AP Calculus AB

Trigonometry Review and Application

Be sure to show your work wherever possible. NO CALCULATORS are necessary for this.

- 1. cos(x) = sin(?)
- 2. Multiply every term in the equation $1 + \cot^2 x = \csc^2 x$ by $\sin^2 x$. Simplify. How is the new equation related to the coordinates of a point on the unit circle?
- 3. Show that $\frac{d}{dx}(\sec x) = \sec(x)\tan(x)$ using only the derivative of cosine.
- 4. Is the trigonometric function in the brackets positive or negative?

a) $\sin(-x) = [?\sin(x)]$	b) $\tan(-x) = [? \tan(x)]$	c) $\operatorname{sec}(-x) = [? \operatorname{sec}(x)]$
d) $\cot(-x) = [?\cot(x)]$	e) $\csc(-x) = [?\csc(x)]$	f) $\cos(-x) = [?\cos(x)]$

- 5. Restrict the <u>range</u> of the following trigonometric relations to make them functions. (Principle branches)
- a) $y = \arcsin(x)$

b) $y = \arccos(x)$

c) $y = \arctan(x)$

Back to the AP Exam:

Answer each question and provide a *justification* for your answer. Years for each question are given.

1993

- 13. The fundamental period of $2\cos(3x)$ is
 - (A) $\frac{2\pi}{3}$
- (B) 2π
- (C) 6π
- (D) 2
- (E) 3

32. Which of the following does NOT have a period of π ?

(A)
$$f(x) = \sin\left(\frac{1}{2}x\right)$$

(B)
$$f(x) = |\sin x|$$

(C)
$$f(x) = \sin^2 x$$

(D)
$$f(x) = \tan x$$

(E)
$$f(x) = \tan^2 x$$

Justification:

1988

$$35. \quad 4\cos\left(x+\frac{\pi}{3}\right) =$$

- (A) $2\sqrt{3}\cos x 2\sin x$
- (B) $2\cos x 2\sqrt{3}\sin x$ (C) $2\cos x + 2\sqrt{3}\sin x$

- (D) $2\sqrt{3}\cos x + 2\sin x$
- (E) $4\cos x + 2$

Justification:

1993

- The position of a particle moving along the x-axis is $x(t) = \sin(2t) \cos(3t)$ for time $t \ge 0$. 12. When $t = \pi$, the acceleration of the particle is
 - (A) 9
- (B) $\frac{1}{9}$
- (C) 0
- (D) $-\frac{1}{9}$ (E) -9

- 79. The position of an object attached to a spring is given by $y(t) = \frac{1}{6}\cos(5t) \frac{1}{4}\sin(5t)$, where t is time in seconds. In the first 4 seconds, how many times is the velocity of the object equal to 0?
 - (A) Zero
 - Three (B)
 - (C) Five
 - Six (D)
 - (E) Seven

Justification:

1988

- The $\lim_{h\to 0} \frac{\tan 3(x+h) \tan 3x}{h}$ is
 - (A) 0
- (B) $3\sec^2(3x)$ (C) $\sec^2(3x)$
- (D) $3\cot(3x)$
- (E) nonexistent

Justification:

1993

29.
$$\lim_{\theta \to 0} \frac{1 - \cos \theta}{2 \sin^2 \theta}$$
 is

- (A) 0
- (B) $\frac{1}{8}$ (C) $\frac{1}{4}$
- (D) 1
- (E) nonexistent

1993

10. If $f(x) = (x-1)^2 \sin x$, then f'(0) =

- (A) -2
- (B) -1
- (C) 0
- (D) 1
- (E) 2

Justification:

1993

If $y = \tan x - \cot x$, then $\frac{dy}{dx} =$

- (A) $\sec x \csc x$ (B) $\sec x \csc x$ (C) $\sec x + \csc x$ (D) $\sec^2 x \csc^2 x$ (E) $\sec^2 x + \csc^2 x$

Justification:

1997

7.
$$\frac{d}{dx}\cos^2(x^3) =$$

- (A) $6x^2\sin(x^3)\cos(x^3)$
- (B) $6x^2 \cos(x^3)$
- (C) $\sin^2(x^3)$
- (D) $-6x^2 \sin(x^3) \cos(x^3)$
- (E) $-2\sin(x^3)\cos(x^3)$

10. An equation of the line tangent to the graph of $y = \cos(2x)$ at $x = \frac{\pi}{4}$ is

(A)
$$y-1=-\left(x-\frac{\pi}{4}\right)$$

(B)
$$y-1=-2\left(x-\frac{\pi}{4}\right)$$

(C)
$$y = 2\left(x - \frac{\pi}{4}\right)$$

(D)
$$y = -\left(x - \frac{\pi}{4}\right)$$

(E)
$$y = -2\left(x - \frac{\pi}{4}\right)$$

Justification:

1988

4. If u, v, and w are nonzero differentiable functions, then the derivative of $\frac{uv}{w}$ is

(A)
$$\frac{uv' + u'v}{w'}$$

(B)
$$\frac{u'v'w - uvw'}{w^2}$$

(C)
$$\frac{uvw' - uv'w - u'vw}{w^2}$$

(D)
$$\frac{u'vw + uv'w + uvw'}{w^2}$$

(E)
$$\frac{uv'w + u'vw - uvw'}{w^2}$$