CAMBRIDGE INTERNATIONAL EXAMINATIONS International General Certificate of Secondary Education

## MATHEMATICS

Paper 2
October/November 2003
1 hour 30 minutes
Candidates answer on the Question Paper. Additional Materials: Electronic calculator

Geometrical instruments Mathematical tables (optional)
Tracing paper (optional)

## READ THESE INSTRUCTIONS FIRST

Write your Centre number, candidate number and name on all the work you hand in.
Write in dark blue or black pen in the spaces provided on the Question Paper.
You may use a pencil for any diagrams or graphs.
Do not use staples, paper clips, highlighters, glue or correction fluid.
Answer all questions.
If working is needed for any question it must be shown below that question.
The number of marks is given in brackets [ ] at the end of each question or part question.
The total of the marks for this paper is 70.
Electronic calculators should be used.
If the degree of accuracy is not specified in the question, and if the answer is not exact, give the answer to three significant figures. Answers in degrees should be given to one decimal place.
For $\pi$, use either your calculator value or 3.142.

If you have been given a label, look at the details. If any details are incorrect or missing, please fill in your correct details in the space given at the top of this page.

Stick your personal label here, if provided.

University of Cambridge
Local Examinations Syndicate

1 Work out $\frac{2+12}{4+3 \times 8}$.

Answer

2 The altitude of Death Valley is -86 metres.
The altitude of Mount Whitney is 4418 metres.
Calculate the difference between these two altitudes.

Answer m [1]

3 The first five terms of a sequence are $4,9,16,25,36, \ldots$
Find
(a) the 10th term,

> Answer (a).
(b) the $n$th term.

Answer (b)

4 Rearrange the quantities in order with the smallest first.

$$
\frac{1}{8} \%, \quad \frac{3}{2500}, \quad 0.00126
$$

Answer $\qquad$ .<. <
$5 \mathscr{E}=\left\{-2 \frac{1}{2},-1, \sqrt{2}, 3.5, \sqrt{30}, \sqrt{36}\right\}$
$X=\{$ integers $\}$
$Y=\{$ irrational numbers $\}$
List the members of
(a) $X$,

$$
\text { Answer (a) } X=\{
$$

\} [1]
(b) $Y$.

$$
\begin{equation*}
\text { Answer (b) } Y=\{. \tag{1}
\end{equation*}
$$

6 Abdul invested $\$ 240$ when the rate of simple interest was $r \%$ per year.
After $m$ months the interest was $\$ I$.
Write down and simplify an expression for $I$, in terms of $m$ and $r$.

$$
\text { Answer } I=
$$

7 A baby was born with a mass of 3.6 kg .
After three months this mass had increased to 6 kg .
Calculate the percentage increase in the mass of the baby.
$\qquad$

8 (a) $3^{x}=\frac{1}{3}$.
Write down the value of $x$.

$$
\text { Answer (a) } x=.
$$

(b) $5^{y}=k$.

Find $5^{y+1}$, in terms of $k$.

$$
\begin{equation*}
\text { Answer (b) } 5^{y+1}= \tag{1}
\end{equation*}
$$

9 (a) 32493 people were at a football match.
Write this number to the nearest thousand.

> Answer (a).
(b) At another match there were 25500 people, to the nearest hundred.

Complete the inequality about $n$, the number of people at this match.

Answer (b)
$\leqslant n<$

10 When cars go round a bend there is a force, $F$, between the tyres and the ground.
$F$ varies directly as the square of the speed, $v$.
When $v=40, F=18$.
Find $F$ when $v=32$.

$$
\begin{equation*}
\text { Answer } F=. \tag{3}
\end{equation*}
$$

11 In April 2001, a bank gave the following exchange rates.
1 euro $=0.623$ British pounds.
1 euro = 1936 Italian lire .
(a) Calculate how much one pound was worth in lire.

Answer (a) lire [2]
(b) Calculate how much one million lire was worth in pounds.

12 The diagram shows the graphs of $y=\sin x^{\circ}$ and $y=\cos x^{\circ}$.


Find the values of $x$ between 0 and 360 for which
(a) $\sin x^{\circ}=\cos x^{\circ}$,

Answer (a) $x=$ $\qquad$ or $x=$
(b) $\sin x^{\circ}=\sin 22 \cdot 5^{\circ}(x \neq 22.5)$.

$$
\begin{equation*}
\text { Answer (b) } x=\text {. } \tag{1}
\end{equation*}
$$



NOT TO
SCALE

The two cones are similar.
(a) Write down the value of $l$.

Answer (a) $l=$
(b) When full, the larger cone contains $172 \mathrm{~cm}^{3}$ of water.

How much water does the smaller cone contain when it is full?

Answer (b) $\qquad$ $\mathrm{cm}^{3}$

14 (a) Write $\frac{3}{x}-\frac{2}{x+1}$ as a single fraction in its simplest form.

Answer (a)
(b) Solve the equation $\frac{3}{x}-\frac{2}{x+1}=0$.

15

$P T$ and $P U$ are tangents to an arc of a circle at $T$ and $U$.
(a) Using a straight edge and compasses only, construct the bisector of angle TPU.
(b) By drawing another line accurately, find the centre of the circle and label it $O$.

16 The straight line graph of $y=3 x-6$ cuts the $x$-axis at $A$ and the $y$-axis at $B$.
(a) Find the coordinates of $A$ and the coordinates of $B$.

Answer (a) A (............., ................)
$\qquad$
(b) Calculate the length of $A B$.

> Answer (b)
(c) $M$ is the mid-point of $A B$.

Find the coordinates of $M$.
Answer (c) (................., .................)


NOT TO SCALE
$A B C D$ is a cyclic quadrilateral.
$A D$ is parallel to $B C$. The diagonals $D B$ and $A C$ meet at $X$.
Angle $A C B=62^{\circ}$ and angle $A C D=20^{\circ}$.
Calculate
(a) angle $D B A$,

Answer (a) Angle $D B A=$
(b) angle $D A B$,

$$
\text { Answer (b) Angle } D A B=
$$

(c) angle $D A C$,

Answer (c) Angle $D A C=$
(d) angle $A X B$,

Answer (d) Angle $A X B=$
(e) angle $C D B$.

18 The population of Europe is 580000000 people.
The land area of Europe is 5900000 square kilometres.
(a) Write 580000000 in standard form.
Answer (a)......................................... [1]
(b) Calculate the number of people per square kilometre, to the nearest whole number.

Answer (b)
(c) Calculate the number of square metres per person.

> Answer (c)
$\qquad$ $\mathrm{m}^{2}$

19 f: $x \rightarrow 1-2 x$ and g: $x \rightarrow \frac{x}{2}$.
(a) Find $\mathrm{fg}(7)$.
$\qquad$
(b) (i) Solve $\mathrm{f}(x)=\mathrm{g}(x)$.

$$
\begin{equation*}
\text { Answer }(b)(\mathrm{i}) x= \tag{2}
\end{equation*}
$$

(ii) The graphs of $y=\mathrm{f}(x)$ and $y=\mathrm{g}(x)$ meet at $M$.

Find the coordinates of $M$.
$\qquad$


In the diagram $O A=\frac{2}{3} O P$ and $O B=\frac{3}{4} O Q$.
$\overrightarrow{O P}=\mathbf{p}$ and $\overrightarrow{O Q}=\mathbf{q}$.
(a) Find in terms of $\mathbf{p}$ and $\mathbf{q}$
(i) $\overrightarrow{A Q}$,

Answer (a)(i) $\overrightarrow{A Q}=$
(ii) $\overrightarrow{B P}$.

Answer (a)(ii) $\overrightarrow{B P}=$
(b) $A Q$ and $B P$ intersect at $T$.
$B T=\frac{1}{3} B P$.
Find $\overrightarrow{Q T}$ in terms of $\mathbf{p}$ and $\mathbf{q}$, in its simplest form.

Answer (b) $\overrightarrow{Q T}=$

21 Marina goes to the shop to buy loaves of bread and cakes.
One loaf of bread costs 60 cents and one cake costs 80 cents.
She buys $x$ loaves of bread and $y$ cakes.
(a) She must not spend more than $\$ 12$.

Show that $3 x+4 y \leqslant 60$.
Answer (a)
(b) The number of loaves of bread must be greater than or equal to the number of cakes. Write down an inequality in $x$ and $y$ to show this information.
Answer (b).
(c) On the grid below show the two inequalities by shading the unwanted regions. Write $R$ in the required region.

(d) The total number of loaves of bread and cakes is $x+y$.

Find the largest possible value of $x+y$.
Answer (d)

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