

Scholarship Algebra II
Circular Trig Worksheet #1
Angles and Radians

Name _____

Show work on the back or on a separate sheet of paper.

Express each degree measure as a radian measure using π .

1. 240° 2. -225° 3. 150° 4. -60° 5. 330°
6. -300° 7. 315° 8. 270° 9. -108° 10. 144°

Express each radian measure as a degree measure.

11. $\frac{3\pi^R}{4}$ 12. $\frac{5\pi^R}{3}$ 13. $-\frac{7\pi^R}{4}$ 14. $\frac{3\pi^R}{2}$ 15. $\frac{5\pi^R}{6}$
16. $-\frac{3\pi^R}{2}$ 17. $-\frac{11\pi^R}{6}$ 18. $\frac{7\pi^R}{3}$ 19. $-\frac{8\pi^R}{9}$ 20. $\frac{7\pi^R}{12}$

Find the length of the arc on a circle with the given radius that is intercepted by the central angle of the given measure.

21. 35 cm; 72° 22. 2.8 cm; 330° 23. 105 cm; 150°
24. 630 mm; $\frac{5\pi^R}{6}$ 25. 56 cm; $\frac{\pi^R}{8}$ 26. 0.42 cm; $\frac{9\pi^R}{2}$

Scholarship Algebra II
Circular Trig Worksheet #2
Sine and Cosine

Name _____

Sketch the angle α whose terminal side in standard position passes through the given point, and find $\sin \alpha$ and $\cos \alpha$. Leave your answers in fractional form.

1. $(9, 12)$ 2. $(-4, 3)$ 3. $(5, -12)$ 4. $(7, 24)$ 5. $(0, 3)$
6. $(-2, -2)$ 7. $(3, 6)$ 8. $(-3, 1)$ 9. $(-8, -6)$ 10. $(-4, 0)$

Find $\sin \alpha$ or $\cos \alpha$ (whichever is not given) for α in the given quadrant.

11. $\sin \alpha = -\frac{12}{13}$; III 12. $\sin \alpha = -\frac{5}{13}$; III 13. $\cos \alpha = \frac{15}{17}$; I 14. $\cos \alpha = -\frac{21}{25}$; II
15. $\cos \alpha = \frac{1}{4}$; IV 16. $\sin \alpha = -\frac{\sqrt{3}}{2}$; IV 17. $\sin \alpha = \frac{2\sqrt{6}}{5}$; II 18. $\cos \alpha = \frac{5}{7}$; I

Scholarship Algebra II
Circular Trig Worksheet #3
Special Angles

Name _____

Find the exact value of the given function (no decimals!).

1. $\cos 495^\circ$

2. $\sin(-210^\circ)$

3. $\cos 765^\circ$

4. $\sin 600^\circ$

5. $\sin \frac{9\pi^R}{4}$

6. $\sin \frac{5\pi^R}{2}$

7. $\cos\left(-\frac{7\pi^R}{3}\right)$

8. $\cos\left(-\frac{7\pi^R}{6}\right)$

9. $\sin\left(-\frac{4\pi^R}{3}\right)$

10. $\cos \frac{19\pi^R}{6}$

11. $\cos(-5\pi^R)$

12. $\sin \frac{15\pi^R}{4}$

Find the angle that passes through the given point. Give your answer in radians and degrees.

13. $(1, \sqrt{3})$

14. $(5, -5)$

15. $(-2\sqrt{3}, -2)$

16. $(9, 9)$

17. $(-3, -3)$

18. $(\sqrt{5}, -\sqrt{15})$

19. $(-\sqrt{3}, -\sqrt{3})$

20. $\left(-\frac{1}{3}, \frac{1}{3}\sqrt{3}\right)$

Scholarship Algebra II
Circular Trig Worksheet #4
Reference Angles

Name _____

Sketch each given angle and give its reference angle in degrees.

1. 150° 2. 240° 3. 295° 4. -50° 5. -300°
6. 405° 7. -600° 8. 15° 9. -100° 10. 1000°

Sketch each given angle and give its reference angle in radians (without converting to degrees).

11. $\frac{5\pi}{6}$ 12. $\frac{4\pi}{3}$ 13. $-\frac{3\pi}{5}$ 14. $\frac{13\pi}{6}$ 15. $-\frac{7\pi}{3}$

Find the sine and cosine of each using reference angles. Make sure you include the proper sign.

16. 150° 17. 240° 18. -45° 19. 300° 20. -60° 21. 225°

22. $\frac{5\pi}{6}$ 23. $\frac{4\pi}{3}$ 24. $\frac{13\pi}{6}$

Scholarship Algebra II
Circular Trig Worksheet #5
"Nasty" Angles

Name _____

Answer all questions on a separate sheet of paper. Show work and provide sketches where necessary.

Evaluate using a calculator. Provide answers rounded to four decimal places.

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|------------------------|------------------------|---------------------|---------------------|
| 1. $\sin 136.7^\circ$ | 2. $\sin 314.8^\circ$ | 3. $\cos 226^\circ$ | 4. $\cos 117^\circ$ |
| 5. $\sin (-128^\circ)$ | 6. $\cos (-251^\circ)$ | 7. $\cos 339^\circ$ | 8. $\sin 675^\circ$ |
| 9. $\cos (-3.4^R)$ | 10. $\sin (-2.7^R)$ | 11. $\sin 8.7^R$ | 12. $\cos 11.6^R$ |

Determine the measure of α such that $0^\circ \leq \alpha < 360^\circ$. Give your answer to the nearest tenth of a degree.

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|---|---|
| 13. $\sin \alpha = -0.2079$; $\cos \alpha < 0$ | 14. $\cos \alpha = 0.9239$; $\sin \alpha < 0$ |
| 15. $\cos \alpha = -0.1132$; $\sin \alpha < 0$ | 16. $\sin \alpha = 0.7716$; $\cos \alpha < 0$ |
| 17. $\cos \alpha = -0.9150$; $\sin \alpha > 0$ | 18. $\sin \alpha = -0.7408$; $\cos \alpha < 0$ |
| 19. $\sin \alpha = 0.8854$; $\cos \alpha < 0$ | 20. $\cos \alpha = -0.2538$; $\sin \alpha < 0$ |

Determine the measure of α such that the terminal side of α passes through the given point and $0^\circ \leq \alpha < 360^\circ$. Give your answer to the nearest tenth of a degree.

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|---------------|---------------|----------------------|------------------------|
| 21. (-20, 21) | 22. (-15, -8) | 23. $(2, -\sqrt{5})$ | 24. $(-7, 6\sqrt{2})$ |
| 25. (3, -4) | 26. (-5, 12) | 27. (-9, -40) | 28. $(3, -2\sqrt{10})$ |

Determine the measure of α such that the terminal side of α passes through the given point and $0^R \leq \alpha < 2\pi^R$. Give your answer in radians to the nearest hundredth.

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|--------------|----------------------|------------------------|-----------------------|
| 29. (15, -8) | 30. $(-\sqrt{7}, 3)$ | 31. $(-2, -3\sqrt{5})$ | 32. $(7, -4\sqrt{2})$ |
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Scholarship Algebra II
Circular Trig Worksheet #6
The Other Trig Functions

Name _____

Answer all questions on a separate sheet of paper. Show work and provide sketches where necessary.

Find the value to four decimal places using your calculator.

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| 1. $\tan 132^\circ$ | 2. $\sec 305^\circ$ | 3. $\csc 213^\circ$ | 4. $\tan 325^\circ$ |
| 5. $\cot 247.3^\circ$ | 6. $\csc 289.7^\circ$ | 7. $\sec 2.46^R$ | 8. $\cot 3.75^R$ |
| 9. $\tan 5.87^R$ | 10. $\csc 6.02^R$ | 11. $\cot 3.5^R$ | 12. $\sec 0.74^R$ |

Find α to the nearest tenth of a degree so that $0^\circ \leq \alpha \leq 90^\circ$

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|---------------------------|---------------------------|---------------------------|
| 13. $\tan \alpha = 1.904$ | 14. $\sec \alpha = 1.080$ | 15. $\csc \alpha = 1.313$ |
| 16. $\tan \alpha = 5.000$ | 17. $\sec \alpha = 1.271$ | 18. $\cot \alpha = 4.372$ |

Find α to the nearest tenth of a degree so that α lies in the given quadrant

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|---------------------------------|--------------------------------|---------------------------------|
| 19. IV: $\tan \alpha = -0.7265$ | 20. II: $\csc \alpha = 1.244$ | 21. III: $\sec \alpha = -1.108$ |
| 22. II: $\cot \alpha = -0.3899$ | 23. IV: $\csc \alpha = -2.572$ | 24. III: $\tan \alpha = 8.000$ |

Find the values of all six trigonometric functions of the angle whose terminal side passes through the given point. Give all answers as reduced fractions in simplified radical form.

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|-------------|--------------|-----------------------|-----------------------|
| 25. (6, -8) | 26. (-5, 12) | 27. (0, -3) | 28. (-7, -24) |
| 29. (-2, 0) | 30. (3, 6) | 31. $(2\sqrt{6}, -5)$ | 32. $(-4, 2\sqrt{5})$ |

Find the values of the other five trigonometric functions of α having the given information. Give all answers as reduced fractions in simplified radical form.

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|---|--|---|
| 33. $\sin \alpha = -\frac{\sqrt{3}}{2}; Q_{IV}$ | 34. $\sin \alpha = -\frac{1}{\sqrt{2}}; Q_{III}$ | 35. $\sin \alpha = \frac{\sqrt{5}}{3}; Q_{II}$ |
| 36. $\sec \alpha = -\frac{3}{2\sqrt{2}}; Q_{III}$ | 37. $\csc \alpha = \frac{7}{\sqrt{15}}; Q_{II}$ | 38. $\cos \alpha = \frac{2}{\sqrt{13}}; Q_{IV}$ |
| 39. $\tan \alpha = \frac{1}{5}; Q_{III}$ | 40. $\cot \alpha = -\frac{3\sqrt{5}}{2}; Q_{II}$ | |