# Comparison of Population Distribution Models using Areal Interpolation on Data with Incompatible Spatial Zones

Bonnie L Horner

Department of Resource Analysis, Saint Mary's University of Minnesota, Minneapolis, MN 55404

Keywords: GIS, Interpolation, Population, Dasymetric, Zip Codes

# Abstract

Population data is collected by the government and released in census spatial zones as aggregate counts. The key problem in using this valuable dataset is the need to reassign the data to other geographical areas when the geographical zonal systems are incompatible. Areal interpolation is used to dis-aggregate census data into areas or zones that are compatible and can be analyzed. In this project, two population distribution models are compared using areal interpolation. The two distribution models evaluated consist of simple areal weighting and a dasymetric-based approach. Simple areal weighting is used with 2000 census data in various zip code areas. The dasymetric approach uses the Hennepin County, MN parcels to redistribute the same 2000 census data. The analysis is conducted using a five mile radius around a new hospital site in Hennepin County, MN. The proposed output of this study concludes that dasymetric areal interpolation is more representative of actual density than simple areal weighting.

# Introduction

Population estimates are critical for many spatial analysis tasks in government, urban planning, criminology, research and marketing. Government instigated national censuses (i.e. US Census) are the foundation for most geodemographic analysis. This census data offers the most accurate and nationally complete record of both geographical patterns and socio-economic characteristics of population (Langford et al., 2006).

Census data is not available in pointto-point format. Due to confidentiality requirements and to reduce data volumes, this information is available only as aggregate values. The smallest spatial zone of aggregate data is the census block group. Population mapping most commonly displays population data as evenly distributed within the census enumeration area (Holt et al., 2004). Population density is shown to be the same throughout the zones with abrupt population changes at the zone boundaries. However, population is continuous and does not follow boundaries. Additionally, population in urban areas is more dense than population in rural areas.

GIS is a great tool to use with population analysis. One of the key strengths of GIS is the ability to integrate data from one incompatible spatial zone to another spatial zone and then, to perform spatial analysis on the spatial zone. GIS can also utilize large or multiple datasets and create smaller manageable datasets to use for analysis or areal interpolation. Intersection of datasets or spatial buffers can also be joined to ancillary data to help interpret the results of the newly created datasets.

In this study, two population distribution models were used to perform areal interpolation and analyze population counts. Zip code areas are used to represent simple areal weighting. This is compared to dasymetric interpolation. The dasymetric interpolation uses county parcels as the ancillary data to redistribute population counts within census blocks. In this study a buffer was created around a hospital in the city of Maple Grove study area (Figure 1). The results of the two models are then descriptively compared.



Figure 1. Hospital site and ten zip code study area. One inch = 4 miles.

## Areal Interpolation

One method of determining population distribution is through areal interpolation. Areal interpolation refers to interpolation using polygons or "areas." Areal interpolation transfers data into a common dataset for use in analysis and comparison (Mennis, 2003). The two types of interpolation that are used in this study are the simple areal weighting and a dasymetricbased interpolation method.

Population Distribution Models

Simple Areal Weighting

Simple areal interpolation is the simplest approach to spatially distribute population counts. This process distributes the population count evenly within the limits of the zone boundaries studied. This distribution, however, does not represent the actual distribution of population. Population is not evenly distributed within the boundary, but population is continuous. This even-distribution of population over estimates or distorts the data within each unit/block (Holt et al., 2004). In reality, population would be concentrated within multi-family or apartments over single family housing, and urban areas over rural areas. Simple areal weighting does give commercial, industrial and public lands a population value. In reality, these areas do not have population.

Simple areal weighting is often mapped in the form of choropleth maps. Choropleth maps display the values distributed in each block as color blocks. Each different value has a distinct color.

In Figure 2, the 55311 zip code has a total population of 19,827. The total area of zip code 55311 is 13,793.82 acres.

Density = Total population / Total acres

According to simple areal weighting, the density in this zip code is 19827 / 13,793.82 or 1.44 people per acre.

## Dasymetric Interpolation

The dasymetric approach to areal interpolation is an area based approach to interpolation (Holt et al., 2004). It uses ancillary information to determine the distribution of the chosen variable. The ancillary or additional data could be landuse/land-cover data or census data. Ancillary data further refines data inside boundaries into more accurate zones of internal



Figure 2. Zip Code 55311. One inch = 5 miles.

homogeneity (Eicher and Brewer, 2001). Dasymetric mapping was first popularized in the United States by John Wright (1936). Wright used ancillary data to distribute population data into populated/unpopulated areas and mapped the results.

With computers and GIS, the ability to use ancillary data has become easier. Dasymetric mapping has the ability to achieve a more thorough representation of the underlying geography. Dasymetric maps create zones of internal homogeneity and reflect the spatial distribution of the variable being mapped. It removes the abrupt zone changes of the simple areal interpolation by redistributing the data according to the ancillary data into the target zones to be analyzed. Most ancillary data used in this method consists of land use data derived from satellite imagery (Mennis, 2003). Land use data divides the areas into populated/unpopulated and population is distributed accordingly.

In this study, parcels are the ancillary data to be used to distribute the population counts by the dasymetric method. The parcel use-description attribute is used to interpolate population into categories for analysis.

Figure 3 illustrates parcels within the zip code area of 55311. The parcels are given a value according to their parcel type. The parcel types are commercial, duplex, condo/townhouse and single family/farm.



Figure 3. Parcel types of zip code area 55311. One inch = 5 miles.

# US Census

The first US Census was taken in 1790. The US constitution mandates that the Census of Population and Housing be completed every ten years to apportion seats in the House of Representatives. Over the years, the census has grown in size and function. It is the world's oldest continuous national census (Peters and MacDonald, 2004). Census data is released as aggregate counts and statistics for corresponding zones. This is due to the legal requirement to maintain confidentiality of the individuals and it also aids in controlling data volume (Langford, 2004).

Census data is stored as polygons or areal units and contain demographical data such as average household size, family households, income, household status and children (Mennis, 2003). The data is broken down from largest to smallest geography units as follows: nation, region, division, state, counties, census tracts, block groups, and finally into census blocks. The block group is the smallest spatial unit for which there is sample data available. The boundaries of census zones are arbitrary and can change from one census to another (Cai, 2006).

In research, the spatial zones required for an analysis rarely follow census zones (Langsford, 2004). Additionally, various agencies such as schools, retail, and government that report information create their own administrative boundaries. These boundaries can change over time as do the census boundaries. Using GIS for analysis can create additional analytical zones such as those of buffers, overlays and viewshed analyses. The solution to integrate incompatible spatial zones into zones that are compatible is to transform the data using area interpolation techniques into compatible spatial zones (Langford, 2004).

#### Zip Codes

US zip codes are one of the "quirkier geographies" in the world. The idea of partitioning addresses was first proposed during World War II when thousands of postal employees left to serve in the military and the United States Postal Service (USPS) needed to facilitate postal deliveries. Five digit zip codes were developed in the 1960's by the USPS to make postal deliveries to every household more efficient. Zip stands for zone improvement plan. Zip codes do not correspond to a discrete bounded geographic area or polygon. They are linear features associated with roads and addresses. If an area does not have population, it also does not have a zip code. Zip codes correspond to mailing addresses and streets (Grubesic,

2006).

The use of zip codes for spatial, demographic and socio-economic analysis is growing. It is easy to ask "what is your zip code?" and then gather data accordingly. Zip codes are used in geodemographics since each zip code has its own geographic place and is thought to represent like-minded consumer of similar demographic and socioeconomic attributes (Grubesic, 2006).

For this study, the zip code area shapefile that was used has been created by Hennepin County from the Metro GIS polygons.

#### **Data Collection**

#### **County Data**

The primary polygon dataset utilized here is the Metro GIS parcel base dataset. The total dataset consists of 421,745 parcels. The attributes used from the dataset are the fields that specify the parcel use description and size of parcel. These were intersected with zip code areas to create more workable, smaller datasets. The use description attribute was used to classify the parcels into commercial/industrial/public lands, condos/townhouses, duplex and singlefamily/farm.

#### Census Data

The census data used in this study was obtained from Metro GIS in the form of TIGER polygons. The 2000 US Census data for Hennepin County is used in this study for population counts. The data consists of aggregate counts within each census block.

#### Zip Code Data

Zip code data is included in the attributes of the Metro GIS polygons. With this

information, zip code polygons were created for each zip code. The zip code boundary shapefile and zip code area polygon shapefile were created by Hennepin County. These are used here to create individual zip code polygons for analysis.

#### Methods

The Metro GIS polygon dataset consists of 421,745 parcel polygons. The area that is used in this study is the city of Maple Grove. The ten Maple Grove zip code areas used in this study are shown in Figure 1.

Using the zip code area polygons, polygons of parcels were created from the underlying Metro GIS polygon dataset for each of the selected zip codes. These smaller parcel polygons reduced the size of datasets and facilitated faster analysis. A layer was created from the Metro GIS polygons that included the areas five miles from the selected polygon, a new hospital being built in Maple Grove. The layer was created by buffering the hospital polygon five miles in all directions (Figure 4).

#### Simple Areal Weighting

Simple areal weighting averages the selected data across the total area or polygon. In this study, the population counts are averaged across each zip code area. The area is listed in square feet as noted below.

Population count / Zip code area = Average population per zip code.

The five mile hospital buffer layer was created around the hospital parcel. The buffer is then used to create a layer for each of the zip codes underlying the buffer. The area attribute in Table 1 shows each zip code And also the total area of each zip code parcel.



Figure 4. The Buffer Polygon created around hospital parcel. One inch = 5 miles.

The total area of each zip code parcel area was the area included in the five mile buffer. Dividing the five mile area by the total area for each zip code provided the value or what percent of the total of each zip code area was included in the buffer layer.

Five mile area / Total area = % of Total area

The percent of total area was then multiplied by the total population per zip code to determine the population in the five mile buffer.

% of Total area x Total zip code population = Population in five mile area buffer.

Table 1 displays each zip code with the number of parcels, area, and population. The next columns display the five mile/buffer number of parcels in the five mile, area per zip code and what percent of the area lies in the five mile buffer. The final column displays the five mile population for each zip code and total population of the five mile

ZIP CODES	NUMBER OF PARCELS	AREA	POPULATION PER ZIP CODE	5 MILE PARCELS (NUMBER)	5 MILE AREA	5 MILE AREA/AREA (%)	5 MILE POPULATION
55316	8477	5523.7	22422	2732	1779.2	0.32	7222
55374	5301	21163.5	9317	873	4623.3	0.22	2035
55327	1612	11302.7	3502	462	5025.9	0.44	1557
55340	2749	22967.3	5836	465	470.3	0.02	120
55369	13047	16100.7	33294	12132	12987.6	0.81	26856
55428	8763	6819.7	29933	20	109.6	0.02	481
55442	4789	5973.6	13196	3	67.9	0.01	150
55446	7029	8713.2	12464	541	794.6	0.09	1137
55311	12811	13793.8	19827	12811	13793.8	1.00	19827
					5 MILE TOTAL POPULATION		59386

Table 1. Simple areal weighting. Zip codes and five mile buffer area.

buffer – 59386.

## Dasymetric interpolation

Dasymetric interpolation is a method of interpolation that utilizes ancillary data. In this case, parcels are used as the ancillary data. The individual parcels are given a value that corresponds with their description type.

> Single Family/Farm = 4 Condominium and Townhouse = 3 Duplex = 2 Commercial, Industrial, Farmland and Public Lands = 0

The parcels have an attribute field that lists the land-use description for each parcel. This is combined into 4 parcel types – No Population, Duplex, Condo/Townhouse and Single Family/Farm. The "No Population" land use is commercial, industrial and public lands that do not have population.

The census blocks that were nested completely within the buffer are complete in population counts. Their total population is 43,521. Figure 5 shows census blocks that are completely contained, or nested within the buffer.

An intersection is performed using the buffer boundary to intersect with the census blocks (Figure 6). This intersection of census blocks was used to intersect with the underlying parcels (Figure 7). The



Figure 5. Census blocks completely within buffer. One inch = 5 miles.

parcels that had centroids within the buffer were selected (Figure 8). A population count was calculated for these parcels and added to the nested census population.



Figure 6. Intersection of Census Blocks and Boundary. Teal color represents the intersected blocks. One inch = 5 miles.



Figure 7. Intersection of selected census blocks with parcels contained within the 5 mile buffer. Purple represents census block parcels completely within buffer. One inch = 5 miles.

As with simple areal interpolation, each zip code has its own population value. To determine the value to be apportioned to each parcel in each zip code, a zip code parcel value for each zip code area was calculated (Appendix A). The parcels were divided into the four categories – No population (NOP), Duplex (DU), Condo/Townhouse (CT), Single Family/Farm (SFF) with their corresponding values as noted here.

NOP = 0	DU = 2
CT = 3	SFF = 4

Each category of values was totaled. The total population for each zip code was divided by the total parcel value to calculate the zip code parcel value that was used to calculate population in the buffer areas.

Zip Code Population / Parcel value total = Zip code parcel value.



Figure 8. Parcels within the census blocks intersection. One inch = 5 miles.

Once a zip code parcel value was calculated for the parcels in each zip code, that value was used to determine the population of the parcels in the census blocks not completely contained in the buffer.

The next calculation was for the

parcels in the census blocks that were not completely contained in the buffer. The buffer parcels were again divided into the four categories. Their values were calculated and totaled. This total was then multiplied by the parcel value for each zip code (Appendix B).

Buffer value total x Parcel value = Buffer zip code population count.

The counts were then be totaled. This was the total of the population in the parcels of the census blocks not completely contained in the buffer. This count is 6,351 (Appendix B). When added to the nested census block population (43,521), the total population of the buffer is 43,521 + 6,351, or 49,872.

In most dasymetric approaches to areal interpolation, the counts are divided into populated versus unpopulated. With the data already acquired, this calculation can be performed also. In Table 4, the parcels were divided into "No Population" versus "Population."

No Population = 0 Population = 1

A new parcel value for each zip code was calculated as shown below.

Zip code population/ Total parcel value = Parcel value.

This value was used to calculate the buffer population counts per each zip code and then was totaled. When this amount was added to the nested census block totals, the total population for the buffer was 43,521 + 6,353 = 49,874 (Appendix C).

#### Results

This study compared two population

distribution models. Simple areal weighting averages population counts within a zone. In this study, the zones were zip code areas. Dasymetric interpolation involved more analysis, area selection, and calculations. The difference in the results between the two distribution models was that with simple areal weighting, the total population was estimated to be 59,836 and for dasymetric interpolation, it was 49,872. When the categories in the dasymetric interpolation were changed from 4 categories to 2 categories, the total population is 49,874.

Simple Areal Weighting	= 59,836
Dasymetric (4 categories)	= 49,872
Dasymetric (2 categories)	= 49,874

In Figure 9, all parcels are shown for all zip codes. In eastern zip codes (55327, 55316, and 55445), there are areas of no population in the buffer. The parcels would be commercial, industrial, farmland or public lands such as parks, schools, government buildings. These would skew the results in the simple areal interpolation. The areas that have no population would be calculated into the totals. This is the over-estimation that Holt (et al., 2004) discusses and is shown in the representation of population in this study (Figure 9).

Figure 10 is a "close up" of the zip code 55369. The light grey areas represent areas where there is no population. This shows that the hospital is being built in a commercial area. What appears to be dark grey areas are areas of smaller single family houses. These darker areas have more population and are visible with dasymetric interpolation. This difference between areas of no population and dense population would not be visible by simple area weighting.

Though dasymetric interpolation distributes population more accurately, it is



Figure 9. Zip Codes with Parcels and 5 Mile Buffer Boundary. (NOP = No Population; DU = Duplex; CT = Condominium/Townhouse; SFF = Single Family/Farm). One inch = 2.5 miles.

subjective to what categories are chosen. The values for single family/farms were based on the assumption that a single family is 2 adults and 2 children; therefore, the value is 4. For condo/townhouse value of 3, it is based on the reasoning that there would be more single parents and 2 children or a young family with 1 child. For duplex, the value is given for 2 people. As for commercial, industrial and public lands, they do not have residents or population. Apartments were given a value of 4. That would be very low and not represent the population of apartments. However, it would be difficult to know how many units are in each apartment building without researching each building.

Even with this subjective choice, the results did not show much difference between using 4 categories or 2 categories for the dasymetric interpolation. This was consistent with research conducted by Eicher and Brewer (2001). They performed dasymetric interpolation using a polygon



Figure 10. Close up of zip code area. One inch = 2.5 miles.

binary method and grid three-class method of interpolation and did not find significant difference between the 2 types. Also, in research performed by Langford (2003), 3class dasymetric interpolation was compared to binary dasymetric interpolation and it was found the binary or two-class dasymetric method performed better. In both of these examples of comparing two-class populated/unpopulated) to 3 classes (urban/forested/agricultural) or (urban/dense/suburban), the difference between the two methods was not significant.

# Conclusions

Dasymetric interpolation has been shown to more accurately re-distribute population than simple areal interpolation. With increasingly more powerful computers and the use of GIS, this analysis is possible. However, there is not great use of this technique among the GIS community (Langford, 2004). Simple areal weighting is much easier to perform and does not require any extra ancillary data. The perceived cost of the ancillary data, added time and complexity of dasymetric interpolation hinders its use. There is familiarity with the simple areal weighting and a lack of awareness of other possibilities, such as dasymetric interpolation.

Even though dasymetric mapping does represent data more closely to actual population density, it still estimates the population. This estimation of what most likely is occurring can be mapped and shown using dasymetric interpolation (Poulsen and Kennedy, 2004). With any population distribution, individuals become population distributed to patterns or areas. These patterns or areas are very helpful in socio-demographic analysis. However, we are individuals and not estimations.

#### Acknowledgements

I would like to thank Cliff Moyer for his insight and technical assistance on this study, as well as Robert Moulder and William Brown for the use of the datasets. I would also like to thank John Ebert and Dr. Dave McConville of the Resource Analysis staff at Saint Mary's University of Minnesota for his guidance through this process.

## References

Cai, Q. 2006. Estimating Small-Area Population by Age and Sex Using Spatial Interpolation and Statistical Inference Methods. *Transitions in GIS*, *10*, 577-598. Retrieved January 2008 from EBSCO database.

Eicher, C. L. and Brewer, C. 2001. Dasymetric Mapping and Areal Interpolation: Implementation and Evaluation. *Cartography and Geographic Information Science*, 20, 125-138. Retrieved February 2008 from EBSCO database.

Grubesic, T. H. 2006. Zip Codes and Spatial Analysis: Problems and Prospects. Socio-Economic Planning Sciences, *42*, 129-149. Retrieved January 2008 from Elsevier Ltd. Database.

Holt, J. B., Lo, C. P., and Holder, T. W.
2004. Dasymetric Estimations of Population Density and Areal Interpolation of Census Data. *Cartography and Geographic Information Science*, *31*, 103-121.Retrieved January 2008 from SMU Interlibrary Loan.

- Langford, M. 2003. Obtaining Population Estimates in Non-Census Reporting Zones: An Evaluation of the 3-class Dasymetric Method. *Computers, Environment and Urban Systems, 30*, 161-180. Retrieved January 2008 from Science Direct database.
- Langford, M. 2004. Rapid Facilitation of Dasymetric-Based Population Interpolation is Means of Raster Pixel Maps. *Computers, Environment and Urban Systems*, 31, 19-32. Retrieved January 2008 from Elsevier Ltd. database.
- Langford, M., Higgs, G., Radcliffe, J., and White, S. 2006. Urban population Distribution Models and Service Accessibility Estimation. *Computers, Environment and Urban Systems, 32,* 66-80. Retrieved January 2008 from Science Direct database.
- Mennis, J. 2003. Generating Surface Models of Population Using Dasymetric Mapping. *The Professional Geographer*, 55, 31-42. Retrieved February 2008 from Science Press. 297 pp.

Poulsen, E. and Kennedy, L. 2004. Using Dasymetric Mapping for Spatially Aggregated Crime Data. *Journal of Quantitative Criminology*, 20, 243-262. Retrieved January 2008 from EBSCO database.

ZIP CODE		Commercial Industry Value = 0	Duplex Value = 2	Condo Townhouse Value = 3	Single Family/ Farm value = 4	Totals	Population	Zip Code Parcel Value
55311							19827	0.48
	parcels	1675	17	3355	7764	12811		
	values	0	34	10065	31056	41155		
55316							22422	0.77
	parcels	672	83	937	6785	8477		
	values	0	186	1874	27140	29200		
55327							3502	0.69
	parcels	348	0	1	1263	1612		
	values	0	0	3	5052	5055		
55340							5836	0.76
	parcels	802	4	123	1820	2749		
	values	0	2	369	7280	7651		
55369							33294	0.78
	parcels	1648	75	2671	8653	13047		
	values	0	150	8013	34612	42775		
55374							9317	0.62
	parcels	1403	11	420	3462	5296		
	values	0	22	1260	13848	15130		
55428							29933	0.95
	parcels	656	110	801	7196	8763		
	values	0	220	2403	28784	31407		
55442							13196	0.80
	parcels	314	11	1321	3143	4789		
	values	0	22	3963	12572	16557		
55445							8853	0.72
	parcels	633	32	1135	2224	4024		
	values	0	64	3405	8896	12365		
55446							12464	0.58
	parcels	1002	6	2735	3286	7029		
	values	0	12	8205	13144	21361		

Appendix A. Calculated zip code parcel value.

BUFFER ZIP CODE		NOP value = 0	DU value=1	CT value = 3	SFF value = 4	Buffer Value Total	Zip Code Parcel Value	Buffer Population Total
55311								
	parcels	124	1		225		0.48	
	values	0	2		900	902		433
55316								
	parcels	59	32		675		0.77	
	values	0	64		2700	2764		2128
55327								
	parcels	19	1		131		0.69	
	values	0	2		524	526		363
55340								
	parcels	32			170		0.76	
	values	0			680	680		517
55369								
	parcels	64	3	133	250		0.78	
	values	0	6	399	1000	1405		1096
55374								
	parcels	35	2	82	187		0.62	
	values	0	4	246	748	998		619
55428								
	parcels	12			7		0.95	
	values	0			28	28		27
55442								
	parcels						0.80	
-	values							
55445								
	parcels	70		187	125		0.72	
	values	0		561	500	1061		764
55446								
	parcels	175	59	28	124		0.58	
	values	0	118	84	496	698		405
								6351

#### Appendix B. Use parcel value to calculate buffer population.

ZIP CODE		No Population value = 0	Populated value=1	Totals	Zip Code Population		Zip Code Parcel Value	Buffer No Pop.	Buffer Populated	Buffer Value Total	Buffer Pop. Total
55311					19827						
	parcels	1675	11136	12811			1.78	124	226		
	values	0	11136	11136		-		0	226	226	402
55316					22422						
	parcels	672	7805	8477		-	2.87	59	707		
	values	0	7805	7805		-		0	707	707	2031
55327					3502						
	parcels	348	1264	1612			2.77	19	231		
	values	0	1264	1264		-		0	132	132	366
55340					5836						
	parcels	802	1947	2749			3.00	32	170		
	values	0	1947	1947		-		0	170	170	510
55369					33294						
	parcels	1648	11399	13047			2.92	64	383		
	values	0	11399	11399				0	383	383	1119
55374					9317						
	parcels	1403	3893	5296			2.39	35	271		
	values	0	3893	3893		-		0	271	271	649
55428					29933						
	parcels	656	8107	8763		-	3.69	12	7		
	values	0	8107	8107				0	7	7	26
55442					13196	-					
	parcels	314	4475	4789			2.95				
	values	0	4475	4475							
55445					8853	-		70	312		
	parcels	633	3391	4024		-	2.61	0	312	312	815
	values	0	3391	3391							
55446					12464			175	211		
	parcels	1002	6027	7029			2.07	0	211	211	436
	values	0	6027	6027							
											6353

Appendix C. Buffer counts using Population versus No Population.