-1} + P(y_i = \zeta_k|H_0)}{B_{k-1} + P(y_i = \zeta_k|H_1)}\end{aligned} \quad (3.6)$$

Using inequality Eq.(3.3) again,

$$\frac{A_{k-1}}{B_{k-1}} < \frac{A_{k-1} + P(y_i = \zeta_k|H_0)}{B_{k-1} + P(y_i = \zeta_k|H_1)} < \frac{P(y_i = \zeta_k|H_0)}{P(y_i = \zeta_k|H_1)} \quad (3.7)$$

Applying Eq.(3.2) and Eq.(3.6) yields:

$$\frac{A_{k-1} + P(y_i = \zeta_k|H_0)}{B_{k-1} + P(y_i = \zeta_k|H_1)} < \frac{P(y_i = \zeta_k|H_0)}{P(y_i = \zeta_k|H_1)} < \frac{P(y_i = \zeta_{k+1}|H_0)}{P(y_i = \zeta_{k+1}|H_1)}$$

Using Eq.(3.3)

$$\begin{aligned}\frac{A_{k-1} + P(y_i = \zeta_k|H_0)}{B_{k-1} + P(y_i = \zeta_k|H_1)} &< \frac{A_{k-1} + P(y_i = \zeta_k|H_0) + P(y_i = \zeta_{k+1}|H_0)}{B_{k-1} + P(y_i = \zeta_k|H_1) + P(y_i = \zeta_{k+1}|H_1)} \\ &\Rightarrow \frac{A_k}{B_k} < \frac{A_{k+1}}{B_{k+1}} \Rightarrow \alpha_k < \alpha_{k+1}\end{aligned} \quad (3.8)$$

From Eq.(3.4), Eq.(3.7) and Eq.(3.8), the α decreases monotonically with τ_2 increasing.

□

3.1.2 Lemma IV

$\beta = \frac{P(\widehat{H}_0|H_1)}{P(\widehat{H}_0|H_0)}$ is monotonically increasing with τ_1 .

Proof:

It is similar to the proof of Lemma III.

□

3.1.3 Lemma V

If τ_1 decreases and τ_2 increases, $\epsilon = |w_i - \widehat{w}_i|$ is decreasing.

Proof:

From Lemma III and Lemma IV as τ_1 decreases and τ_2 increases, α and β are decreasing. Thus, From Lemma II, $\epsilon = |w_i - \widehat{w}_i|$ is decreasing.

□

3.2 Updating

The distributed decision system is assumed to have no knowledge of the probability mass functions of the observations. Thus, the estimated probability of detection and false alarm for the i th detector \widehat{P}_{D_i} and \widehat{P}_{F_i} can be approximated by relative frequencies. Let m be the number of \widehat{H}_1 , n be the number of \widehat{H}_0 . Let m_i and n_i be, respectively, the number of decisions made by the i th detector that conform to and contradict to the reliable fused decisions. Hence m , n , m_i and n_i can simply be obtained by counting in the simulations. That is,

$$\frac{m}{n} \approx \frac{P(\widehat{H}_1)}{P(\widehat{H}_0)}.$$

$$\frac{m_i}{n_i} \approx \begin{cases} \frac{P(u_i = +1, \widehat{H}_1)}{P(u_i = +1, \widehat{H}_0)}, & \text{if } u_i = +1, \\ \frac{P(u_i = -1, \widehat{H}_0)}{P(u_i = -1, \widehat{H}_1)}, & \text{if } u_i = -1. \end{cases} \quad (3.9)$$

We shall next develop the updating rule for the fusion center. From Eq.(2.19),

$$\widehat{w}_0 = \log \frac{P(\widehat{H}_1)}{P(\widehat{H}_0)}.$$

$$\widehat{w}_i = \begin{cases} \log \frac{P(u_i = +1 | \widehat{H}_1)}{P(u_i = +1 | \widehat{H}_0)}, & \text{if } u_i = +1, \\ \log \frac{P(u_i = -1 | \widehat{H}_0)}{P(u_i = -1 | \widehat{H}_1)}, & \text{if } u_i = -1. \end{cases}$$

Using the Bayes rule $P(x, y) = p(x|y)P(y)$,

$$\widehat{w}_i = \begin{cases} \log \frac{P(u_i = +1, \widehat{H}_1)P(\widehat{H}_0)}{P(u_i = +1, \widehat{H}_0)P(\widehat{H}_1)}, & \text{if } u_i = +1, \\ \log \frac{P(u_i = -1, \widehat{H}_0)P(\widehat{H}_1)}{P(u_i = -1, \widehat{H}_1)P(\widehat{H}_0)}, & \text{if } u_i = -1. \end{cases} \quad (3.10)$$

Applying Eq.(3.9) and Eq.(2.19) yields

$$\hat{w}_0 \approx \log \frac{m}{n}$$

$$\hat{w}_i \approx \begin{cases} \log \frac{m_i}{n_i} - \hat{w}_0, & \text{if } u_i = +1 \\ \log \frac{m_i}{n_i} + \hat{w}_0, & \text{if } u_i = -1 \end{cases} \quad (3.11)$$

and

$$m \approx \epsilon^{\hat{w}_0} n$$

$$m_i \approx -\frac{1}{n_i} = \begin{cases} e^{\hat{w}_i + \hat{w}_0} n_i, & \text{if } u_i = +1 \\ e^{\hat{w}_i - \hat{w}_0} n_i, & \text{if } u_i = -1 \end{cases} \quad (3.12)$$

Talking the partial derivative of Eq. (3.11) with respect to m_i and n_i , respectively.

$$\frac{\partial \hat{w}_0}{\partial m} \approx \frac{1}{m} \quad , \quad (3.13)$$

$$\frac{\partial \hat{w}_0}{\partial n} \approx -\frac{1}{n} = -\frac{1}{m} \epsilon^{\hat{w}_0}.$$

and

$$\frac{\partial \hat{w}_i}{\partial m_i} \approx \frac{1}{m_i}$$

$$\frac{\partial \hat{w}_i}{\partial n_i} \approx \begin{cases} -\frac{1}{m_i} \epsilon^{\hat{w}_i + \hat{w}_0}, & \text{when } u = +1 \\ -\frac{1}{m_i} \epsilon^{\hat{w}_i - \hat{w}_0}, & \text{when } u = -1 \end{cases} \quad (3.14)$$

If the current local detector's decision conforms to the reliable fusion, its weight \hat{w}_i should be reinforced. In this case,

$$\Delta \hat{w}_i \approx \frac{1}{m_i} \Delta m_i = \frac{1}{m_i} \quad (3.15)$$

On other hand, if the current local decision contradicts to the reliable decision, its weight \hat{w}_i should be reduced. That is,

$$\Delta \hat{w}_i \approx \begin{cases} -\frac{1}{n_i} \Delta n_i = -\frac{1}{m_i} \epsilon^{\hat{w}_i + \hat{w}_0} \Delta n_i = -\frac{1}{m_i} \epsilon^{\hat{w}_i + \hat{w}_0}, & \text{if } u = +1 \\ -\frac{1}{n_i} \Delta n_i = -\frac{1}{m_i} \epsilon^{\hat{w}_i - \hat{w}_0} \Delta n_i = -\frac{1}{m_i} \epsilon^{\hat{w}_i - \hat{w}_0}, & \text{if } u = -1 \end{cases} \quad (3.16)$$

and

$$\Delta \hat{w}_0 \approx \begin{cases} \frac{1}{m} \Delta m = \frac{1}{m} & \text{When } \widehat{H}_1 \text{ occurs} \\ -\frac{1}{n} \Delta n = -\frac{1}{m} e^{\hat{w}_0} \Delta n = -\frac{1}{m} e^{\hat{w}_0} & \text{When } \widehat{H}_0 \text{ occurs} \end{cases} \quad (3.17)$$

Thus, we obtain the following updating rule:

$$\hat{w}_i^+ = \hat{w}_i^- + \Delta \hat{w}_i, \quad i = 0, 1, 2, \dots \quad (3.18)$$

where \hat{w}_i^+ and \hat{w}_i^- represent the weight after and before each update. Since the steady state \hat{w}_i 's are what we are trying to compute, for actual implementation, we use the current estimated weight \hat{w}_i^- to compute $\Delta \hat{w}_i$. That is, to update the weights according to Eq.(3.18), $\Delta \hat{w}_i$ is computed according to the following table:

	\widehat{H}_1		\widehat{H}_1	
	$u = +1$	$u = -1$	$u = +1$	$u = -1$
$\Delta \hat{w}_0$	$\frac{1}{m_i}$		$-\frac{1}{m_i} e^{\hat{w}_0^-}$	
$\Delta \hat{w}_i$	$\frac{1}{m_i}$	$-\frac{1}{m_i} e^{\hat{w}_i^- - \hat{w}_0^-}$	$-\frac{1}{m_i} e^{\hat{w}_i^- + \hat{w}_0^-}$	$\frac{1}{m_i}$

3.2.1 Lemma VI

Using the updating rule according to Eq.(3.18) and the above table, \hat{w}_i^- will converge to the desired steady state estimate weight \hat{w}_i .

Proof:

At steady state,

$$E[\hat{w}_i^+ - \hat{w}_i^-] = 0 \quad (3.19)$$

Using the definition $E[X] = \sum x_i P(x_i)$ and the updating rule according to Eq.(3.18) and table, Eq.(3.19) becomes,

$$\frac{1}{m_i} P(u = +1, \widehat{H}_1) - \frac{1}{m_i} e^{\hat{w}_i^- + \hat{w}_0^-} P(u = +1, \widehat{H}_0) = 0$$

Using Eq.(3.10) for further simplification yields,

$$\widehat{w}_i^- + \widehat{w}_0^- = \widehat{w}_i + \widehat{w}_0. \quad (3.20)$$

Similarly, if $u = -1$, we have,

$$\widehat{w}_i^- - \widehat{w}_0^- = \widehat{w}_i - \widehat{w}_0. \quad (3.21)$$

For $i = 0$, the following condition can similarly be obtained at steady state:

$$\frac{1}{m} P(\widehat{H}_1) - \frac{1}{m} e^{\widehat{w}_0^-} P(\widehat{H}_0) = 0.$$

Thus,

$$\widehat{w}_0^- = \widehat{w}_0. \quad (3.22)$$

Hence, $\widehat{w}_i^- \rightarrow \widehat{w}_i$, for $i = 0, 1, \dots$.

□

CHAPTER 4
SIMULATION

Figure 4.1 shows the simulation set up to validate the proposed adaptive fusion model.

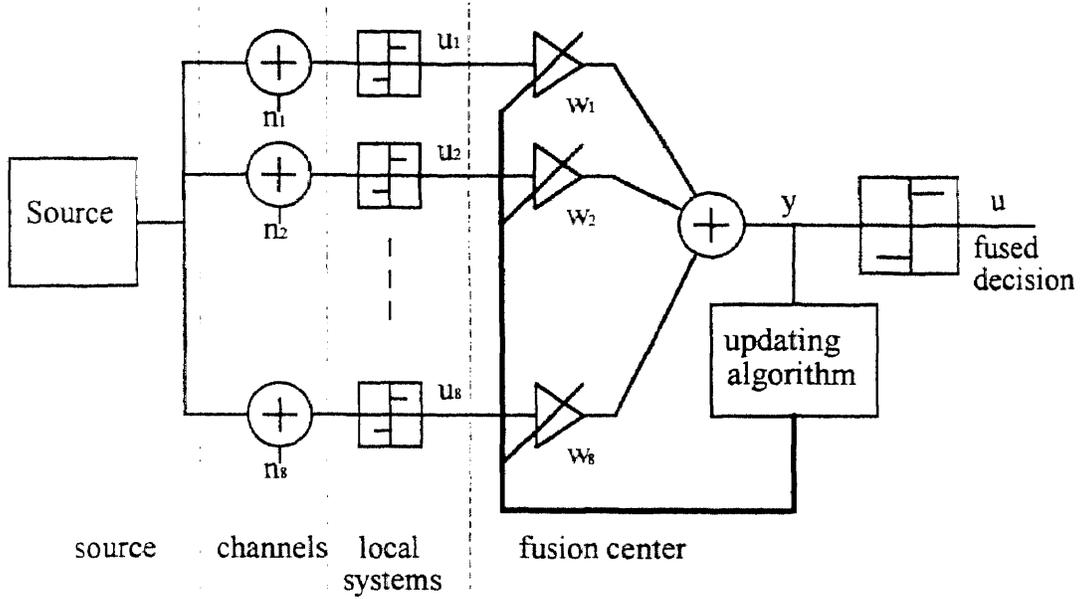


Figure 4.1 Computer simulation diagram

In this simulation, presented here, the source produces binary signal with $P(H_1) = 0.3$ and $P(H_0) = 0.7$, where $H_1 : +1$ and $H_0 : -1$. Eight sensors are used. The probabilities of false alarm and detection P_F and P_D of each sensor are fixed, but not known to the system. The channel is additive Gaussian noise. The Gaussian random variables are generated according to the following transformation,

$$\begin{cases} x = (-2 \ln r_1)^{1/2} \cos 2\pi r_2 \\ y = (-2 \ln r_1)^{1/2} \sin 2\pi r_2 \end{cases}$$

where r_1 and r_2 are uniformly distributed on $(0, 1]$, and (x, y) becomes a pair of orthogonal normalized *Gaussian* random variables. The additive Gaussian variable for each sensor is zero-mean with standard deviation ranged from 0.5 to 1.2.

4.1 Conditional Probability Mass Function of y

Figure 4.2 shows the histograms of $P(y = \zeta|H_0)$ and $P(y = \zeta|H_1)$ for 8 sensors and 250000 samples. We can see that the waveforms are not monotonic. Figure 4.3

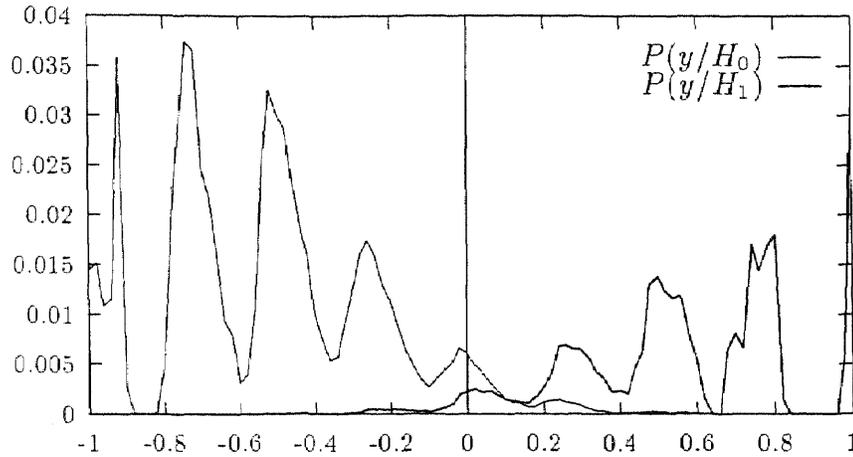


Figure 4.2 Probability mass functions $P(y/H_1)$ and $P(y/H_0)$

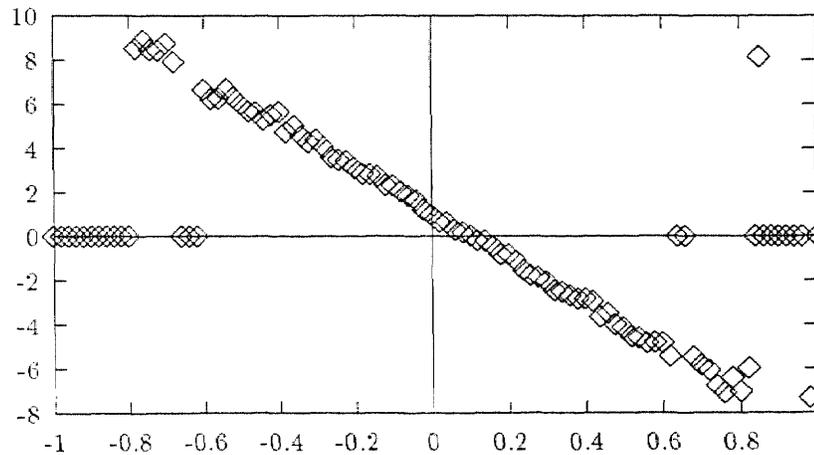


Figure 4.3 The log-ratio of probability mass functions $\log P(y/H_1)/P(y/H_0)$ shows $\ln \frac{P(y = \zeta|H_1)}{P(y = \zeta|H_0)}$. It is almost a straight line which conforms to Lemma I:

$$\epsilon^\zeta = \frac{P(y - w_0 = \zeta|H_1)}{P(y - w_0 = \zeta|H_0)}$$

4.2 Convergence of Weights

Figure 4.4 shows average errors of weights $|w_i - \hat{w}_i|$ for different τ , $\tau = 0, 0.5$, and 0.75 . As shown in the figure, the larger the τ , the smaller the error, which agrees with Lemma II. As the number of unreliable samples increases, the training time becomes longer.

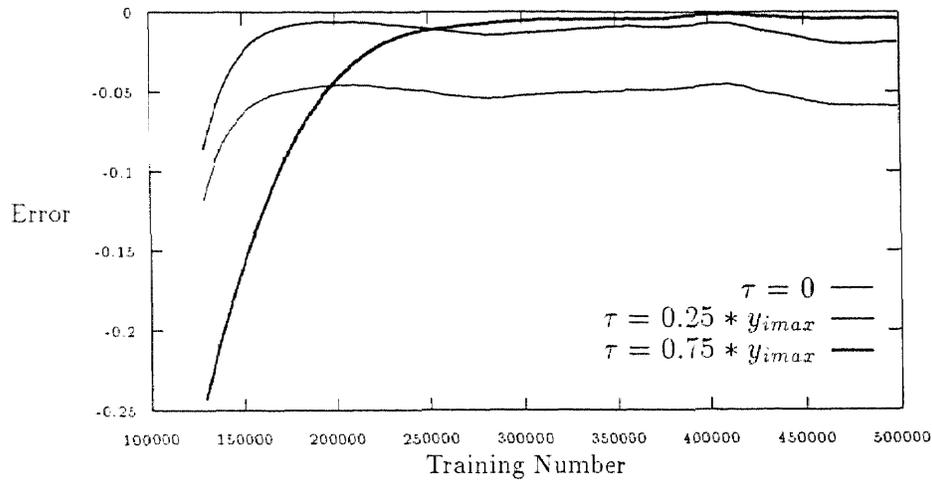


Figure 4.4 The error with different reliability threshold

CHAPTER 5

CONCLUSIONS

In the real-world environment, the probability mass functions of the observations at local detectors may not be known and the performance of the local detectors may not be consistent. Under such circumstances, a system which can adapt itself during the decision making process is needed. The major advantage is that the system can still have smaller error and does not need *a priori* knowledge of the probability density functions of the observations. Simulation results conform to our theoretical analysis.

APPENDIX A

SIMULATION PROGRAMS

```

/*****
    main.c
*****/
/* #define IBM_PC */
/* #define STATISTICS_OF_Y */
/* #define DEBUG */
/* #define DISPLAY_SOURCE */
#define SHOW_W_ADJ

#define CONVERGE

#define RunTime 350000
#define SanIntv 1000

#include <stdio.h>
#include <math.h>
#include "main.h"
#include "noise.h"
#include "sensor.h"

double Na[SensorNum],WO[SensorNum],W1[SensorNum],Wdc;
double Y,Ym1,Ym0,PH1=0.3;
int i,d,D,u[SensorNum];
long t,P1,P11[SensorNum],P10[SensorNum],P01[SensorNum],P00[SensorNum],Pe=0;

w_adj(T)
double T;
{
    int i,j;
    double B,s,y;
    static double delta=0.0001;

#ifdef SHOW_W_ADJ
    double yi[SensorNum];

    printf("source: H%d\tfusion decision=%d\ty=%.4f\ttao=%.4f\nu:\t",
           d,D,Y-Wdc,T);
    for(i=0; i<SensorNum; i++)
        printf("%d\t",u[i]);
    printf("\nWO:\t");
    for(i=0; i<SensorNum; i++)

```

```

        printf("%.4f\t",WO[i]);
        printf("\nW1:\t");
        for(i=0; i<SensorNum; i++)
            printf("%.4f\t",W1[i]);
        printf("\n\t");
#endif SHOW_W_ADJ

        for(i=0; i<SensorNum; i++){
            if( u[i] == 1 ){
/*          y = (Y-Wdc-W1[i])/(Ym1-W1[i]); */
                y = (2.*(Y-Wdc-W1[i])-(Ym1-Ym0-W1[i]))/(Ym1+Ym0-W1[i]);
                if( y > T ){
                    W1[i] += delta;
#ifdef SHOW_W_ADJ
                    printf("W1++\t");
#endif SHOW_W_ADJ
                }
                else if( y < -T ){
                    W1[i] -= exp(W1[i]+Wdc)*delta;
#ifdef SHOW_W_ADJ
                    printf("W1--\t");
#endif SHOW_W_ADJ
                }
#ifdef SHOW_W_ADJ
                else
                    printf("W1\t");
#endif SHOW_W_ADJ
            }
            else {
/*          y = (Y-Wdc+WO[i])/(Ym0-WO[i]); */
                y = (2.*(Y-Wdc+WO[i])-(Ym1-Ym0+WO[i]))/(Ym1+Ym0-WO[i]);
                if( y < -T ){
                    WO[i] += delta;
#ifdef SHOW_W_ADJ
                    printf("WO++\t");
#endif SHOW_W_ADJ
                }
                else if( y > T ){
                    WO[i] -= exp(WO[i]-Wdc)*delta;
#ifdef SHOW_W_ADJ
                    printf("WO--\t");
#endif SHOW_W_ADJ
                }
#ifdef SHOW_W_ADJ
                else
                    printf("W1\t");
#endif SHOW_W_ADJ
            }
        }

```

```

    }
#ifdef SHOW_W_ADJ
    yi[i] = y;
#endif SHOW_W_ADJ
} /* for i */

#ifdef SHOW_W_ADJ
printf("\nyi:\t");
for(i=0; i<SensorNum; i++)
    printf("%.4f\t",yi[i]);
printf("\n");
#endif SHOW_W_ADJ

    y = (2.*(Y-Wdc)-(Ym1-Ym0))/(Ym1+Ym0);

    if( y > T ){
        Wdc += delta;
#ifdef SHOW_W_ADJ
        printf("Wdc+\n\n");
#endif SHOW_W_ADJ
    }
    else if( y < -T ){
        Wdc -= exp(Wdc) * delta;
#ifdef SHOW_W_ADJ
        printf("Wdc+\n\n");
#endif SHOW_W_ADJ
    }
#ifdef SHOW_W_ADJ
    else
        printf("Wdc\n\n");
#endif SHOW_W_ADJ
}

void main(argc,argv)
int argc;
char **argv;
{
    double tmp_d,tmp_d1,tao=0;
    int tmp_i;

#ifdef STATISTICS_OF_Y
    long SY0[101],SY1[101];
    for(i=0; i<101; i++){
        SY0[i] = 0;
        SY1[i] = 0;
    }
#endif
}
#endif

```

```

if(argc>1) tao = atof(argv[1]);
if(argc>2) PH1 = atof(argv[2]);

/* initialize each weights */
for(i=0; i<SensorNum; i++){
    tmp_d = .4; /* initial probability for every weights */
    Na[i] = (double)i*0.1+.5;
    W1[i] = W0[i] = log((1.0-tmp_d)/tmp_d);
    P11[i] = P10[i] = P01[i] = P00[i] = 0;
}
Wdc = -1;
sensor_init();

printf("RunTime=%ld tao=%lf PH1=%lf\n", (long)RunTime, tao, PH1);

#ifdef CONVERGE
    printf("CONVERGE\n%ld %ld\n", (long)RunTime, (long)SanIntv);
#endif

for(t=1; t<=RunTime; t++){

    if((d = Data(PH1))==1) P1++;

#ifdef DISPLAY_SOURCE
    printf("%d", d);
    if(t%50 == 0) printf("\n");
#endif DISPLAY_SOURCE

#ifdef DEBUG
    printf("----- d=%d -----\nu=\t", d);
#endif DEBUG

    /* local decision */
    for(i=0; i<SensorNum; i++){
        u[i] = sensor( gausNoise(Na[i]) + d*2-1, i);

#ifdef DEBUG
        printf("%d\t", u[i]);
#endif DEBUG

    }

#ifdef DEBUG
    /* display weights */
    printf("\nW0=\t");

```

```

    for(i=0; i<SensorNum; i++)
        printf("%.4f\t",WO[i]);
    printf("\nW1=\t");
    for(i=0; i<SensorNum; i++)
        printf("%.4f\t",W1[i]);
    printf("\n");
#endif DEBUG

    /* fusion */
    for(i=0, Y=Wdc, Ym0=0, Ym1=0; i<SensorNum; i++){
        Ym1 += W1[i]; Ym0 += WO[i];
        if( u[i] == 1 ) Y += W1[i];
        else Y -= WO[i];
    }

#ifdef STATISTICS_OF_Y
    tmp_i = ((Y-Wdc)/Ym1+1.)*50;
    if( (tmp_i >=0) && (tmp_i<=100) ){
        if( d == 0 ) SY0[tmp_i]++;
        else SY1[tmp_i]++;
    }
#endif

    D = (Y>0)?1:0;

#ifdef DEBUG
    printf("Y=%.4f\t D=%d",Y,D);
#endif DEBUG

    w_adj(tao);

#ifdef DEBUG
    /* display weights */
    printf("\nWO=\t");
    for(i=0; i<SensorNum; i++)
        printf("%.4f\t",WO[i]);
    printf("\nW1=\t");
    for(i=0; i<SensorNum; i++)
        printf("%.4f\t",W1[i]);
    printf("\n\n");
#endif DEBUG

    if( D != d ) Pe++;
    for(i=0; i<SensorNum; i++ )
        if( ((u[i] == 1) && (d == 1)) P11[i]++;
        else if((u[i] == 0) && (d == 0)) P00[i]++;

```

```

        else if((u[i] == 1) && (d == 0)) P10[i]++;
        else                               P01[i]++;

#ifdef CONVERGE
    if( t%SanIntv == 0){
        printf("t=%ld\nWdc=%.4f\nWO:\t",t,Wdc);
        for(i=0; i<SensorNum; i++)
            printf("%.4f\t",WO[i]);
        printf("\nW1:\t");
        for(i=0; i<SensorNum; i++)
            printf("%.4f\t",W1[i]);
        tmp_d1 = (double)P1/(double)t;
        printf("\n-----\nWdc=%.4f\nWO:\t",log(tmp_d1/(1-tmp_d1)));
        for( i=0; i<SensorNum; i++){
            tmp_d =log((double)P00[i]/(double)P01[i]*tmp_d1/(1-tmp_d1));
            printf("%.4f\t",tmp_d);
        }
        printf("\nW1:\t");
        for( i=0; i<SensorNum; i++){
            tmp_d =log((double)P11[i]/(double)P10[i]*(1-tmp_d1)/tmp_d1);
            printf("%.4f\t",tmp_d);
        }
        printf("\n\n");
    }
#endif
    }
    printf("\nPE_DATA\n");

    printf("\nPe=%e\n",(double)Pe/RunTime);

#ifdef STATISTICS_OF_Y
    printf("\nSTAT_Y\n");
    for(i=0; i<101; i++)
        printf("%e %e %e %e\n", (float)(i-50)/50, (double)SY0[i]/RunTime,
            (float)(i-50)/50, (double)SY1[i]/RunTime );
#endif

#ifdef IBM_PC
    getch();
#endif
}
/*****
 *      noise.h
 *****/
#include <stdlib.h>
#ifdef _noise
#define _noise

```

```

#ifdef IBM_PC
#define RND (((double)rand()+1.)/32768.)
#else
#define RND (((double)rand()+1.)/2147483600.)
#endif

/* Data will generate 1 bit data. P(H1) = prob */
#define Data(prob) ((RND<prob)? 1:0)
double gausNoise(double sigma);/* gausNoise */

#endif _noise
/*****
 *      noise.h
 *****/
#include <stdlib.h>
#ifndef _noise
#define _noise

#ifdef IBM_PC
#define RND (((double)rand()+1.)/32768.)
#else
#define RND (((double)rand()+1.)/2147483600.)
#endif

/* Data will generate 1 bit data. P(H1) = prob */
#define Data(prob) ((RND<prob)? 1:0)
double gausNoise(double sigma);/* gausNoise */

#endif _noise
/*****
      sensor.c
 *****/
#include "main.h"
double T[SensorNum];

int sensor(double s,int no){

    if( s>T[no] ) return 1;
    else      return 0;
}

sensor_init(){
    int i;
    for(i=0; i<SensorNum; i++)
        T[i] = 0;
}

```

```
# *****  
# makefile  
# *****  
CC=gcc  
CFLAGS=-g  
  
SRCS= main.c noise.c sensor.c  
  
HDRS= main.h noise.h sensor.h  
  
OBJS= main.o noise.o sensor.o  
  
LIB= -lm  
  
all: main  
  
clean:  
rm -f $(TESTS) *.o *.ln *~  
  
main: $(OBJS) $(HDRS)  
$(CC) $(CFLAGS) -o $@ $(OBJS) $(LIB)  
  
bk:  
zip bk *.c *.h makefile  
tar:  
tar cvf - makefile *.c *.h | compress > bk.tar.Z
```

REFERENCES

1. R. R. Tenney and N. R. Sandell, Jr., "Detection With Distributed Sensors," *IEEE Trans. Aerosp. Electron. Syst.*, vol. AES-17, pp.501-510, July 1981.
2. F. A. Sadjadi, "Hypotheses Testing in a Distributed Environment," *IEEE Trans. Aerosp. Electron. Syst.*, vol. AES-22, pp.134-137, Mar. 1986.
3. Z. Chair and P. K. Varshney, "Optimal Data Fusion in Multiple Sensor Detection Systems," *IEEE Trans. Aerosp. Electron. Syst.*, vol. AES-22, no.1, pp.98-101, Jan. 1986.
4. S. C. A. Thomopoulos, R. Viswanathan, and D. C. Bougoulas, "Optimal Decision Fusion in Multiple Sensor Systems," *IEEE Trans. Aerosp. Electron. Syst.*, vol. AES-23, pp.644-653, Sept. 1987.
5. K. Demirbas. "Maximum a posteriori Approach to Object Recognition With Distributed Sensors," *IEEE Trans. Aerosp. Electron. Syst.*, vol. AES-24, pp.309-313, May 1988.
6. B. Zhu, N. Ansari, E. Hou. "An Adaptive Fusion Model for Distributed Detection Systems," *Proceedings of SPIE, Sensor Fusion V*, vol. 1828, November 15-20, 1992, Boston, MA, pp.332-341.
7. J. L. Melsa and D. L. Cohn, Decision and Estimation Theory. McGraw-Hill Book Company.
8. J. M. Zmada. Introduction to Artificial Neural Systems, St. Paul, MN: West Publishing Company, 1992.
9. R. Hecht-Nielsen, Neurocomputing. Reading, MA: Addison Wesley, 1990.
10. J. A. Hertz Introduction to The Theory of Neural Computation. Reading, MA: Addison Wesley, 1991.
11. B. Kosko, Neural Networks and Fuzzy Systems. Englewood Cliffs, NJ: Prentice Hall, 1992.