

Expressing numbers as the product of their prime factors

Make a list of the first 10 prime numbers:

$$18 = 2 \times 9 = 2 \times 3 \times 3$$

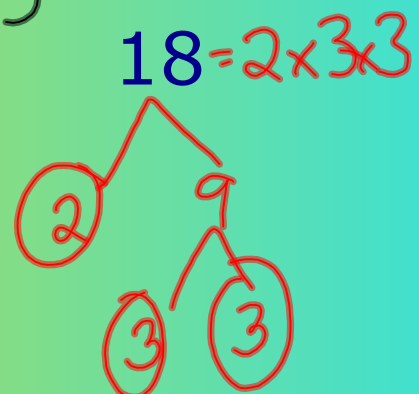
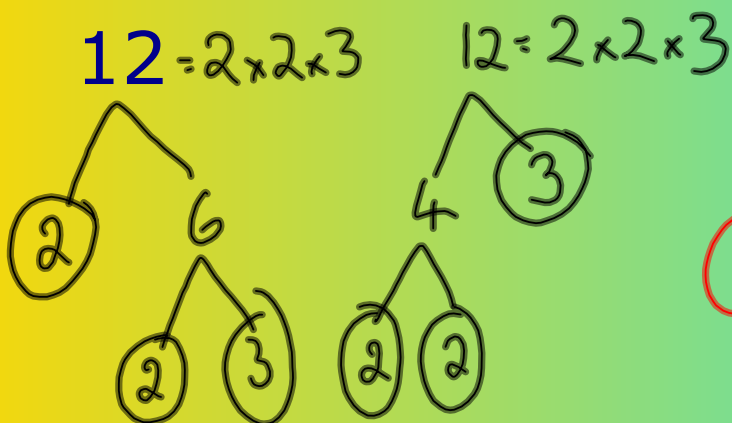
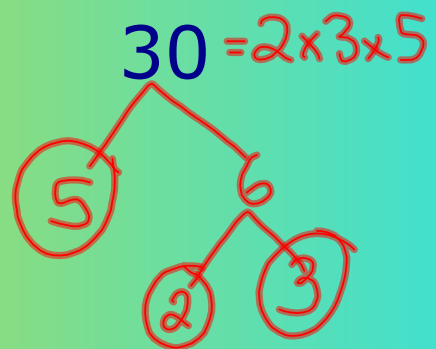
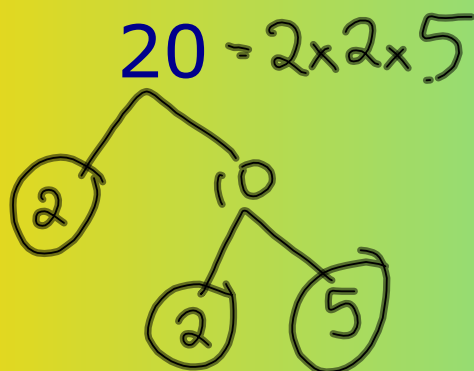
$$2, 3, 5, 7, 11, 13, 17, 19, 23$$

$$4 = 2 \times 2$$

$$27 = 3 \times 3 \times 3 = 3^3$$

$$2^9, \dots$$

Factor trees:



$$40$$

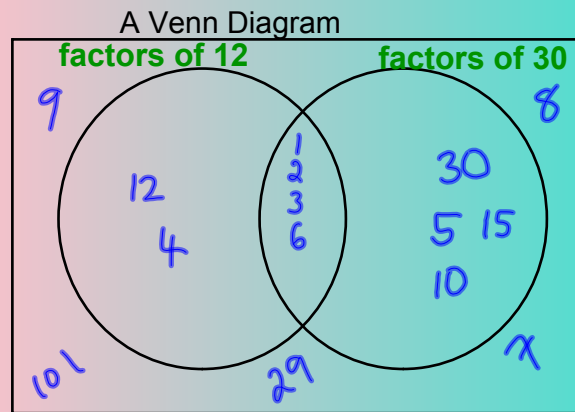
$$= 2 \times 2 \times 5 \times 2$$

$$= 2^3 \times 5$$

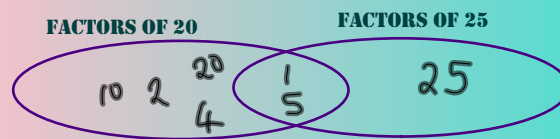
$$50 = 2 \times 5 \times 5$$

```

graph TD
    50 --- 2
    50 --- 25
    25 --- 5
    25 --- 5
  
```



HCF



Express 42 and 60 as the product of their primes.

$$42 = 3 \times 2 \times 7 \quad 60 = 2 \times 2 \times 3 \times 5$$

$$\text{HCF} = 3 \times 2 = 6$$

Find all the common factors of 42 and 60.

Find the highest common factor (HCF) of 42 and 60.

Express 630 and 660 as the product of their primes.

$$630 = 2 \times 3 \times 3 \times 7 \times 5$$

$$660 = 2 \times 2 \times 3 \times 5 \times 11$$

Find all the common factors of 630 and 660.

Find the highest common factor (HCF) of 630 and 660.

$2 \times 3 \times 3 \times 5 \times 7 \times 11 = 30$ ✓

Find the hcf of these numbers

$$2 \times 2 \times 3 \times 5 \times 11$$
$$2 \times 5 \times 11 \times 13$$

$$\text{HCF} = 2 \times 5 \times 11$$
$$= 110$$

$$2 \times 2 \times 3 \times 3 \times 5$$
$$2 \times 3 \times 3 \times 3 \times 7$$

$$\text{HCF}$$
$$= 2 \times 3 \times 3$$
$$= 18$$

$$5 \times 7 \times 7 \times 7 \times 11$$
$$3 \times 7 \times 11 \times 11$$

$$\text{HCF}$$
$$= 77$$

Highest Common Factor

Find the hcf of

33,6 $HCF = 3$

27,18 $HCF = 9$

10,12 $HCF = 2$

18,90 $HCF = 18$

$$\begin{array}{r} 180 \times \\ \div 2 \\ \hline 90 \end{array}$$

Find the prime factorisation of

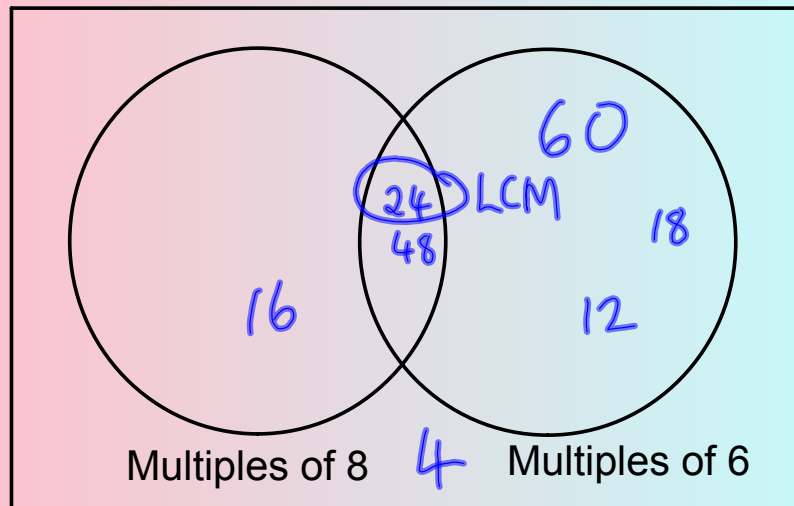
10 and 35.

Find the HCF.

Find the prime factorisation of 100 and 140.**Find the HCF.**

$$\begin{array}{l} 100 = 2 \times 2 \times 5 \times 5 \\ 140 = 2 \times 2 \times 5 \times 7 \\ HCF = 2 \times 2 \times 5 \\ = 20. \end{array}$$

Find the prime factorisation of 105 and 140.**Find the HCF.**

Multiples

10, 25

$$\begin{aligned} \text{LCM} &= 50 \\ \text{HCF} &= 5 \end{aligned}$$

LCM=
HCF=

6, 10

$$\begin{aligned} \text{LCM} &= 30 \\ \text{HCF} &= 2 \end{aligned}$$

15, 20

$$\begin{aligned} \text{HCF} &= 5 \\ \text{LCM} &= 60 \end{aligned}$$

4, 16

$$\begin{aligned} \text{HCF} &= 4 \\ \text{LCM} &= 16 \end{aligned}$$

9, 12

$$\begin{aligned} \text{HCF} &= 3 \\ \text{LCM} &= 36 \end{aligned}$$

Express 6 and 8 as the product of their primes.

$$6 = 2 \times 3$$

$$8 = 2 \times 2 \times 2$$

$$\text{HCF} = 2$$

$$\begin{aligned} \text{LCM} &= 2 \times 2 \times 2 \times 3 \\ &= 24 \end{aligned}$$

Find some common multiples of 6 and 8.

Find the lowest common multiple (LCM) of 6 and 8

Lowest common multiples

find the lcm of these numbers

5,6

10,12

25, 15

Write 20 and 32 as products of their prime factors. Find their lcm.

$$\left. \begin{array}{l} 2 \times 5 \times 11 \\ 2 \times 2 \times 3 \times 11 \end{array} \right\} \text{LCM} = 2 \times 2 \times 3 \times 11 \times 5$$

$$2 \times 3 \times 3 \times 3 \times 7 \times 2 \times 5 \left\{ \begin{array}{l} 2 \times 2 \times 3 \times 3 \times 5 \\ 2 \times 3 \times 3 \times 3 \times 7 \end{array} \right. \text{LCM}$$

$$\left. \begin{array}{l} 5 \times 7 \times 7 \times 7 \times 11 \\ 3 \times 7 \times 11 \times 11 \end{array} \right\} \text{LCM} = 5 \times 7 \times 7 \times 7 \times 11 \times 3 \times 11$$

Exam style question:

Express 84 and 105 as products of their prime factors.

Find the HCF and LCM of 84 and 105.

$$\begin{array}{ll} 84 = 2 \times 2 \times 3 \times 7 & \text{HCF} = 3 \times 7 = 21 \\ 105 = 3 \times 5 \times 7 & \text{LCM} = 2 \times 2 \times 3 \times 7 \times 5 \\ & = \underline{\underline{420}} \end{array}$$

A pair of numbers have HCF of 5.
What numbers could they be?

A pair of numbers have HCF of
12. What numbers could they be?

A pair of numbers have LCM of
15.

What numbers could they be?

Express each pair of numbers as the product of their primes. Find the LCM and HCF for each pair.

For Wednesday

$$1.) 8, 10 \quad 2.) 14, 20$$

$$3.) 15, 50 \quad 4.) 42, 60$$

$$5.) 450, 120 \quad \text{EXT:} 6.) 210, 1540$$

$$6. 210 = 2 \times 3 \times 5 \times 7 \quad 1540 = 2 \times 2 \times 5 \times 7 \times 11$$

$$\text{HCF} = 2 \times 5 \times 7 = 70$$

$$\text{LCM} = 2 \times 2 \times 3 \times 5 \times 7 \times 11 = 4620$$

$$7. 3000 = 2 \times 2 \times 2 \times 3 \times 5 \times 5 \times 5 \quad 780 = 2 \times 2 \times 3 \times 5 \times 13$$

$$\text{HCF} = 2 \times 2 \times 3 \times 5 = 60$$

$$\text{LCM} = 2 \times 2 \times 2 \times 3 \times 5 \times 5 \times 5 \times 13 \quad \neq 39000$$

Express 42 and 60 as the product of their primes.

Find some of the common multiples of 42 and 60.
Find the Lowest Common Multiple (LCM) of 42 and 60.

Standard (index) Form

$$10^6 = 1\,000\,000$$

$$10^5 = 100\,000$$

$$10^4 = 10\,000$$

$$10^3 = 1\,000$$

$$10^2 = 100$$

$$10^1 = 10$$

$$10^0 = 1$$

$$10^{-1} = 0.1$$

$$10^{-2} = 0.01$$

p96 qu 2 -9

A number written in standard form is written as a multiple of a power of 10.

The number is of the form $a \times 10^x$ where $1 \leq a < 10$

$$26000 = 2.6 \times 10^4$$

$$22 = 2.2 \times 10^1$$

$$560 = 5.6 \times 10^2$$

$$= 2.3 \times 10^3$$

$$4 \times 10^3 = 4000$$

$$7.01 \times 10^9$$

$$= 7\,010\,000\,000$$

$$3.2 \times 10^4 = 32\,000$$

$$6.3001 \times 10^2 = 630.01$$

9 x 1

Which of these numbers are written in standard form?

two hundred and four

$$2.3 \times 10$$

~~32×10~~

~~4.7×10^4~~

~~62×10^6~~

$\checkmark 0.76 \times 10^7$

~~6.9×10^{-2}~~

Write these numbers in standard form...

2600

$= 2.6 \times 10^3$

342

$= 3.42 \times 10^2$

~~740~~ $= 7.4 \times 10^2$

~~4~~ $= 4 \times 10^0$

9 million ⁶
 $= 9 \times 10^6$

0.00456

Calculations using sf

$$2 \times 10^3 \times 4 \times 10^5$$

$$6 \times 10^2 \times 4 \times 10^8$$

$$4 \times 10^4 \times 2 \times 10^3$$

Standard form

Express as a ordinary number:

$$5.1 \times 10^7$$

$$= 51\,000\,000$$

$$3 \times 10^4$$

$$= 30\,000$$

$$2.684 \times 10^6$$

$$2\,684\,000$$

Express in standard form:

$$567000 = 5.67 \times 10^5$$

$$310 = 3.1 \times 10^2$$

$$9123.78 = 9.12378 \times 10^3$$

Small numbers in Standard form

Write these numbers in standard form:

$4000 = 4 \times 10^3$

32000

$400 = 4 \times 10^2$

3200

$40 = 4 \times 10$

$\frac{4}{100}$

320

$4 = 4 \times 10^0$

32

$\frac{1}{10} \times 4$

$0.4 = 4 \times 10^{-1}$

3.2

$0.04 = 4 \times 10^{-2}$

0.32

$\frac{1}{10} = \frac{1}{100}$

$0.004 = 4 \times 10^{-3}$

0.032

0.0032

0.00032

Write these as ordinary numbers:

a) $4.5 \times 10^{-1} = 0.45$

e) $7.5 \times 10^{-3} = 0.0075$

b) $3.6 \times 10^{-1} = 0.36$

f) $3.06 \times 10^{-1} = 0.306$

c) $4.5 \times 10^{-2} = 0.045$

g) $4.05 \times 10^{-7} = 0.000000405$

d) $3.6 \times 10^{-3} = 0.0036$

h) $3.61 \times 10^{-6} = 0.00000361$

Write these in standard form:

a) $0.3 = 3 \times 10^{-1}$

e) $0.0303 = 3.03 \times 10^{-2}$

b) $0.003 = 3 \times 10^{-3}$

f) $0.0103 = 1.03 \times 10^{-2}$

c) $0.13 = 1.3 \times 10^{-1}$

g) $0.83 = 8.3 \times 10^{-1}$

d) $0.073 = 7.3 \times 10^{-2}$

h) $0.0000093 = 9.3 \times 10^{-6}$

Calculations using standard form

$$2 \times 10^7 \times 3 \times 10^5 = 6 \times 10^{12}$$

$$2 \times 10^7 \times 6 \times 10^4 = 12 \times 10^{11} = 1.2 \times 10^{12}$$

$$7 \times 10^{-7} \times 3 \times 10^{11} = 2.1 \times 10^5$$

$$9 \times 10^7 \times 8 \times 10^{-5} = 72 \times 10^2 = 7.2 \times 10^3$$

$$8 \times 10^{-4} \times 3 \times 10^5 = 24 \times 10^1 = 2.4 \times 10^2$$

$$\frac{6 \times 10^7}{3 \times 10^5} = 2 \times 10^2 \quad \frac{8 \times 10^7}{2 \times 10^1} = 4 \times 10^6$$

$$\frac{9 \times 10^4}{3 \times 10^5}$$

$$\frac{3 \times 10^7}{6 \times 10^5}$$

$$(2 \times 10^8) \div (8 \times 10^5)$$

$$(3 \times 10^7) \div (9 \times 10^8)$$

Very small numbers

$10^{-2} = \frac{1}{10^2} = 0.01$ $10^2 = 100$ $10^{-3} = \frac{1}{1000} = 0.001$
 $3 \times 10^{-2} = 0.03$ $4 \times 10^{-1} = \frac{4}{10} = 0.4$
 $6.3 \times 10^{-4} = 0.00063$ $5 \times 10^0 = 5$

Write these as ordinary numbers:

- | | |
|----------------------------------|----------------------------------------|
| a) $4.5 \times 10^{-1} = 0.45$ | e) $7.5 \times 10^{-3} = 0.0075$ |
| b) $3.6 \times 10^{-1} = 0.36$ | f) $3.06 \times 10^{-1} = 0.306$ |
| c) $4.5 \times 10^{-2} = 0.045$ | g) $4.05 \times 10^{-7} = 0.000000405$ |
| d) $3.6 \times 10^{-3} = 0.0036$ | h) $3.61 \times 10^{-6} = 0.00000361$ |

Write these in standard form:

- | | |
|----------|--------------|
| a) 0.3 | e) 0.0303 |
| b) 0.003 | f) 0.0103 |
| c) 0.13 | g) 0.83 |
| d) 0.073 | h) 0.0000093 |

Rounding using significant figures

Round these numbers to 1, 2, 3 dp

	To 1dp	2dp	3dp
a) 3.4502	3.5	3.45	3.450
b) 34.8901	34.9	34.89	34.890
c) 89.9992	90.0	90.00	89.999
d) 301.4951	301.5	301.50	301.495
e) 0.00564	0.0	0.01	0.006

calculations practice page:

To round to a certain number of significant figures, consider zeros

in front of and behind the number as useful only for place value and round appropriately.

eg to 3 sf:

$$34056 = 34100 \text{ to 3 sf}$$

$$0.005672 = 0.00567 \text{ to 3 sf}$$

$$7.045 = 7.05 \text{ to 3 sf}$$

$$3050307 = 3050000 \text{ to 3 sf}$$

	To 1sf	2sf	3sf
a) 2.4602	2	2.5	2.46
b) 704.9901	700	700	705
c) 49.9892	50	50	50.0
d) 1.4951	1	1.5	1.50
e) 0.2345	0.2	0.23	0.235
f) 0.004 532 1	0.005	0.0045	0.00453
g) 0.000 004 985			

Using a calculator for standard form.

Use your calculator to work out :

$$430000 \times 26000 = 1.118 \times 10^{10} \quad \checkmark$$

You cannot copy the calculator's display into your book!

$$1.118^{10} \quad \times$$

Your calculator is quite good at doing standard form!

Try 10^x		
2 EXP 3	= 2000	2×10^3
3 EXP 5	= 300000	3×10^5
4 EXP 4	= 40 000	4×10^4

On your calculator work out:

$$2 \times 10^5 \times 6 \times 10^6 = 1.2 \times 10^{12}$$

$$2 \times 10^5 + 6 \times 10^6 = 6.2 \times 10^6$$

$$230000^2 = 62000000$$

$$= 5.29 \times 10^{10}$$

Page 120