## STP 226

## EXAM \#3 A

Material from chapters 7-9
Honor Statement:
I have neither given nor received information regarding this exam, and I will not do so until all exams have been graded and returned.

Signed $\qquad$
Date $\qquad$

## PRINTED NAME

> CLASS TIME

## DIRECTIONS:

This is a closed book examination. You may use one 4X6 or smaller note card with hand written notes and a graphing calculator.
Formulas, z -tables and t -tables are included at the end of the test.
Part one has 3 questions for which you need to provide complete and well-organized answers. Include sketches as requested to explain your answers. Round up all answers to required decimal places. Part two consists of 8 multiple choice questions and part 3 consists of 8 true-false statements. Place answers to the multiple choice and true-false questions in the tables below. You can earn 104 points (4 points are extra credit points ).

## RELAX and Good Luck!

Place answers to multiple choice questions below, use letters A-E as appropriate

| Question number | $\# 4$ | $\# 5$ | $\# 6$ | $\# 7$ | $\# 8$ | $\# 9$ | $\# 10$ | \#11 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Answer: |  |  |  |  |  |  |  |  |

Place answers to true-false statements below, circle T or F as appropriate

| Statement number | $\# 1$ | $\# 2$ | $\# 3$ | $\# 4$ |  | $\# 5$ |  | $\# 6$ |  | $\# 7$ |  | $\# 8$ |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Answer (circle one) | T | F | T | F | T | F | T | F | T | F | T | F | T | F |

## STUDENT IS ALLOWED A NOTE CARD

Part one. Show all work for questions \#1-\#3 Question \#1 (15 points) Water Taxi Safety
A water taxi sank in Baltimore's Inner Harbor, because it was overloaded. An investigation revealed that the safe passenger load 3500 pounds and it was exceeded that day. Based on the data from National Health survey weights of American men have a normal distribution with a mean $\mu=172$ pounds and a standard deviation $\sigma=29$ pounds. Suppose the water taxi is boarded by 20 randomly selected men and $\bar{x}$ is their average weight.
a) Indicate what the sampling distribution is of $\bar{X}$ for samples of size 20, give the mean and SD of that distribution, round your answers to 3 decimal places as needed.
The Distribution shape is: $\qquad$
Mean= $\qquad$ $\mathrm{SD}=$ $\qquad$
b) Find the probability that $\bar{x}$ will be larger than 175 (so that their total weight exceeds safety capacity of 3500 pounds)
$\mathrm{P}(\bar{x}>175)=$ $\qquad$

## Question \#2 (15 points) Perception of Time

Randomly selected STP226 students participated in an experiment to test their ability to determine when $1 \mathrm{~min}(60 \mathrm{sec})$ had passed. Forty students yielded a sample mean of 58.3 sec . Assume that $\sigma=9.5 \mathrm{sec}$.
a) Construct a $95 \%$ confidence interval of the population mean of all STP 226 students. Clearly show all work by hand. Give 3 decimal places.
b) Based on the results in part a), is it likely that the true population mean is reasonably close to 60 second? Explain your answer.

$$
\text { YES } \quad \text { NO } \quad \text { ( circle one })
$$

Explanation: $\qquad$
c) What sample size is needed for the margin of error in the CI you computed in part a to be no more then 1.5 seconds?

ANSWER $\qquad$

## Question\#3 (10points)

Suppose you are testing hypotheses: $\mathrm{H}_{0}: \mu=8$ versus $\mathrm{H}_{\mathrm{a}}: \mu<8$, you are using a z-test and your test statistics is $\mathrm{z}=-1.57$. Use tables to compute the $\mathbf{p}$ - value for your test, include appropriate sketch illustrating your computation. Give 4 decimal places.

Sketch: $\qquad$ p-value: $\qquad$
Part two: Multiple choice questions. Select one from A to E as appropriate. (5 points each)
Use following information for Questions \#4-\#8

## Red Blood cell count

A simple random sample of 30 US adults is obtained and each person's red blood cell count (in cells per microliter) is measured. A sample mean is 4.63 . Let $\mu$ be a mean blood cell count for all US adults.

Question \#4 Suppose the population standard deviation for red blood cell count is 0.54 . Compute a Margin of Error in $95.44 \%$ confidence interval for $\mu$. Round your answer to 4 decimal places.
A) 1.6906
B) 0.1972
C) 0.0986
D) 0.0180
E) none of these

Question\#5 Suppose population standard deviation for red blood cell count is 0.54 and you want to test at $5 \%$ significance level the following hypotheses:
$\mathrm{H}_{0}: \mu=4.5$ versus $\mathrm{H}_{\mathrm{a}}: \mu \neq 4.5$ using a z-test. Select critical value(s) for the rejection region for your test:
(A) $\pm 1.645$
(B) $\pm 2$
(C) 1.645
(D) $\pm 1.96$
(E) none of these

Question\#6: Suppose the p-value for your test you conducted in previous question (\#5) was 0.1873 , what is the conclusion for your test at $5 \%$ significance level? Select one of the answers below:
(A) Reject $H_{0}$, we have no evidence for $H_{a}$ at $\alpha=0.05$
(B) Do not reject $H_{0}$, we have no evidence for $H_{a}$ at $\alpha=0.05$
(C) Reject $H_{0}$, we have evidence for $H_{a}$ at $\alpha=0.05$
(D) Do not reject $H_{0}$, we have evidence for $H_{a}$ at $\alpha=0.05$

Question \#7 Suppose the population standard deviation is unknown, but a sample standard deviation is given. If you wanted to compute $90 \%$ confidence interval for $\mu$ and use a t-interval procedure, what is the appropriate $t$-value you need to use in computing of a margin of error in your confidence interval, give appropriate degrees of freedom.
A) $\mathrm{df}=29, \mathrm{t}=1.699$
B) $\mathrm{df}=30, \mathrm{t}=1.310$
C) $\mathrm{df}=29, \mathrm{t}=1.311$
D) $\mathrm{df}=30, \mathrm{t}=1.697$
E) none of these

Question \#8 Suppose $95 \%$ confidence interval for $\mu$ is: (4.44, 4.82 ). Based on that interval do you think it is reasonable to assume that $\mu$ is close to 4 cells per microliter?? Select appropriate answer from the following:
A) No, because CI is above 4 cells per microliter
B) Yes, because CI is above 4 cells per microliter
C) Yes, because sample mean was above 4 cells per microliter
D) No, because lower endpoint of CI is only a little above 4 cells per microliter
E) Not enough information

## Use following Information for Questions \#9-\#11

 California SpeedingA simple random sample of 40 recorded speeds (in $\mathrm{mi} / \mathrm{hr}$ ) is obtained from cars traveling on section of Highway 405 in Los Angeles. The sample has a mean of $68.4 \mathrm{mi} / \mathrm{hr}$ and a population standard deviation of $5.7 \mathrm{mi} / \mathrm{hr}$. We want to test if there is evidence at $1 \%$ significance level that the mean speed of all cars on that section of Highway $405(\mu)$ is greater than a posted limit of $65 \mathrm{mi} / \mathrm{hr}$ ?
Question\#9: State appropriate null and alternative hypotheses, use appropriate symbolic notation.
(A) $H_{0}: \mu=65 H_{a}: \mu \neq 65$
(B) $H_{0}: \mu<65 H_{a}: \mu>65$
(C) $H_{0}: \mu=68.4 H_{a}: \mu>65$
(D) $H_{0}: \mu=65 H_{a}: \mu>65$
(E) $H_{0}: \mu \neq 65 H_{a}: \mu=68.4$

Question\#10: Compute the appropriate test statistics, round your answer to 2 decimal places
(A) $\mathrm{z}=3.77$
(B) $\mathrm{z}=2.33$
$(\mathrm{C}) \mathrm{z}=-3.77$
(D) $\mathrm{z}=-2.33$
(E) none of these

Question\#11: Suppose null hypothesis was rejected at $1 \%$ significance level. In that case give the answer to the question posed in the problem.
(A) There is no sufficient evidence at $\alpha=0.01$ that the mean speed of all cars on that section of Highway $405(\mu)$ is greater than a posted limit of $65 \mathrm{mi} / \mathrm{hr}$.
(B) There is sufficient evidence at $\alpha=0.01$ that the mean speed of all cars on that section of Highway $405(\mu)$ is greater than a posted limit of $65 \mathrm{mi} / \mathrm{hr}$.
(C) There is sufficient evidence at $\alpha=0.01$ that the mean speed of all cars on that section of Highway $405(\mu)$ is not greater than a posted limit of $65 \mathrm{mi} / \mathrm{hr}$.
(D)There is no sufficient evidence at $\alpha=0.01$ that the mean speed of all cars on that section of Highway $405(\mu)$ is equal to a posted limit of $65 \mathrm{mi} / \mathrm{hr}$.

Part three: TRUE- FALSE questions (3 points each). Decide if each of the following statements is True or False.

Statement\#1 Suppose 90\% confidence interval for a mean age of participants in a large mathematical conference, based on a random sample of 120 participants, is $(35,49)$. We can say that $90 \%$ of all participants in that mathematical conference are between 35 and 49 years old.

## True False

Statement\#2 Suppose the mean annual income for adult women in one city is $\$ 28,520$ with standard deviation of $\$ 5190$ and the distribution is extremely left skewed. For the samples of size 69 , sample mean $\bar{x}$ has approximately normal distribution.

## True False

Statement\#3 If we compute $95 \%$ and $90 \%$ confidence intervals for the mean final exam score of all Mat 117 students at ASU last semester, then $90 \%$ confidence interval will be wider than $95 \%$ confidence interval.

True False

Statement\#4 In testing hypothesis null hypothesis will be rejected if p -value for the test is greater than selected significance level $\alpha$.

## True False

Statement\#5 If we test $\mathrm{H}_{0}: \mu=18$ versus $\mathrm{H}_{\mathrm{a}}: \mu \neq 18$ and $\mathrm{H}_{0}$ is rejected, but later a mega study concluded that $\mu=22$, then by rejecting $\mathrm{H}_{0}$ we committed Type I error.

True False
Statement\#6 If test statistics falls outside of the rejection region, we reject null hypothesis.

True False

Statement\#7 Suppose we conducted a z-test of the following hypotheses: $\mathrm{H}_{0}: \mu=8$ versus $\quad H_{a}: \mu \neq 8$ and we rejected null hypothesis at $5 \%$ significance level. In that case $95 \%$ confidence interval for $\mu$ computed from the same data would contain 8.

True False

Statement\#8 If p-value for the right tailed z-test test is 0.032 , then p -value for the two tailed z test is 0.064 .

True False

## FORMULAS

Sampling Distribution of $\bar{X}: \mu_{\bar{x}}=\mu, \sigma_{\bar{x}}=\frac{\sigma}{\sqrt{n}}$,
Standardized version of $\bar{X}: z=\frac{\bar{z}-\mu}{\sigma / \sqrt{n}}$

Studentized version of $\bar{X}: t=\frac{\bar{x}-\mu}{\frac{s}{\sqrt{n}}}$

Confidence Intervals for , Confidence level C $=(1-\alpha) * 100 \%$

Z-interval: $\bar{x} \pm z_{\alpha / 2} \frac{\sigma}{\sqrt{n}}$ Margin of error: $E=z_{\alpha / 2} \frac{\sigma}{\sqrt{n}}$
t -interval: $\bar{x} \pm t_{\alpha / 2} \frac{s}{\sqrt{n}}, d f=n-1$,
Sample size estimation: $n=\left(\frac{z_{\alpha / z} \sigma}{E}\right)^{2}$

## Hypothesis test for one Population Mean

$H_{0}: \mu=\mu_{0}$ vs $H_{a}: \mu \neq \mu_{0}$ or $H_{a}: \mu>\mu_{0}$ or $H_{a}: \mu<\mu_{0}$

Z-test ( $\sigma$ known): test statistics: $z=\frac{\bar{z}-\mu_{0}}{\sigma / \sqrt{n}}$
t-test ( $\sigma$ unknown): test statistics: $t=\frac{\bar{x}-\mu_{0}}{s / \sqrt{n}}, d f=n-1$

STUDENT IS ALLOWED A NOTE CARD

| TABLE IV <br> Values of $t_{\omega}$ | df | $t_{0.10}$ | $t_{0.05}$ | $t_{0.025}$ | $t_{0.01}$ | $t_{0.005}$ | df |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1 | 3.078 | 6.314 | 12.706 | 31.821 | 63.657 | 1 |
|  | 2 | 1.886 | 2.920 | 4.303 | 6.965 | 9.925 | 2 |
|  | 3 | 1.638 | 2.353 | 3.182 | 4.541 | 5.841 | 3 |
|  | 4 | 1.533 | 2.132 | 2.776 | 3.747 | 4.604 | 4 |
| $0 \mathrm{ta}_{\text {a }}$ | 5 | 1.476 | 2.015 | 2.571 | 3.365 | 4.032 | 5 |
|  | 6 | 1.440 | 1.943 | 2.447 | 3.143 | 3.707 | 6 |
|  | 7 | 1.415 | 1.895 | 2.365 | 2.998 | 3.499 | 7 |
|  | 8 | 1.397 | 1.860 | 2.306 | 2.896 | 3.355 | 8 |
|  | 9 | 1.383 | 1.833 | 2.262 | 2.821 | 3.250 | 9 |
|  | 10 | 1.372 | 1.812 | 2.228 | 2.764 | 3.169 | 10 |
|  | 11 | 1.363 | 1.796 | 2.201 | 2.718 | 3.106 | 11 |
|  | 12 | 1.356 | 1.782 | 2.179 | 2.681 | 3.055 | 12 |
|  | 13 | 1.350 | 1.771 | 2.160 | 2.650 | 3.012 | 13 |
|  | 14 | 1.345 | 1.761 | 2.145 | 2.624 | 2.977 | 14 |
|  | 15 | 1.341 | 1.753 | 2.131 | 2.602 | 2.947 | 15 |
|  | 16 | 1.337 | 1.746 | 2.120 | 2.583 | 2.921 | 16 |
|  | 17 | 1.333 | 1.740 | 2.110 | 2.567 | 2.898 | 17 |
|  | 18 | 1.330 | 1.734 | 2.101 | 2.552 | 2.878 | 18 |
|  | 19 | 1.328 | 1.729 | 2.093 | 2.539 | 2.861 | 19 |
|  | 20 | 1.325 | 1.725 | 2.086 | 2.528 | 2.845 | 20 |
|  | 21 | 1.323 | 1.721 | 2.080 | 2.518 | 2.831 | 21 |
|  | 22 | 1.321 | 1.717 | 2.074 | 2.508 | 2.819 | 22 |
|  | 23 | 1.319 | 1.714 | 2.069 | 2.500 | 2.807 | 23 |
|  | 24 | 1.318 | 1.711 | 2.064 | 2.492 | 2.797 | 24 |
|  | 25 | 1.316 | 1.708 | 2.060 | 2.485 | 2.787 | 25 |
|  | 26 | 1.315 | 1.706 | 2.056 | 2.479 | 2.779 | 26 |
|  | 27 | 1.314 | 1.703 | 2.052 | 2.473 | 2.771 | 27 |
|  | 28 | 1.313 | 1.701 | 2.048 | 2.467 | 2.763 | 28 |
|  | 29 | 1.311 | 1.699 | 2.045 | 2.462 | 2.756 | 29 |
|  | 30 | 1.310 | 1.697 | 2.042 | 2.457 | 2.750 | 30 |
|  | 31 | 1.309 | 1.696 | 2.040 | 2.453 | 2.744 | 31 |
|  | 32 | 1.309 | 1.694 | 2.037 | 2.449 | 2.738 | 32 |
|  | 33 | 1.308 | 1.692 | 2.035 | 2.445 | 2.733 | 33 |
|  | 34 | 1.307 | 1.691 | 2.032 | 2.441 | 2.728 | 34 |
|  | 35 | 1.306 | 1.690 | 2.030 | 2.438 | 2.724 | 35 |
|  | 36 | 1.306 | 1.688 | 2.028 | 2.434 | 2.719 | 36 |
|  | 37 | 1.305 | 1.687 | 2.026 | 2.431 | 2.715 | 37 |
|  | 38 | 1.304 | 1.686 | 2.024 | 2.429 | 2.712 | 38 |
|  | 39 | 1.304 | 1.685 | 2.023 | 2.426 | 2.708 | 39 |
|  | 40 | 1.303 | 1.684 | 2.021 | 2.423 | 2.704 | 40 |
|  | 41 | 1.303 | 1.683 | 2.020 | 2.421 | 2.701 | 41 |
|  | 42 | 1.302 | 1.682 | 2.018 | 2.418 | 2.698 | 42 |
|  | 43 | 1.302 | 1.681 | 2.017 | 2.416 | 2.695 | 43 |
|  | 44 | 1.301 | 1.680 | 2.015 | 2.414 | 2.692 | 44 |
|  | 45 | 1.301 | 1.679 | 2.014 | 2.412 | 2.690 | 45 |
|  | 46 | 1.300 | 1.679 | 2.013 | 2.410 | 2.687 | 46 |
|  | 47 | 1.300 | 1.678 | 2.012 | 2.408 | 2.685 | 47 |
|  | 48 | 1.299 | 1.677 | 2.011 | 2.407 | 2.682 | 48 |
|  | 49 | 1.299 | 1.677 | 2.010 | 2.405 | 2.680 | 49 |

STUDENT IS ALLOWED A NOTE CARD

| TABLE IV (cont.) Values of $t_{\alpha}$ | df | $t_{0.10}$ | $t_{0.05}$ | $t_{0.025}$ | $t_{0.01}$ | $t_{0.005}$ | df |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 50 | 1.299 | 1.676 | 2.009 | 2.403 | 2.678 | 50 |
|  | 51 | 1.298 | 1.675 | 2.008 | 2.402 | 2.676 | 51 |
|  | 52 | 1.298 | 1.675 | 2.007 | 2.400 | 2.674 | 52 |
|  | 53 | 1.298 | 1.674 | 2.006 | 2.399 | 2.672 | 53 |
|  | 54 | 1.297 | 1.674 | 2.005 | 2.397 | 2.670 | 54 |
|  | 55 | 1.297 | 1.673 | 2.004 | 2.396 | 2.668 | 55 |
|  | 56 | 1.297 | 1.673 | 2.003 | 2.395 | 2.667 | 56 |
|  | 57 | 1.297 | 1.672 | 2.002 | 2.394 | 2.665 | 57 |
|  | 58 | 1.296 | 1.672 | 2.002 | 2.392 | 2.663 | 58 |
|  | 59 | 1.296 | 1.671 | 2.001 | 2.391 | 2.662 | 59 |
|  | 60 | 1.296 | 1.671 | 2.000 | 2.390 | 2.660 | 60 |
|  | 61 | 1.296 | 1.670 | 2.000 | 2.389 | 2.659 | 61 |
|  | 62 | 1.295 | 1.670 | 1.999 | 2.388 | 2.657 | 62 |
|  | 63 | 1.295 | 1.669 | 1.998 | 2.387 | 2.656 | 63 |
|  | 64 | 1.295 | 1.669 | 1.998 | 2.386 | 2.655 | 64 |
|  | 65 | 1.295 | 1.669 | 1.997 | 2.385 | 2.654 | 65 |
|  | 66 | 1.295 | 1.668 | 1.997 | 2.384 | 2.652 | 66 |
|  | 67 | 1.294 | 1.668 | 1.996 | 2.383 | 2.651 | 67 |
|  | 68 | 1.294 | 1.668 | 1.995 | 2.382 | 2.650 | 68 |
|  | 69 | 1.294 | 1.667 | 1.995 | 2.382 | 2.649 | 69 |
|  | 70 | 1.294 | 1.667 | 1.994 | 2.381 | 2.648 | 70 |
|  | 71 | 1.294 | 1.667 | 1.994 | 2.380 | 2.647 | 71 |
|  | 72 | 1.293 | 1.666 | 1.993 | 2.379 | 2.646 | 72 |
|  | 73 | 1.293 | 1.666 | 1.993 | 2.379 | 2.645 | 73 |
|  | 74 | 1.293 | 1.666 | 1.993 | 2.378 | 2.644 | 74 |
|  | 75 | 1.293 | 1.665 | 1.992 | 2.377 | 2.643 | 75 |
|  | 80 | 1.292 | 1.664 | 1.990 | 2.374 | 2.639 | 80 |
|  | 85 | 1.292 | 1.663 | 1.988 | 2.371 | 2.635 | 85 |
|  | 90 | 1.291 | 1.662 | 1.987 | 2.368 | 2.632 | 90 |
|  | 95 | 1.291 | 1.661 | 1.985 | 2.366 | 2.629 | 95 |
|  | 100 | 1.290 | 1.660 | 1.984 | 2.364 | 2.626 | 100 |
|  | 200 | 1.286 | 1.653 | 1.972 | 2.345 | 2.601 | 200 |
|  | 300 | 1.284 | 1.650 | 1.968 | 2.339 | 2.592 | 300 |
|  | $400$ | 1.284 | 1.649 | 1.966 | 2.336 | 2.588 | 400 |
|  | 500 | 1.283 | 1.648 | 1.965 | 2.334 | 2.586 | 500 |
|  | 600 | 1.283 | 1.647 | 1.964 | 2.333 | 2.584 | 600 |
|  | 700 | 1.283 | 1.647 | 1.963 | 2.332 | 2.583 | 700 |
|  | 800 | 1.283 | 1.647 | 1.963 | 2.331 | 2.582 | 800 |
|  | 900 | 1.282 | 1.647 | 1.963 | 2.330 | 2.581 | 900 |
|  | 1000 | 1.282 | 1.646 | 1.962 | 2.330 | 2.581 | 1000 |
|  | 2000 | 1.282 | 1.646 | 1.961 | 2.328 | 2.578 | 2000 |
|  |  | 1.282 | 1.645 | 1.960 | 2.326 | 2.576 |  |
|  |  | $z_{0.10}$ | $z_{0.05}$ | $z_{0.025}$ | $z_{0.01}$ | $z_{0.005}$ |  |

## STUDENT IS ALLOWED A NOTE CARD

## Standard Normal Cumulative Probability Table

Cumulative probabilities for POSITIVE z-values are shown in the following table:


| z | 0.00 | 0.01 | 0.02 | 0.03 | 0.04 | 0.05 | 0.06 | 0.07 | 0.08 | 0.09 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.0 | 0.5000 | 0.5040 | 0.5080 | 0.5120 | 0.5160 | 0.5199 | 0.5239 | 0.5279 | 0.5319 | 0.5359 |
| 0.1 | 0.5398 | 0.5438 | 0.5478 | 0.5517 | 0.5557 | 0.5596 | 0.5636 | 0.5675 | 0.5714 | 0.5753 |
| 0.2 | 0.5793 | 0.5832 | 0.5871 | 0.5910 | 0.5948 | 0.5987 | 0.6026 | 0.6064 | 0.6103 | 0.6141 |
| 0.3 | 0.6179 | 0.6217 | 0.6255 | 0.6293 | 0.6331 | 0.6368 | 0.6406 | 0.6443 | 0.6480 | 0.6517 |
| 0.4 | 0.6554 | 0.6591 | 0.6628 | 0.6664 | 0.6700 | 0.6736 | 0.6772 | 0.6808 | 0.6844 | 0.6879 |
| 0.5 | 0.6915 | 0.6950 | 0.6985 | 0.7019 | 0.7054 | 0.7088 | 0.7123 | 0.7157 | 0.7190 | 0.7224 |
| 0.6 | 0.7257 | 0.7291 | 0.7324 | 0.7357 | 0.7389 | 0.7422 | 0.7454 | 0.7486 | 0.7517 | 0.7549 |
| 0.7 | 0.7580 | 0.7611 | 0.7642 | 0.7673 | 0.7704 | 0.7734 | 0.7764 | 0.7794 | 0.7823 | 0.7852 |
| 0.8 | 0.7881 | 0.7910 | 0.7939 | 0.7967 | 0.7995 | 0.8023 | 0.8051 | 0.8078 | 0.8106 | 0.8133 |
| 0.9 | 0.8159 | 0.8186 | 0.8212 | 0.8238 | 0.8264 | 0.8289 | 0.8315 | 0.8340 | 0.8365 | 0.8389 |
| 1.0 | 0.8413 | 0.8438 | 0.8461 | 0.8485 | 0.8508 | 0.8531 | 0.8554 | 0.8577 | 0.8599 | 0.8621 |
| 1.1 | 0.8643 | 0.8665 | 0.8686 | 0.8708 | 0.8729 | 0.8749 | 0.8770 | 0.8790 | 0.8810 | 0.8830 |
| 1.2 | 0.8849 | 0.8869 | 0.8888 | 0.8907 | 0.8925 | 0.8944 | 0.8962 | 0.8980 | 0.8997 | 0.9015 |
| 1.3 | 0.9032 | 0.9049 | 0.9066 | 0.9082 | 0.9099 | 0.9115 | 0.9131 | 0.9147 | 0.9162 | 0.9177 |
| 1.4 | 0.9192 | 0.9207 | 0.9222 | 0.9236 | 0.9251 | 0.9265 | 0.9279 | 0.9292 | 0.9306 | 0.9319 |
| 1.5 | 0.9332 | 0.9345 | 0.9357 | 0.9370 | 0.9382 | 0.9394 | 0.9406 | 0.9418 | 0.9429 | 0.9441 |
| 1.6 | 0.9452 | 0.9463 | 0.9474 | 0.9484 | 0.9495 | 0.9505 | 0.9515 | 0.9525 | 0.9535 | 0.9545 |
| 1.7 | 0.9554 | 0.9564 | 0.9573 | 0.9582 | 0.9591 | 0.9599 | 0.9608 | 0.9616 | 0.9625 | 0.9633 |
| 1.8 | 0.9641 | 0.9649 | 0.9656 | 0.9664 | 0.9671 | 0.9678 | 0.9686 | 0.9693 | 0.9699 | 0.9706 |
| 1.9 | 0.9713 | 0.9719 | 0.9726 | 0.9732 | 0.9738 | 0.9744 | 0.9750 | 0.9756 | 0.9761 | 0.9767 |
| 2.0 | 0.9772 | 0.9778 | 0.9783 | 0.9788 | 0.9793 | 0.9798 | 0.9803 | 0.9808 | 0.9812 | 0.9817 |
| 2.1 | 0.9821 | 0.9826 | 0.9830 | 0.9834 | 0.9838 | 0.9842 | 0.9846 | 0.9850 | 0.9854 | 0.9857 |
| 2.2 | 0.9861 | 0.9864 | 0.9868 | 0.9871 | 0.9875 | 0.9878 | 0.9881 | 0.9884 | 0.9887 | 0.9890 |
| 2.3 | 0.9893 | 0.9896 | 0.9898 | 0.9901 | 0.9904 | 0.9906 | 0.9909 | 0.9911 | 0.9913 | 0.9916 |
| 2.4 | 0.9918 | 0.9920 | 0.9922 | 0.9925 | 0.9927 | 0.9929 | 0.9931 | 0.9932 | 0.9934 | 0.9936 |
| 2.5 | 0.9938 | 0.9940 | 0.9941 | 0.9943 | 0.9945 | 0.9946 | 0.9948 | 0.9949 | 0.9951 | 0.9952 |
| 2.6 | 0.9953 | 0.9955 | 0.9956 | 0.9957 | 0.9959 | 0.9960 | 0.9961 | 0.9962 | 0.9963 | 0.9964 |
| 2.7 | 0.9965 | 0.9966 | 0.9967 | 0.9968 | 0.9969 | 0.9970 | 0.9971 | 0.9972 | 0.9973 | 0.9974 |
| 2.8 | 0.9974 | 0.9975 | 0.9976 | 0.9977 | 0.9977 | 0.9978 | 0.9979 | 0.9979 | 0.9980 | 0.9981 |
| 2.9 | 0.9981 | 0.9982 | 0.9982 | 0.9983 | 0.9984 | 0.9984 | 0.9985 | 0.9985 | 0.9986 | 0.9986 |
| 3.0 | 0.9987 | 0.9987 | 0.9987 | 0.9988 | 0.9988 | 0.9989 | 0.9989 | 0.9989 | 0.9990 | 0.9990 |
| 3.1 | 0.9990 | 0.9991 | 0.9991 | 0.9991 | 0.9992 | 0.9992 | 0.9992 | 0.9992 | 0.9993 | 0.9993 |
| 3.2 | 0.9993 | 0.9993 | 0.9994 | 0.9994 | 0.9994 | 0.9994 | 0.9994 | 0.9995 | 0.9995 | 0.9995 |
| 3.3 | 0.9995 | 0.9995 | 0.9995 | 0.9996 | 0.9996 | 0.9996 | 0.9996 | 0.9996 | 0.9996 | 0.9997 |
| 3.4 | 0.9997 | 0.9997 | 0.9997 | 0.9997 | 0.9997 | 0.9997 | 0.9997 | 0.9997 | 0.9997 | 0.9998 |


| z | 0.00 | 0.01 | 0.02 | 0.03 | 0.04 | 0.05 | 0.06 | 0.07 | 0.08 | 0.09 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| -3.4 | 0.0003 | 0.0003 | 0.0003 | 0.0003 | 0.0003 | 0.0003 | 0.0003 | 0.0003 | 0.0003 | 0.0002 |
| -3.3 | 0.0005 | 0.0005 | 0.0005 | 0.0004 | 0.0004 | 0.0004 | 0.0004 | 0.0004 | 0.0004 | 0.0003 |
| -3.2 | 0.0007 | 0.0007 | 0.0006 | 0.0006 | 0.0006 | 0.0006 | 0.0006 | 0.0005 | 0.0005 | 0.0005 |
| -3.1 | 0.0010 | 0.0009 | 0.0009 | 0.0009 | 0.0008 | 0.0008 | 0.0008 | 0.0008 | 0.0007 | 0.0007 |
| -3.0 | 0.0013 | 0.0013 | 0.0013 | 0.0012 | 0.0012 | 0.0011 | 0.0011 | 0.0011 | 0.0010 | 0.0010 |
| -2.9 | 0.0019 | 0.0018 | 0.0018 | 0.0017 | 0.0016 | 0.0016 | 0.0015 | 0.0015 | 0.0014 | 0.0014 |
| -2.8 | 0.0026 | 0.0025 | 0.0024 | 0.0023 | 0.0023 | 0.0022 | 0.0021 | 0.0021 | 0.0020 | 0.0019 |
| -2.7 | 0.0035 | 0.0034 | 0.0033 | 0.0032 | 0.0031 | 0.0030 | 0.0029 | 0.0028 | 0.0027 | 0.0026 |
| -2.6 | 0.0047 | 0.0045 | 0.0044 | 0.0043 | 0.0041 | 0.0040 | 0.0039 | 0.0038 | 0.0037 | 0.0036 |
| -2.5 | 0.0062 | 0.0060 | 0.0059 | 0.0057 | 0.0055 | 0.0054 | 0.0052 | 0.0051 | 0.0049 | 0.0048 |
| -2.4 | 0.0082 | 0.0080 | 0.0078 | 0.0075 | 0.0073 | 0.0071 | 0.0069 | 0.0068 | 0.0066 | 0.0064 |
| -2.3 | 0.0107 | 0.0104 | 0.0102 | 0.0099 | 0.0096 | 0.0094 | 0.0091 | 0.0089 | 0.0087 | 0.0084 |
| -2.2 | 0.0139 | 0.0136 | 0.0132 | 0.0129 | 0.0125 | 0.0122 | 0.0119 | 0.0116 | 0.0113 | 0.0110 |
| -2.1 | 0.0179 | 0.0174 | 0.0170 | 0.0166 | 0.0162 | 0.0158 | 0.0154 | 0.0150 | 0.0146 | 0.0143 |
| -2.0 | 0.0228 | 0.0222 | 0.0217 | 0.0212 | 0.0207 | 0.0202 | 0.0197 | 0.0192 | 0.0188 | 0.0183 |
| -1.9 | 0.0287 | 0.0281 | 0.0274 | 0.0268 | 0.0262 | 0.0256 | 0.0250 | 0.0244 | 0.0239 | 0.0233 |
| -1.8 | 0.0359 | 0.0351 | 0.0344 | 0.0336 | 0.0329 | 0.0322 | 0.0314 | 0.0307 | 0.0301 | 0.0294 |
| -1.7 | 0.0446 | 0.0436 | 0.0427 | 0.0418 | 0.0409 | 0.0401 | 0.0392 | 0.0384 | 0.0375 | 0.0367 |
| -1.6 | 0.0548 | 0.0537 | 0.0526 | 0.0516 | 0.0505 | 0.0495 | 0.0485 | 0.0475 | 0.0465 | 0.0455 |
| -1.5 | 0.0668 | 0.0655 | 0.0643 | 0.0630 | 0.0618 | 0.0606 | 0.0594 | 0.0582 | 0.0571 | 0.0559 |
| -1.4 | 0.0808 | 0.0793 | 0.0778 | 0.0764 | 0.0749 | 0.0735 | 0.0721 | 0.0708 | 0.0694 | 0.0681 |
| -1.3 | 0.0968 | 0.0951 | 0.0934 | 0.0918 | 0.0901 | 0.0885 | 0.0869 | 0.0853 | 0.0838 | 0.0823 |
| -1.2 | 0.1151 | 0.1131 | 0.1112 | 0.1093 | 0.1075 | 0.1056 | 0.1038 | 0.1020 | 0.1003 | 0.0985 |
| -1.1 | 0.1357 | 0.1335 | 0.1314 | 0.1292 | 0.1271 | 0.1251 | 0.1230 | 0.1210 | 0.1190 | 0.1170 |
| -1.0 | 0.1587 | 0.1562 | 0.1539 | 0.1515 | 0.1492 | 0.1469 | 0.1446 | 0.1423 | 0.1401 | 0.1379 |
| -0.9 | 0.1841 | 0.1814 | 0.1788 | 0.1762 | 0.1736 | 0.1711 | 0.1685 | 0.1660 | 0.1635 | 0.1611 |
| -0.8 | 0.2119 | 0.2090 | 0.2061 | 0.2033 | 0.2005 | 0.1977 | 0.1949 | 0.1922 | 0.1894 | 0.1867 |
| -0.7 | 0.2420 | 0.2389 | 0.2358 | 0.2327 | 0.2296 | 0.2266 | 0.2236 | 0.2206 | 0.2177 | 0.2148 |
| -0.6 | 0.2743 | 0.2709 | 0.2676 | 0.2643 | 0.2611 | 0.2578 | 0.2546 | 0.2514 | 0.2483 | 0.2451 |
| -0.5 | 0.3085 | 0.3050 | 0.3015 | 0.2981 | 0.2946 | 0.2912 | 0.2877 | 0.2843 | 0.2810 | 0.2776 |
| -0.4 | 0.3446 | 0.3409 | 0.3372 | 0.3336 | 0.3300 | 0.3264 | 0.3228 | 0.3192 | 0.3156 | 0.3121 |
| -0.3 | 0.3821 | 0.3783 | 0.3745 | 0.3707 | 0.3669 | 0.3632 | 0.3594 | 0.3557 | 0.3520 | 0.3483 |
| -0.2 | 0.4207 | 0.4168 | 0.4129 | 0.4090 | 0.4052 | 0.4013 | 0.3974 | 0.3936 | 0.3897 | 0.3859 |
| -0.1 | 0.4602 | 0.4562 | 0.4522 | 0.4483 | 0.4443 | 0.4404 | 0.4364 | 0.4325 | 0.4286 | 0.4247 |
| 0.0 | 0.5000 | 0.4960 | 0.4920 | 0.4880 | 0.4840 | 0.4801 | 0.4761 | 0.4721 | 0.4681 | 0.4641 |

